



Instance-level recognition

Local invariant features, correspondence, image matching

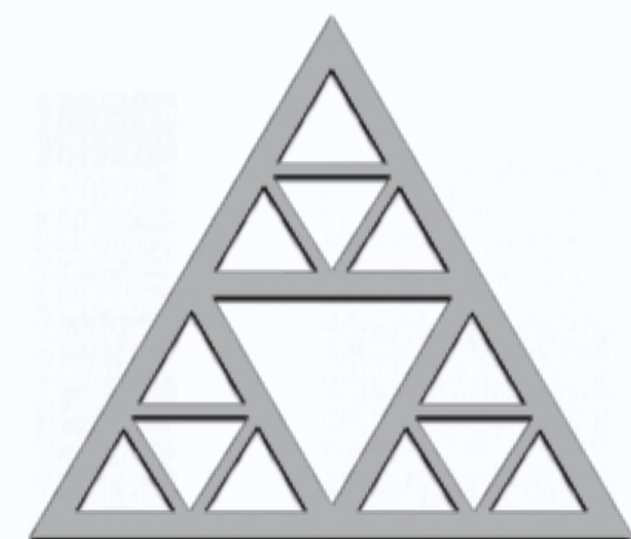
Gül Varol

IMAGINE team, École des Ponts ParisTech

gul.varol@enpc.fr

<http://imagine.enpc.fr/~varolg/>

@RecVis, 10.10.2023



École des Ponts
ParisTech

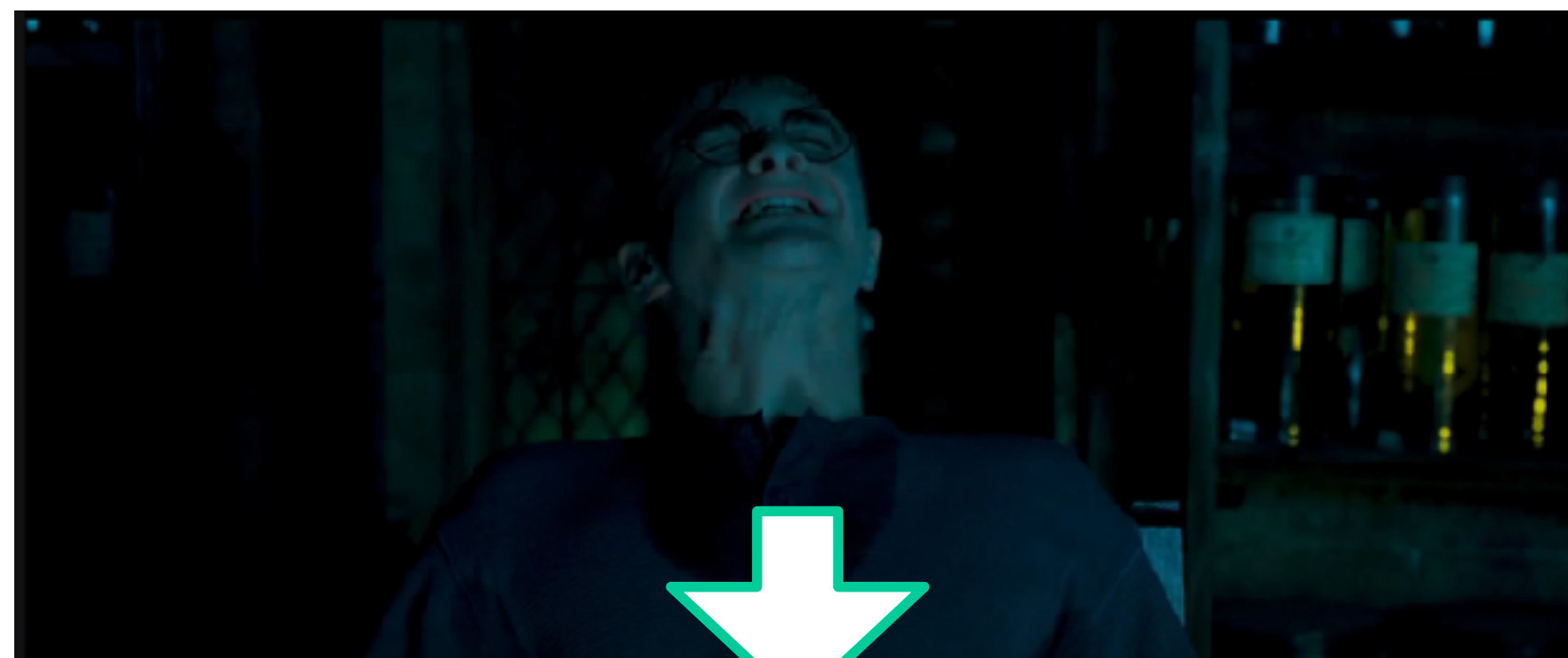


<https://app.sli.do/event/6XF9sNDPBQ1W9mSRdDBzHM>

My research

Computer Vision

- Vision & **Language**
- Text-to-**Video** retrieval
- **Sign** language videos
- 3D **Human motion** generation
- Movie description
- ...

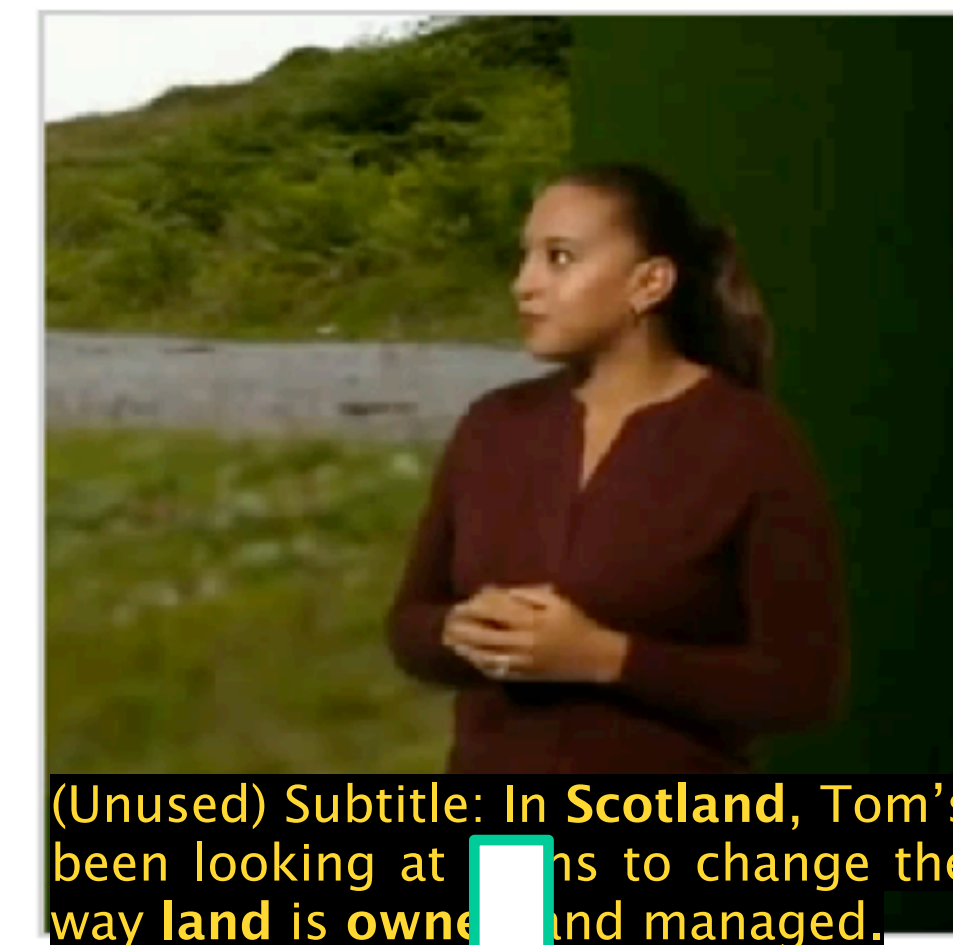
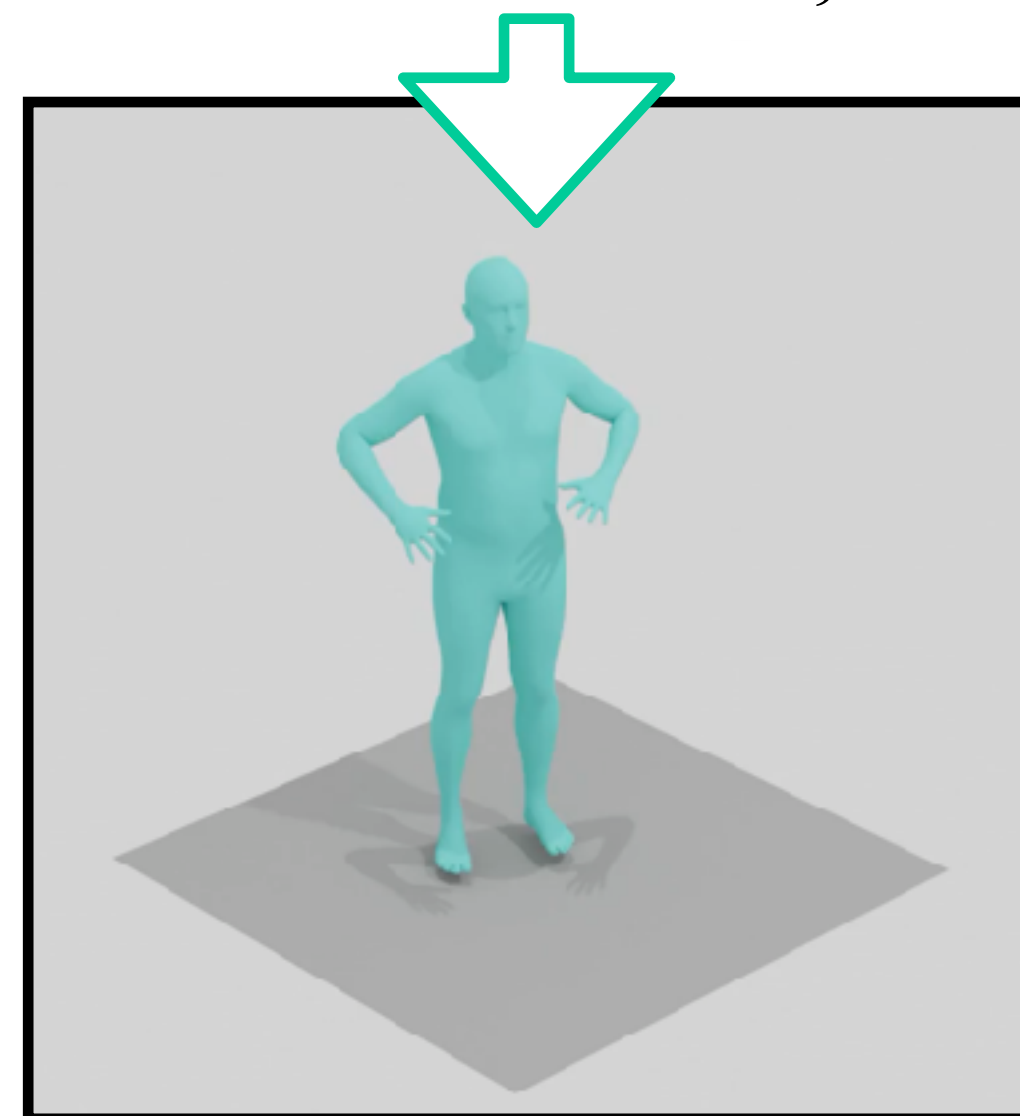


Predicted Audio Description: Snape points at Harry. Harry's eyes close in horror.

"prune this plant"



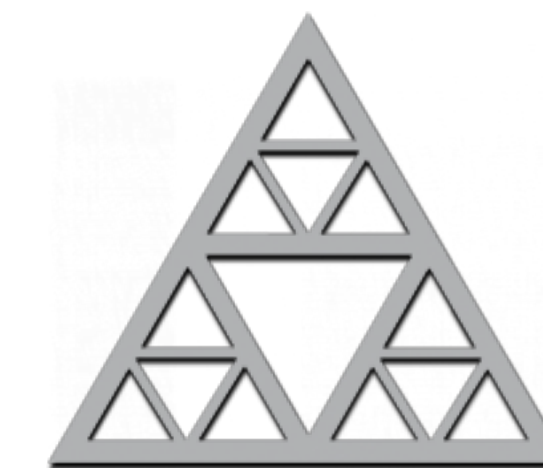
{ put hands on the waist,
move torso left }



(Unused) Subtitle: In **Scotland**, Tom's been looking at **ns** to change the way **land** is **owne** and managed.

Ours	scotland	research	land	own	noise	competition	good
GT	scotland	investigate	land	own	who	competition	we alright

IMAGINE computer vision team, ENPC



École des Ponts
ParisTech

imagine.enpc.fr/



Keep an eye on internships

Announcements

- Assignment 1 out today, due Tuesday Oct 24
- Google Classroom: Register with the code **wbj5g7w**.
- Fill the form on the class webpage to participate the Pytorch tutorial.

Instance-level recognition

Last week (J. Ponce): Introduction to vision, camera geometry, image processing

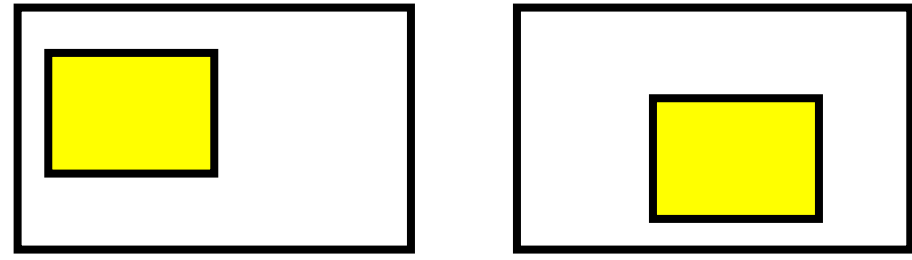
This week (G. Varol): Instance-level recognition

Next week (TAs): Python/Pytorch tutorial at Inria

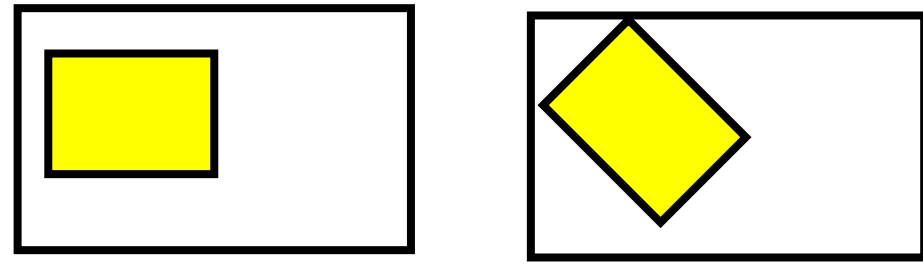
In 2 weeks (A. Joulin): Supervised learning, Introduction to deep learning

Recap: geometry

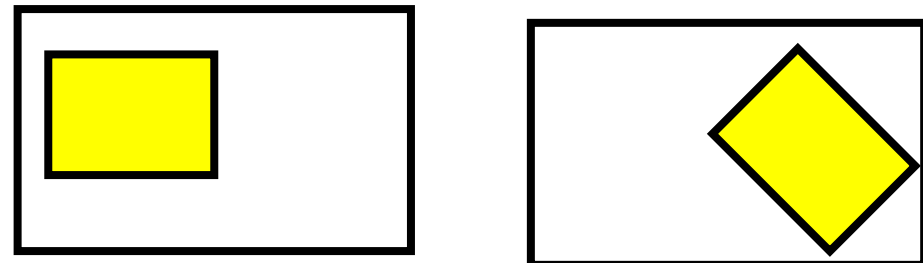
Hierarchy of 2D Geometric Transformations



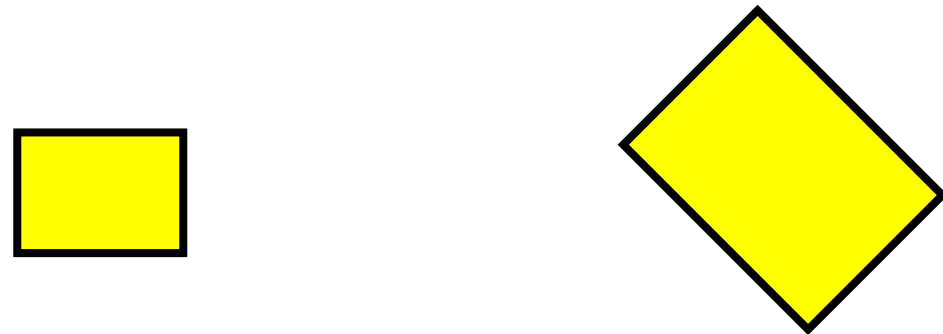
- Translation (T)



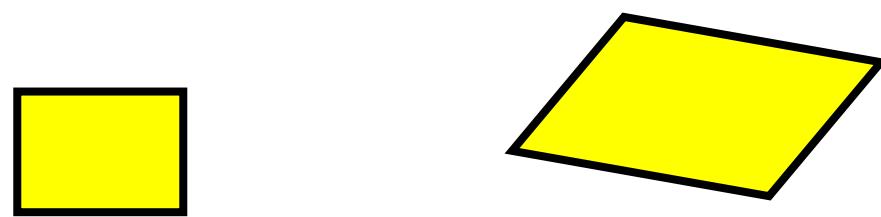
- Rotation (R)



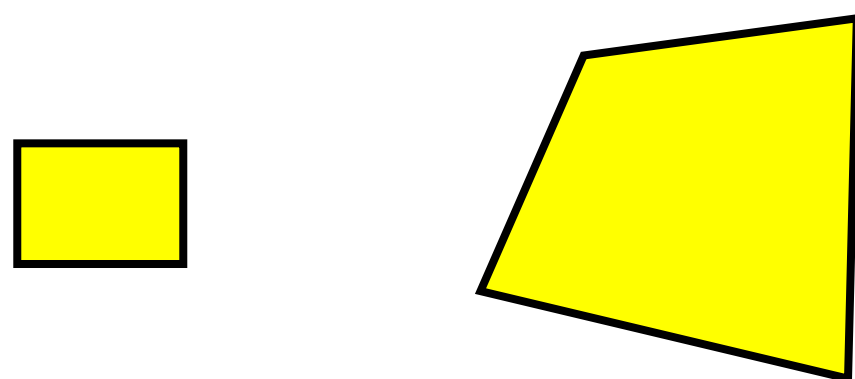
- Euclidean / Rigid (R+T)



- Similarity (+ scaling)



- Affine (+ shear)



- Projective / Homography

$$\begin{bmatrix} r_{11} & r_{12} & t_x \\ r_{21} & r_{22} & y_y \\ 0 & 0 & 1 \end{bmatrix}$$

Preserves:

Lengths, angles

$$\begin{bmatrix} sr_{11} & sr_{12} & t_x \\ sr_{21} & sr_{22} & y_y \\ 0 & 0 & 1 \end{bmatrix}$$

Angles, ratios of lengths

$$\begin{bmatrix} a_{11} & a_{12} & t_x \\ a_{21} & a_{22} & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

Parallelism

$$\begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix}$$

Collinearity

Agenda: Instance-level recognition

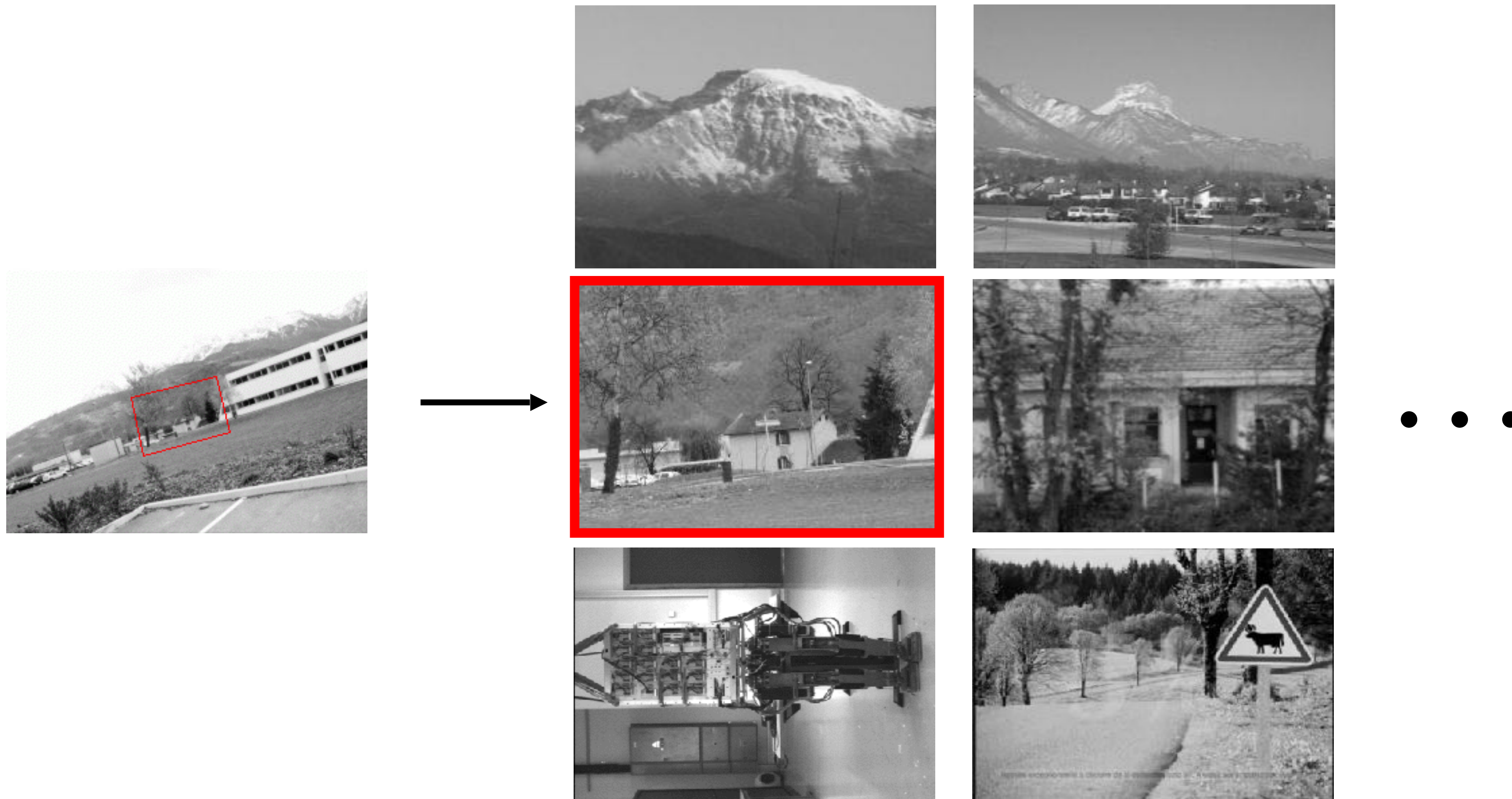
- 1) Introduction to local features
- 2) Interest point detectors (e.g., Harris, scale invariance)
- 3) Comparison of patches (SSD, ZNCC on pixel values)
- 4) Feature descriptors (e.g., SIFT)
- 5) Matching and recognition with local features
- 6) Local feature aggregation for a single image-level description

Agenda: Instance-level recognition

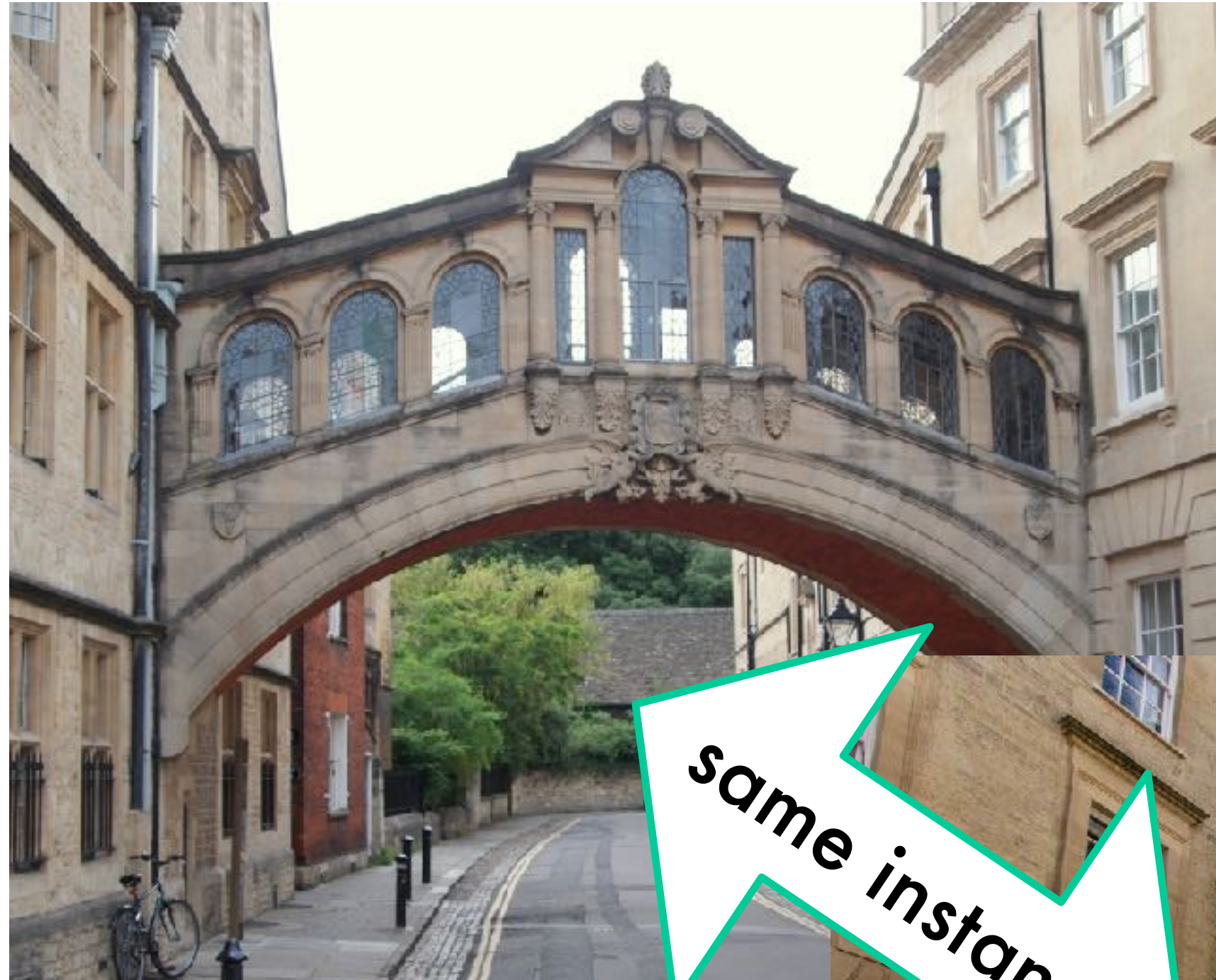
- 1) Introduction to local features
- 2) Interest point detectors (e.g., Harris, scale invariance)
- 3) Comparison of patches (SSD, ZNCC on pixel values)
- 4) Feature descriptors (e.g., SIFT)
- 5) Matching and recognition with local features
- 6) Local feature aggregation for a single image-level description

Instance-level recognition

Search for particular objects and scenes in large databases



Instance-level vs Category-level



Bridge of Sighs, Oxford



Pont Neuf, Paris

same instance

same category

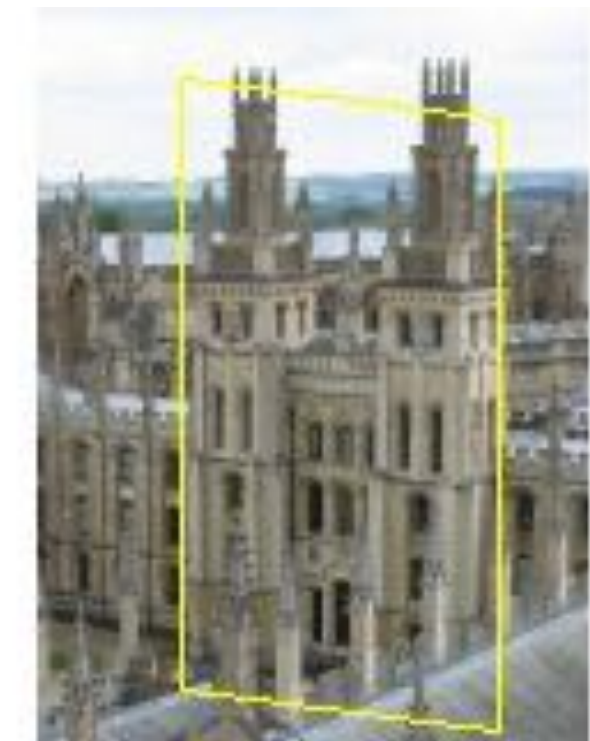


Difficulties

Finding the object despite possibly large changes in scale, viewpoint, lighting and partial occlusion → **requires invariant description**



Scale



Viewpoint



Lighting



Occlusion

Difficulties

- Very large image collections → **need for efficient indexing**
 - ➔ Flickr has 2 billion photographs, more than 1 million added daily*
 - ➔ Facebook has 15 billion images (~27 million added daily)*
 - ➔ Large personal collections

*Potentially outdated numbers

Applications

Search photos on the web for particular places

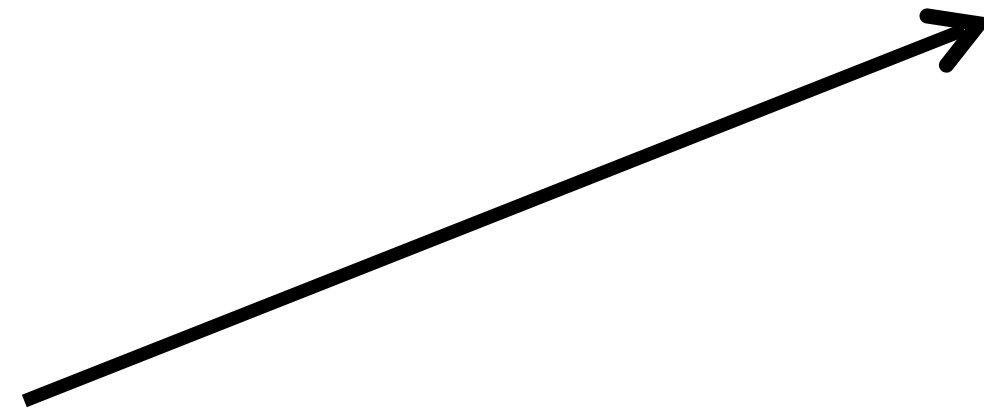


Find these landmarks

...in these images and 1M more

Applications

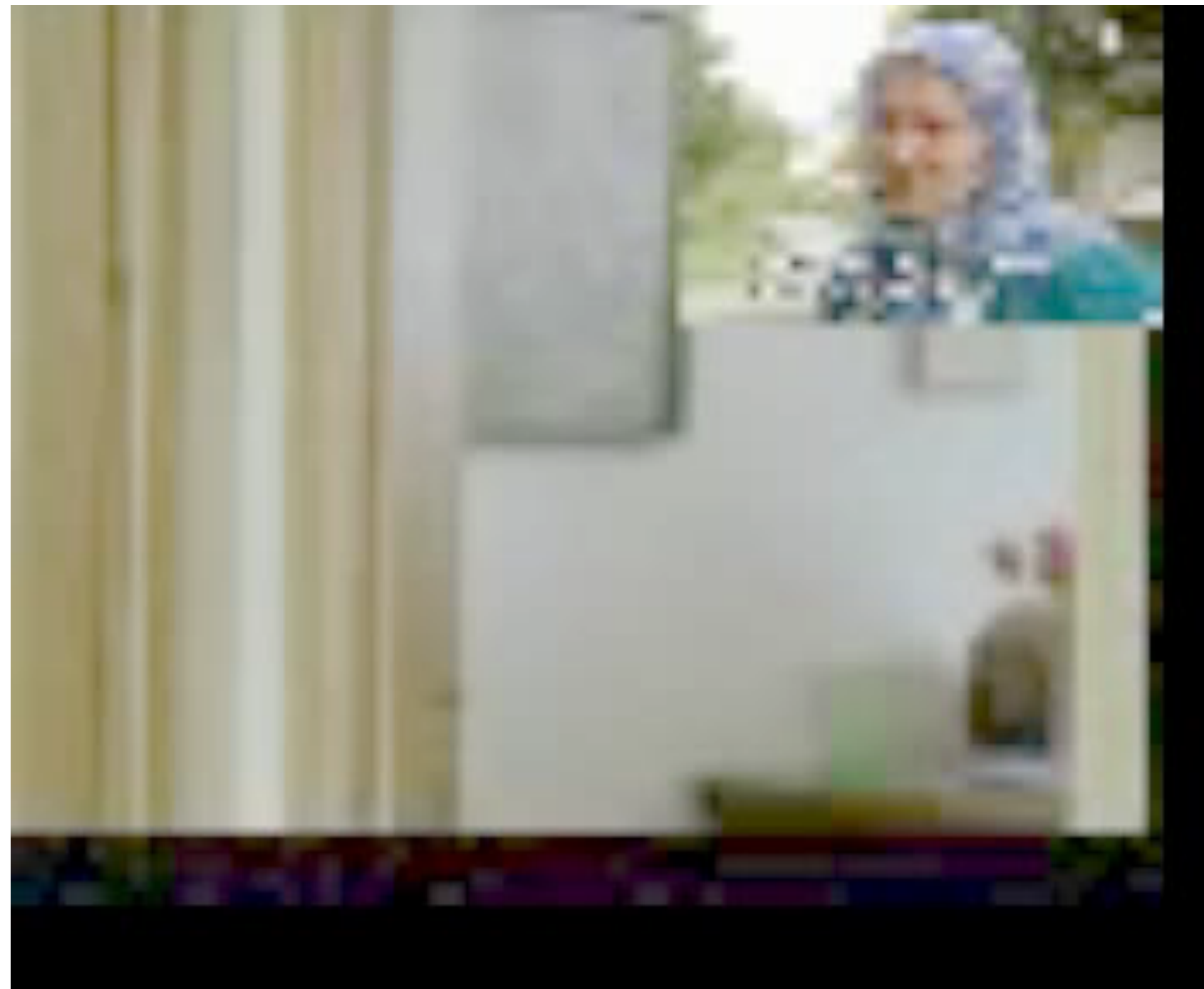
- Finding stolen/missing objects in a large collection



Applications

- Copy detection for images and videos

Query video

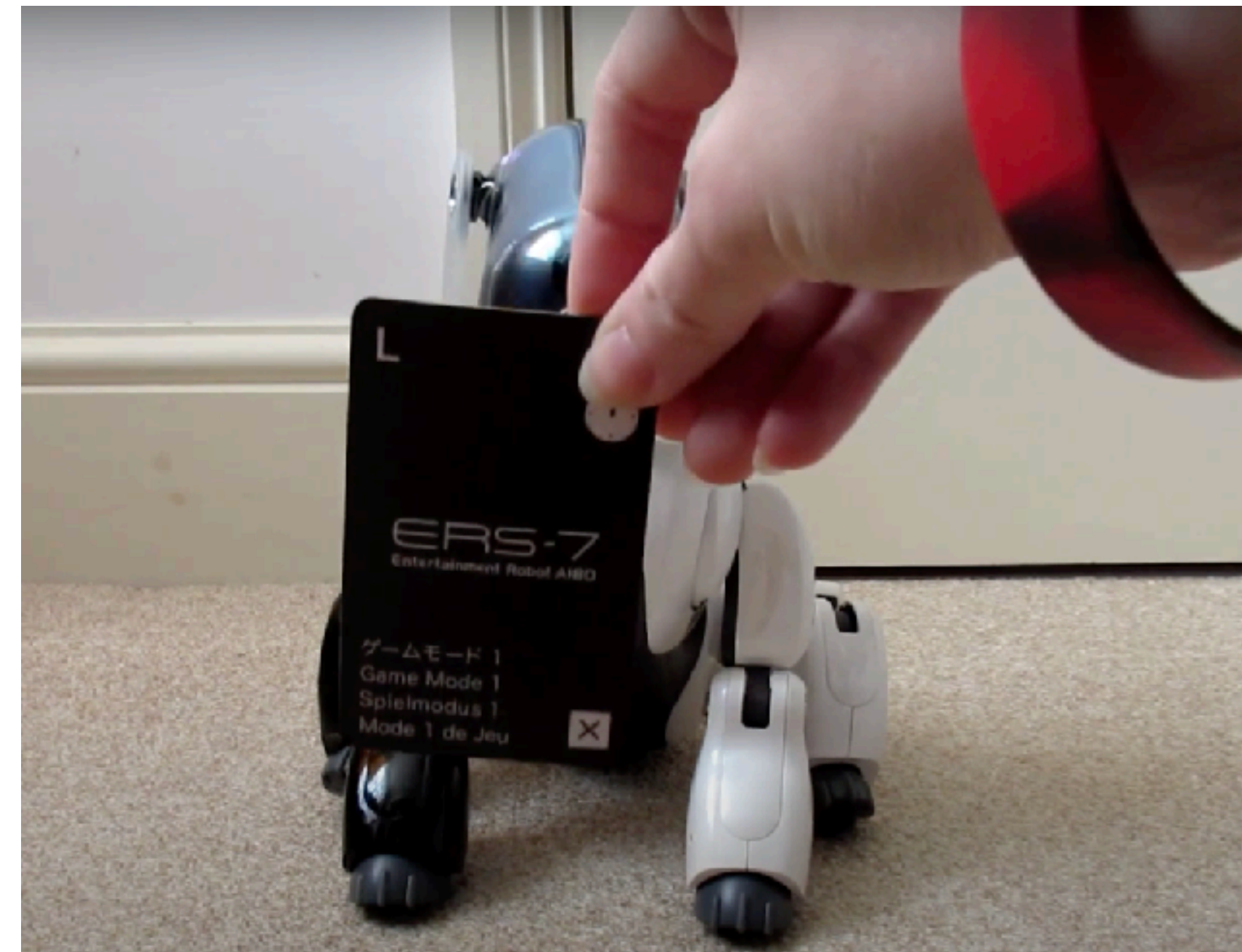


Search in 200h of video



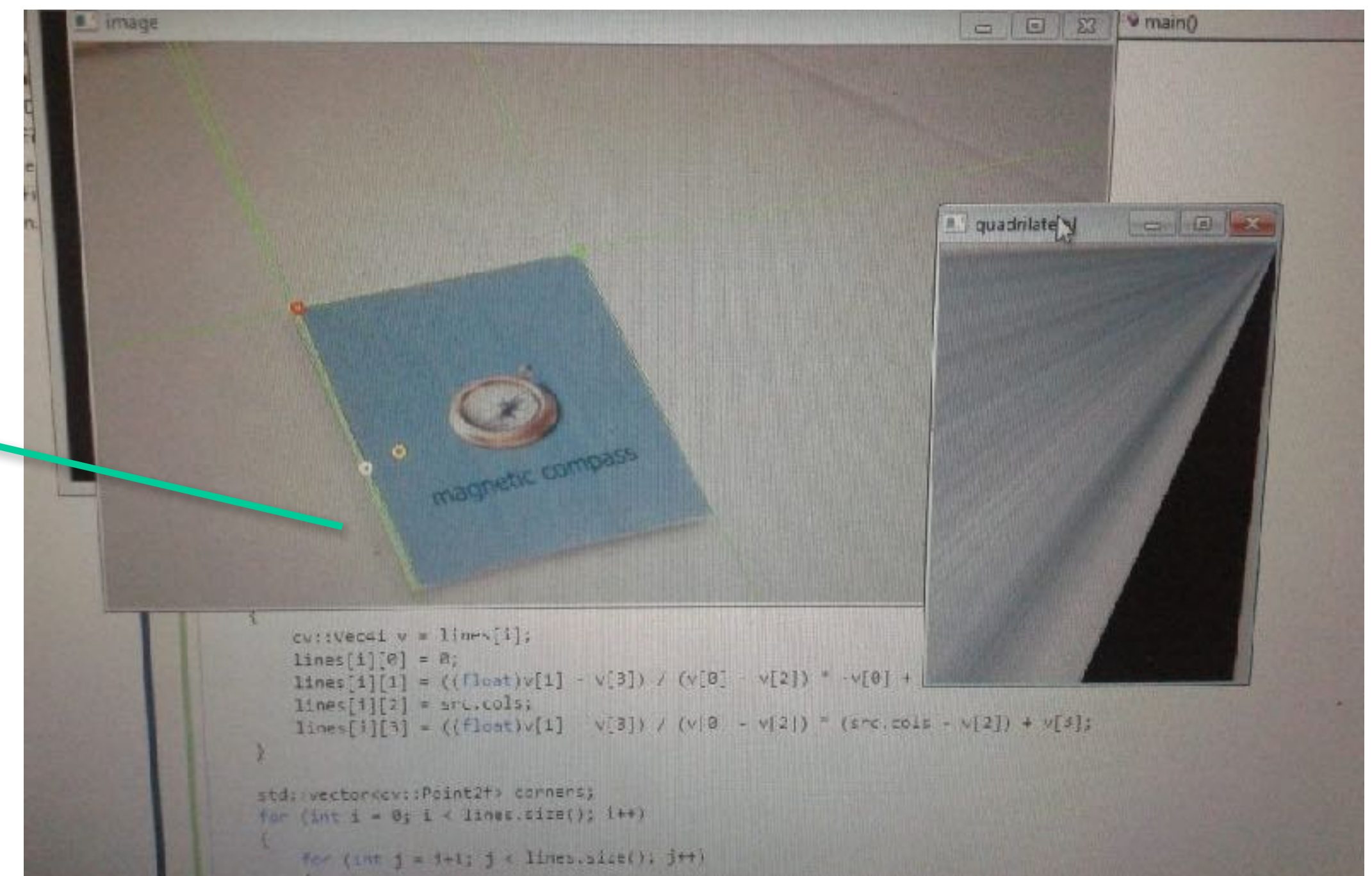
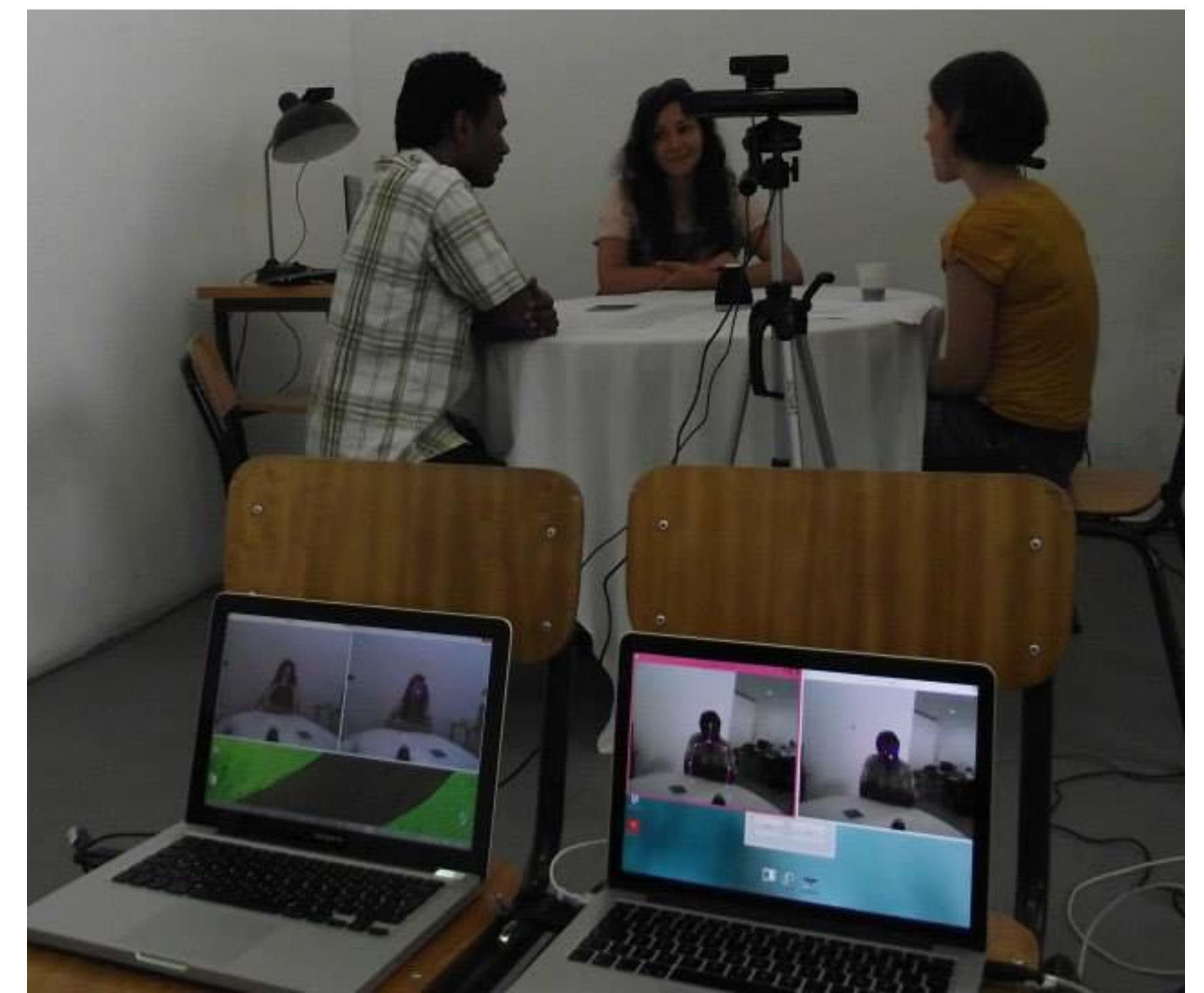
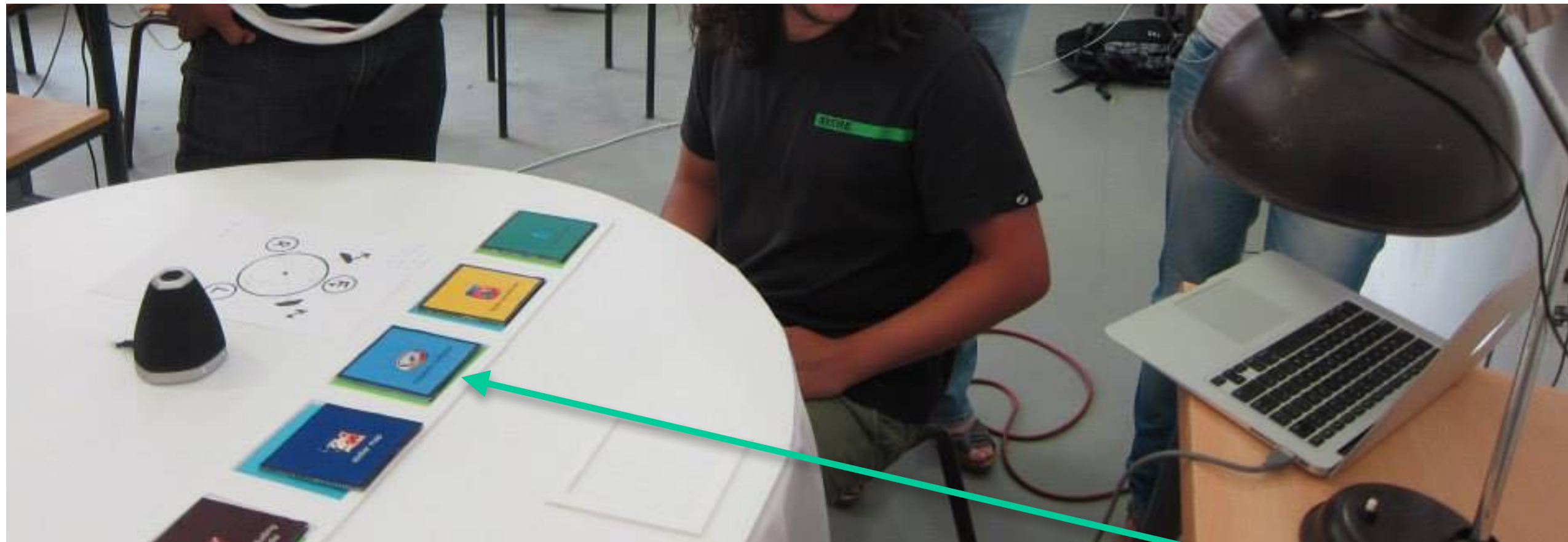
Applications

- Sony Aibo – Robotics
 - Recognize docking station
 - Communicate with visual cards
 - Place recognition
 - Loop closure in SLAM



Applications

- Template matching



Agenda: Instance-level recognition

1) Introduction to local features

2) Interest point detectors (e.g., Harris, scale invariance)

3) Comparison of patches (SSD, ZNCC on pixel values)

4) Feature descriptors (e.g., SIFT)

5) Matching and recognition with local features

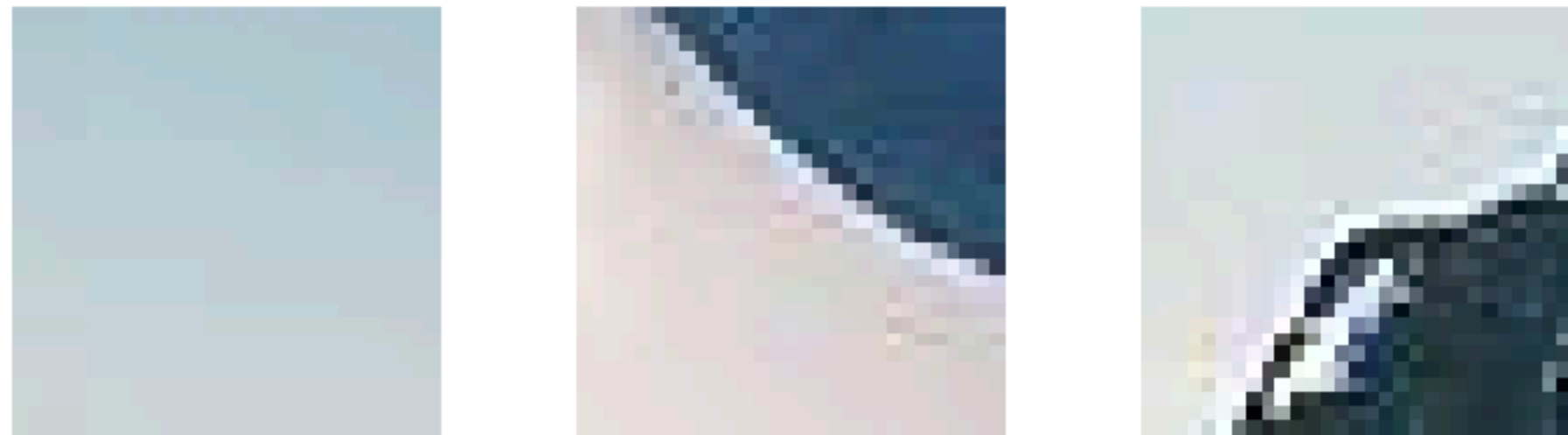
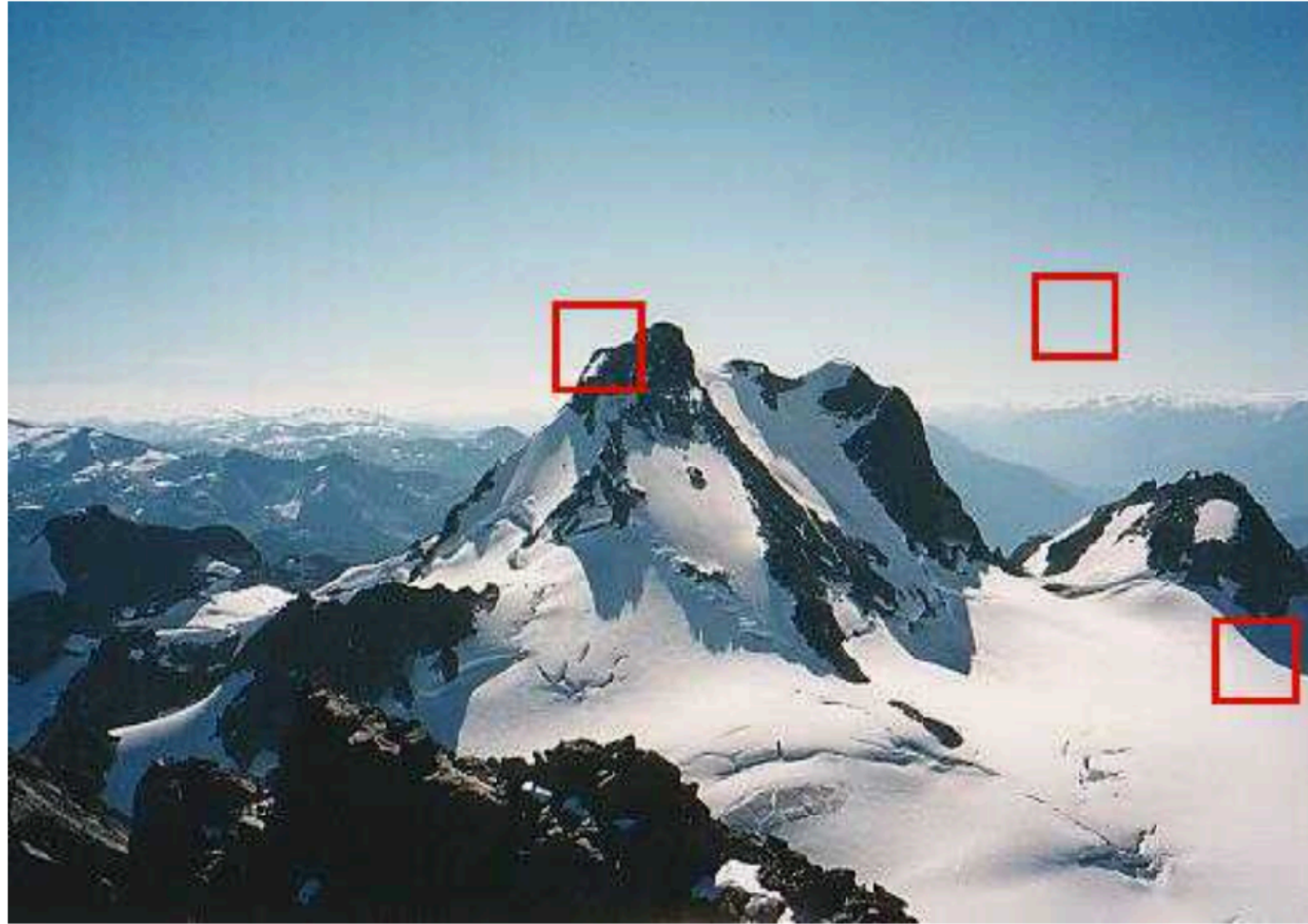
6) Local feature aggregation for a single image-level description



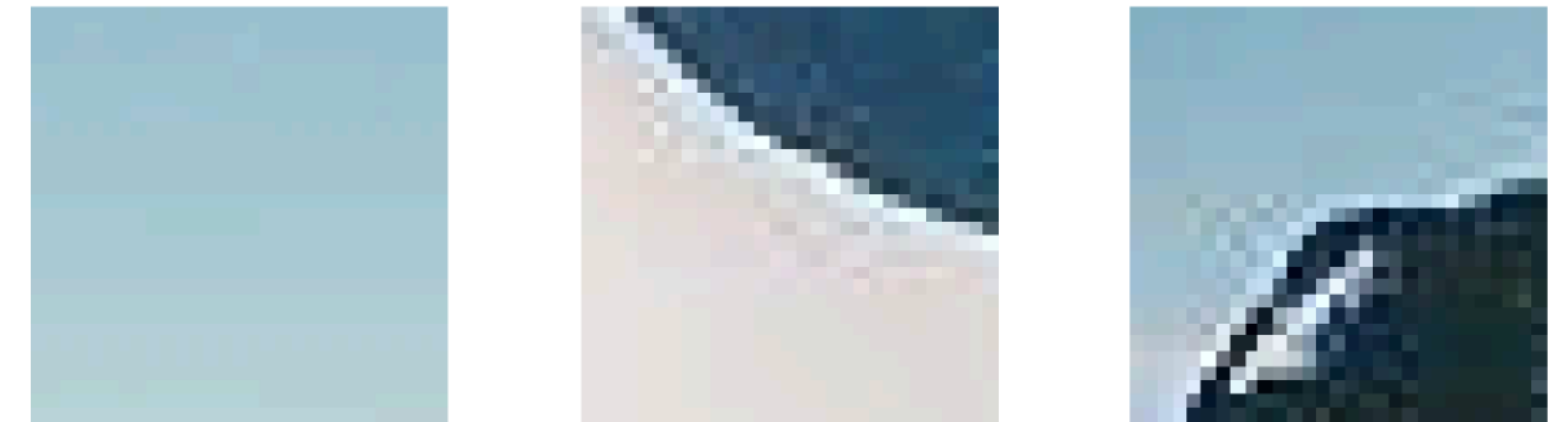
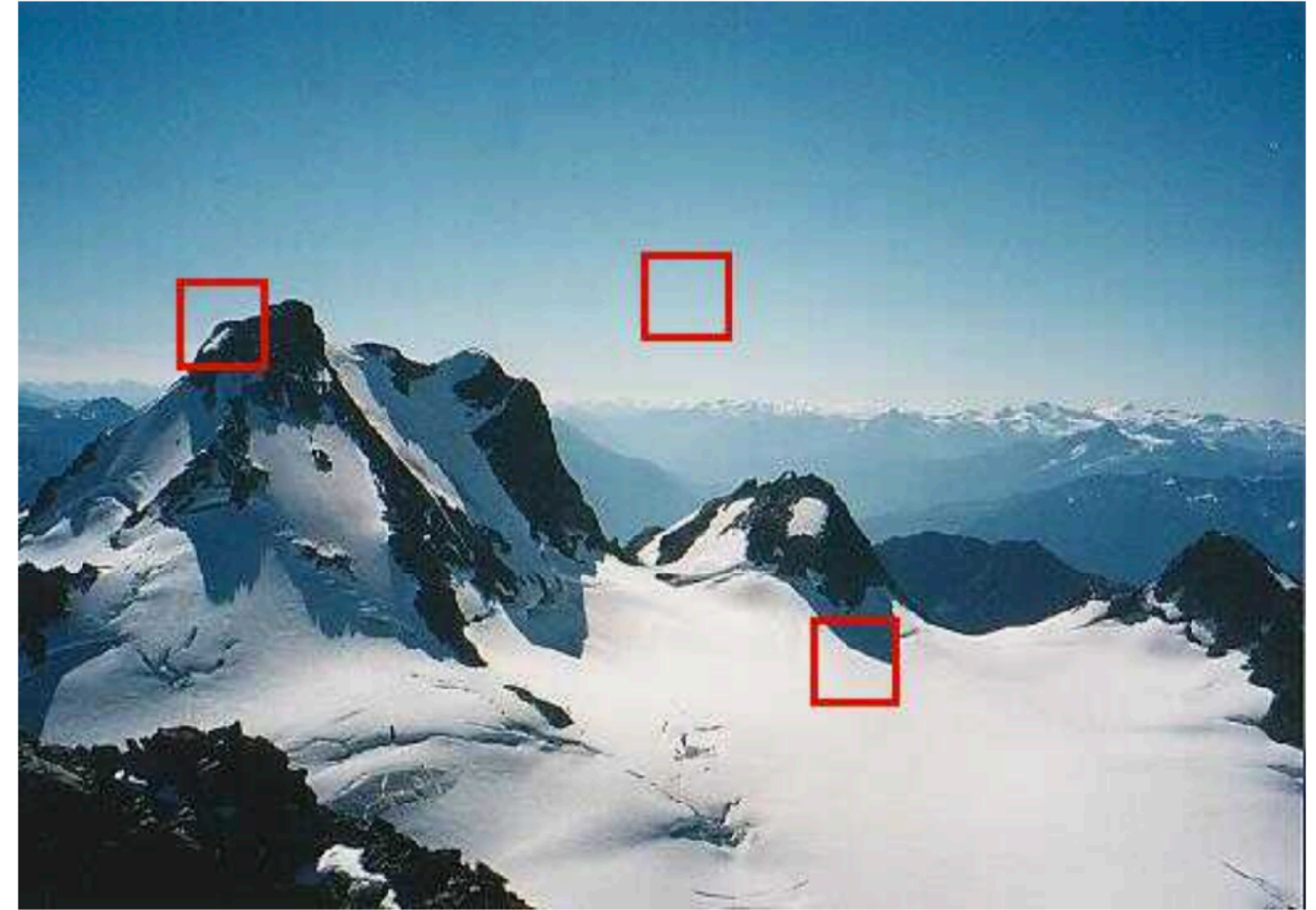
Two pairs of images to be matched. What kinds of features might one use to establish a set of correspondences between these images?



Figure 7.2 Szeliski



Textureless patches are nearly impossible to localize.



Patches with large contrast changes (gradients) are easier to localize.

Figure 7.3 Szeliski

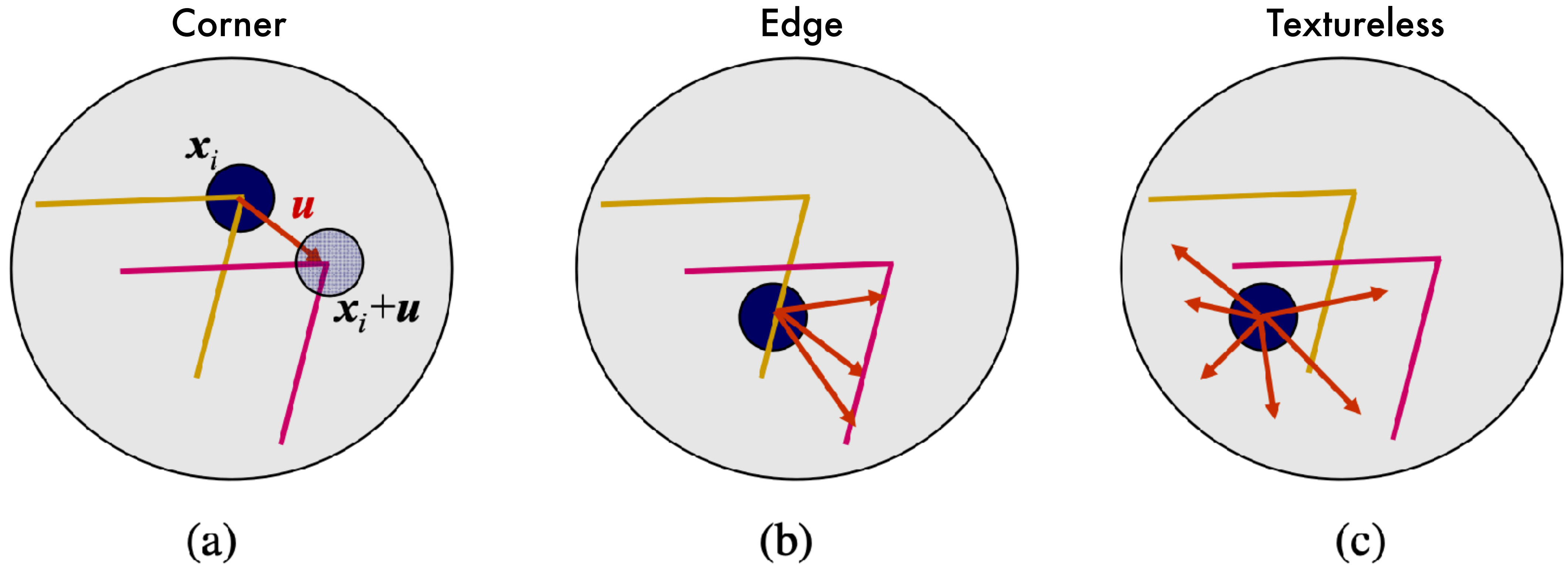
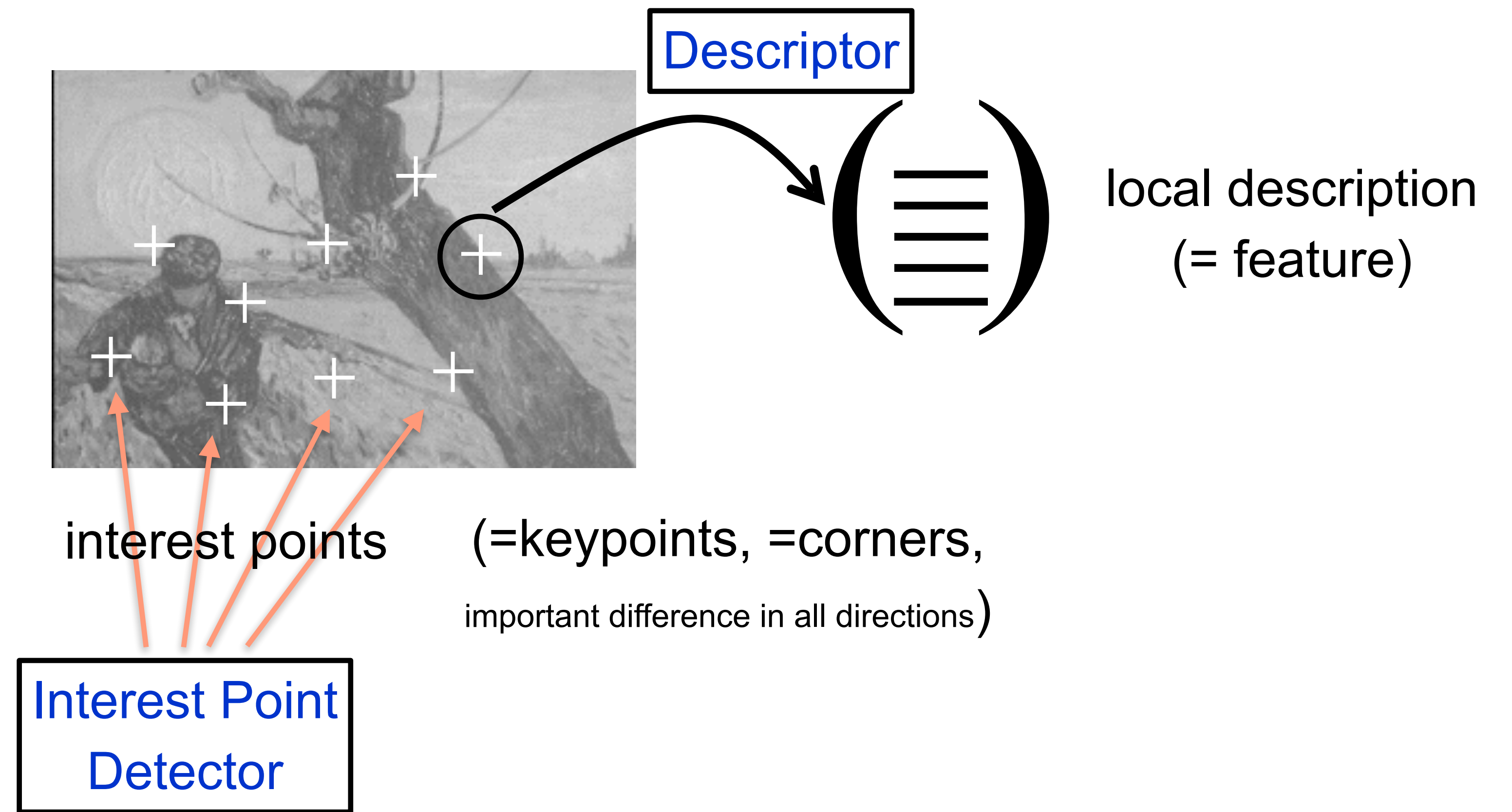


Figure 7.4 Aperture problems for different image patches: (a) stable (“corner-like”) flow; (b) classic aperture problem (barber-pole illusion); (c) textureless region. The two images I_0 (yellow) and I_1 (red) are overlaid. The red vector \mathbf{u} indicates the displacement between the patch centers and the $w(\mathbf{x}_i)$ weighting function (patch window) is shown as a dark circle.

Local features



A **corner** is a point whose **local neighborhood** stands in two dominant and different edge directions. In other words, a corner can be interpreted as the junction of two edges, where an edge is a **sudden change in image brightness**. Corners are the important features in the image, and they are generally termed as **interest points** which are **invariant to translation, rotation and illumination**. Although corners are only a small percentage of the image, they contain the **most important features** in restoring image information... [Harris corner detection, Wikipedia]

Interest points / invariant regions



Harris detector

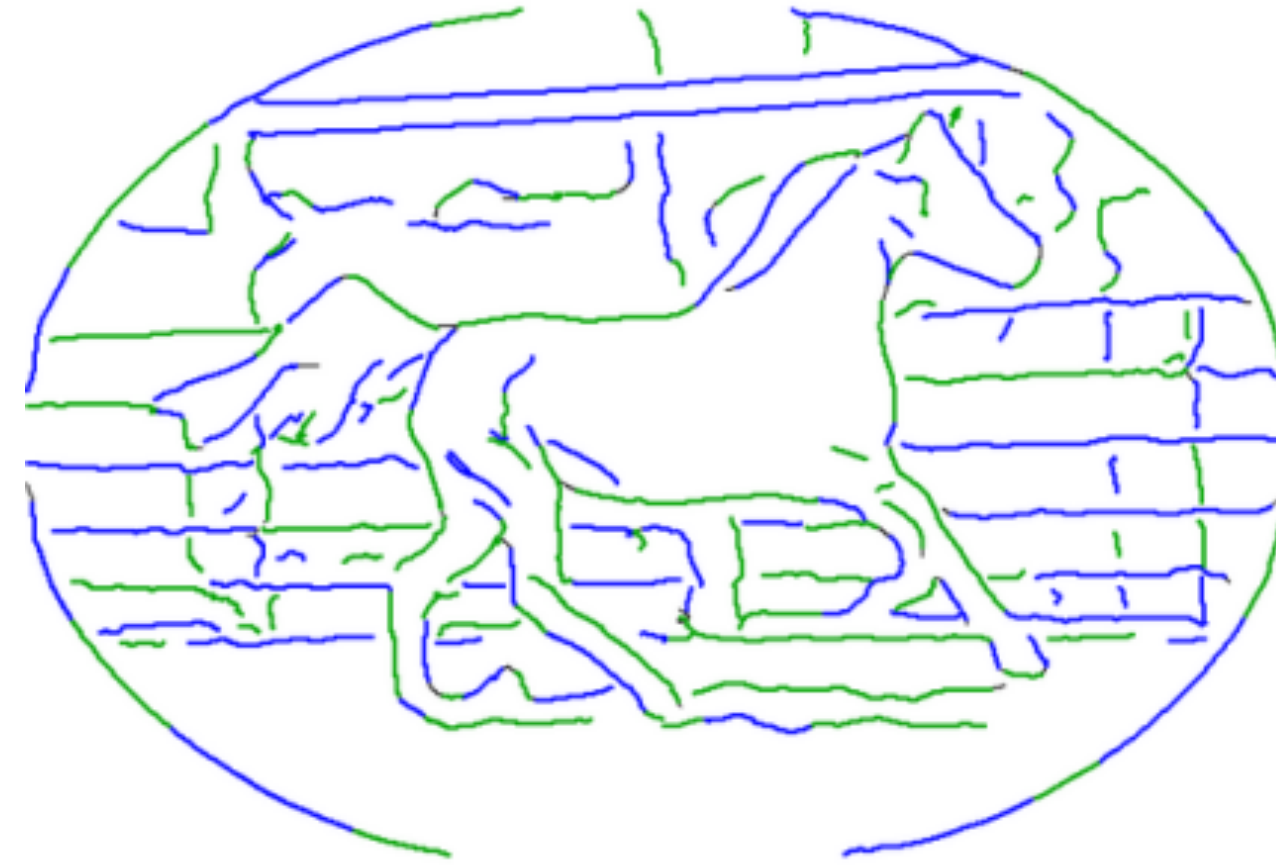


Scale invariant detector

Contours / lines

- **Extraction of contours**

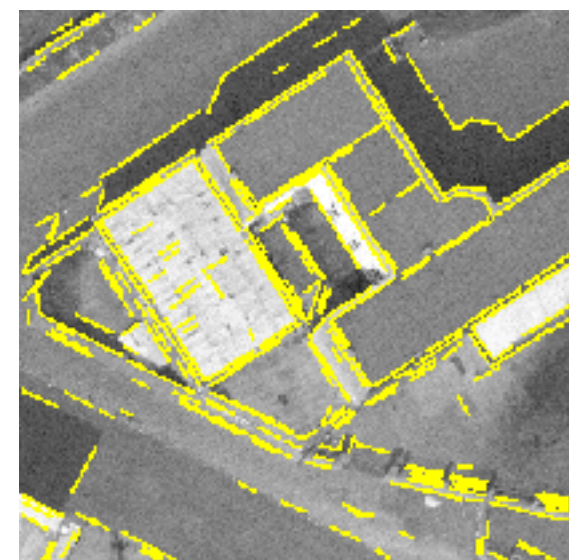
- Zero crossing of Laplacian
- Local maxima of gradients



- **Chain contour points (hysteresis) , Canny detector**

- **Contour detectors**

- Global probability of boundary (gPb) detector [Malik et al., UC Berkeley, CVPR'08]
- Structured forests for fast edge detection (SED) [Dollar and Zitnick, ICCV'13]



Regions segments / superpixels

original image



ground truth



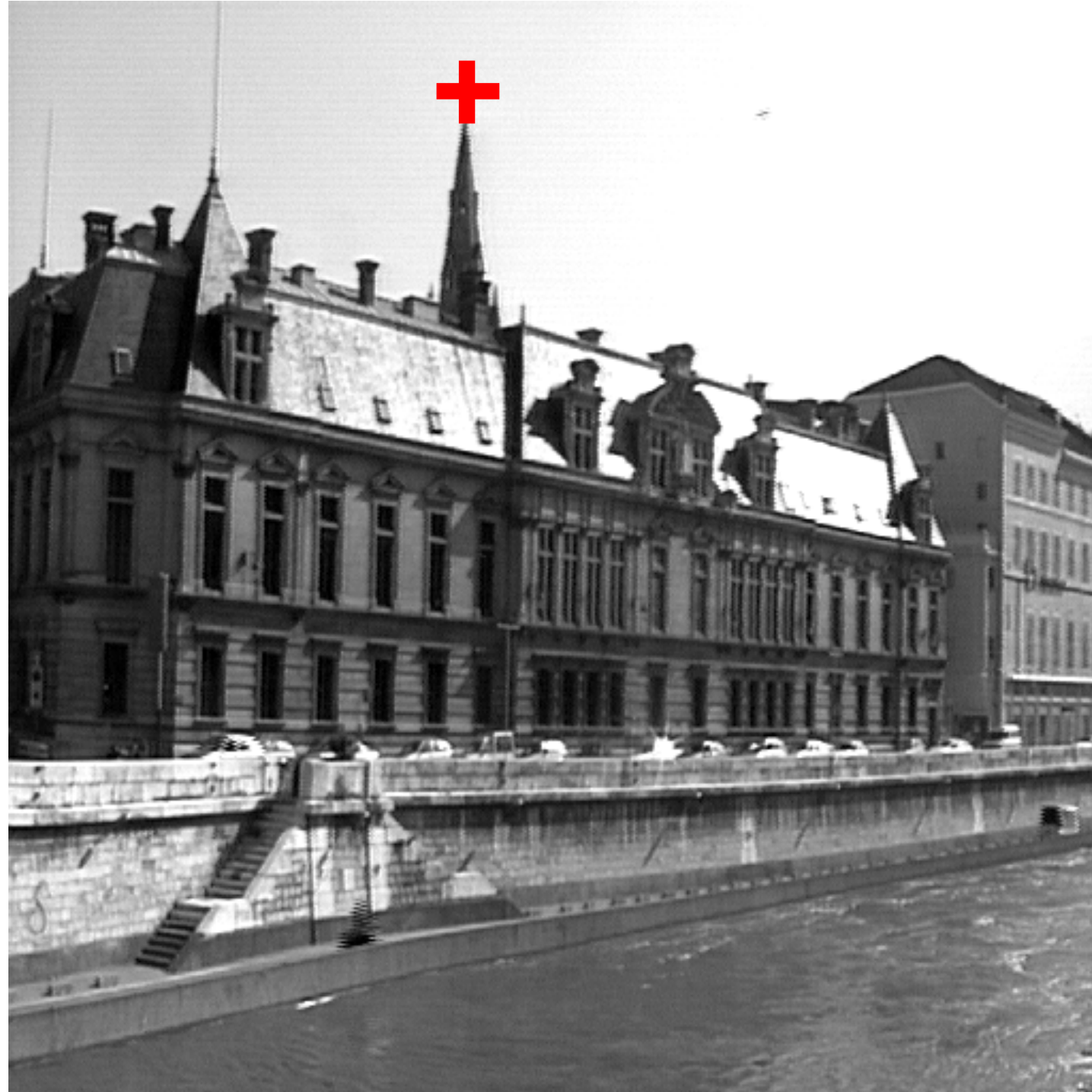
Simple linear iterative clustering (SLIC)



Normalized cut [Shi & Malik], Mean Shift [Comaniciu & Meer],
SLIC superpixels [PAMI'12], ...

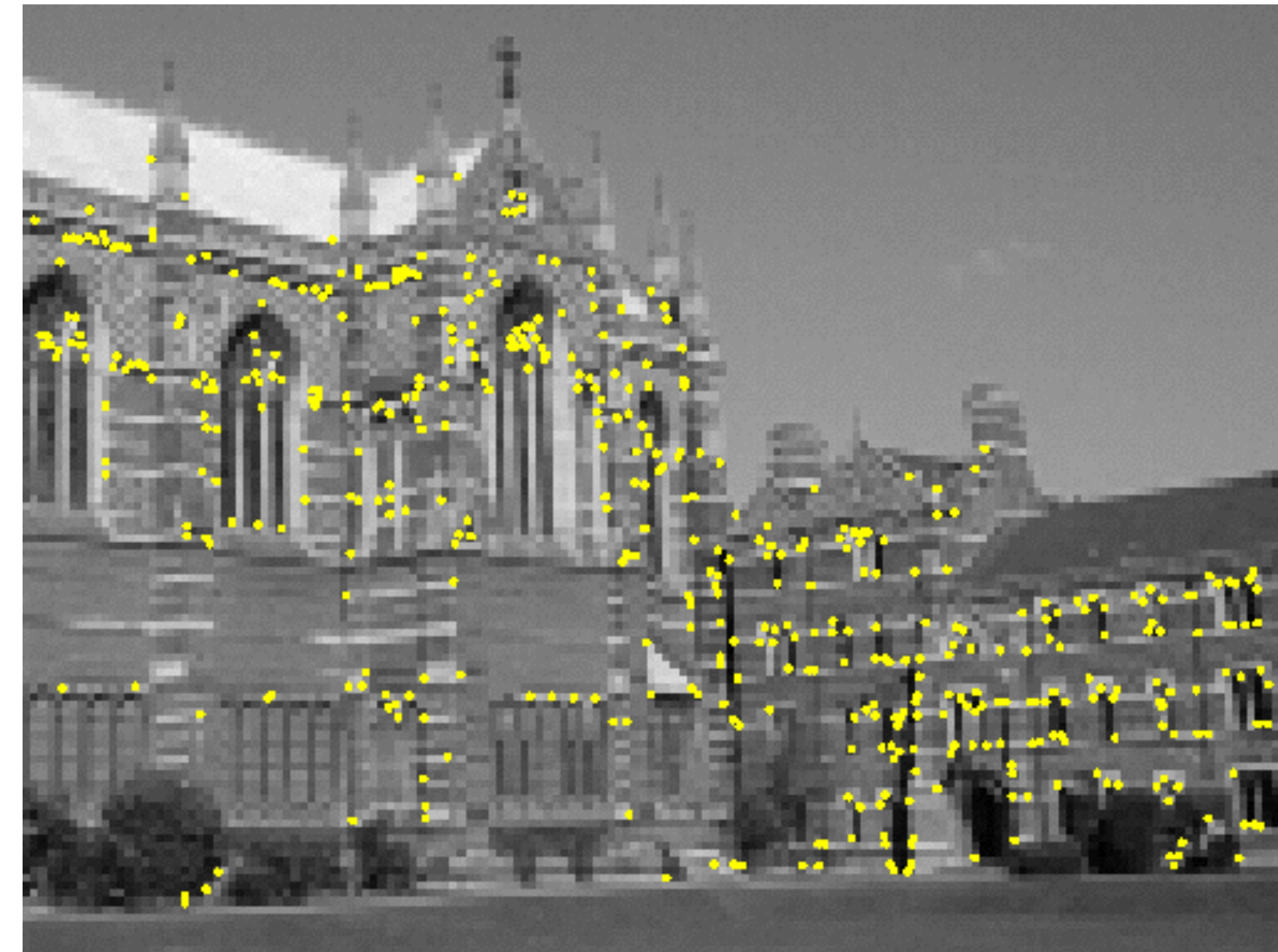
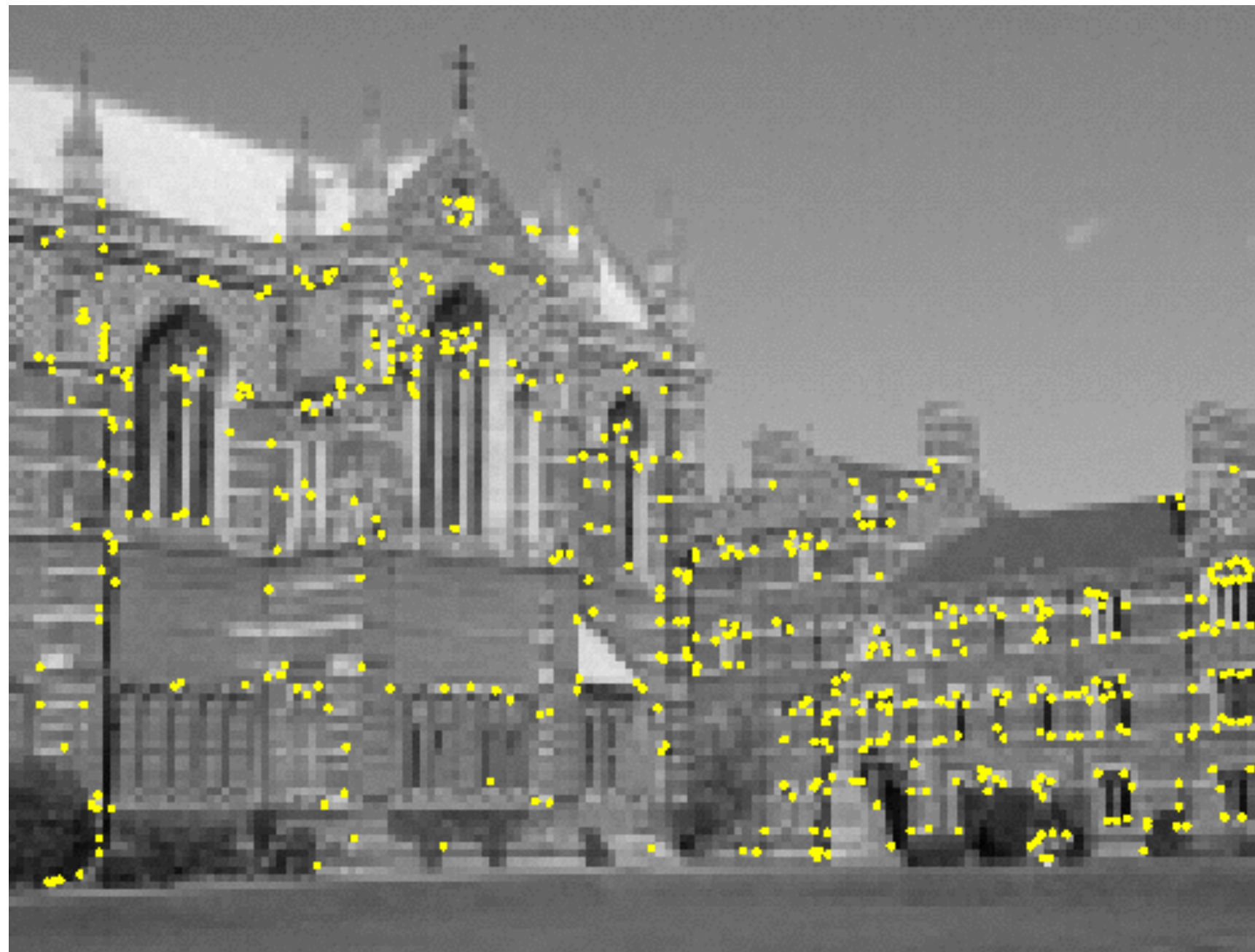
Matching of local descriptors

What can go wrong in matching this image pair?



Find corresponding locations in the image

Illustration – Matching



Interest points extracted with Harris detector (~ 500 points)

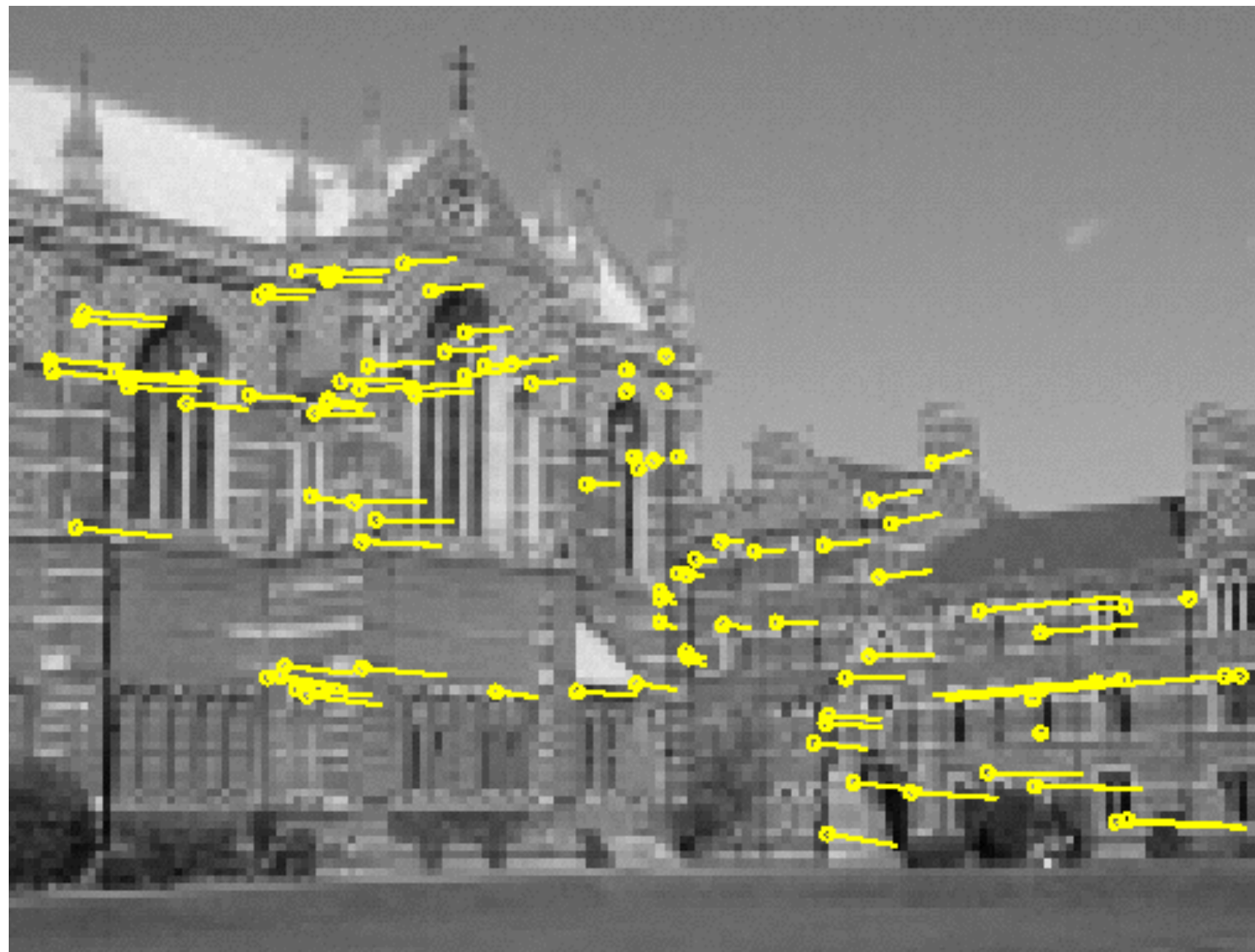
Illustration – Matching



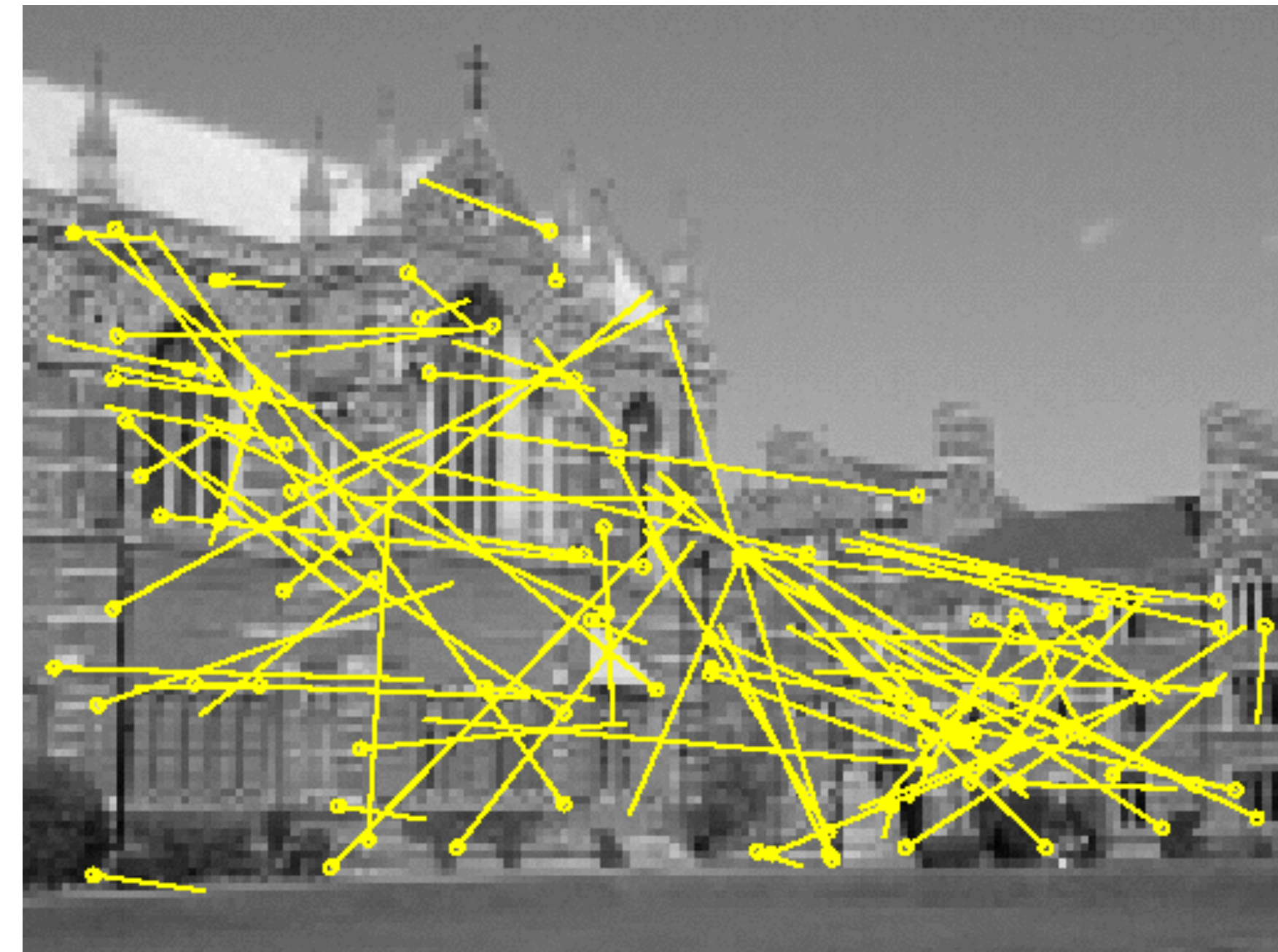
Interest points matched based on cross-correlation (188 pairs)

Illustration – Matching

Global constraint - Robust estimation of the fundamental matrix



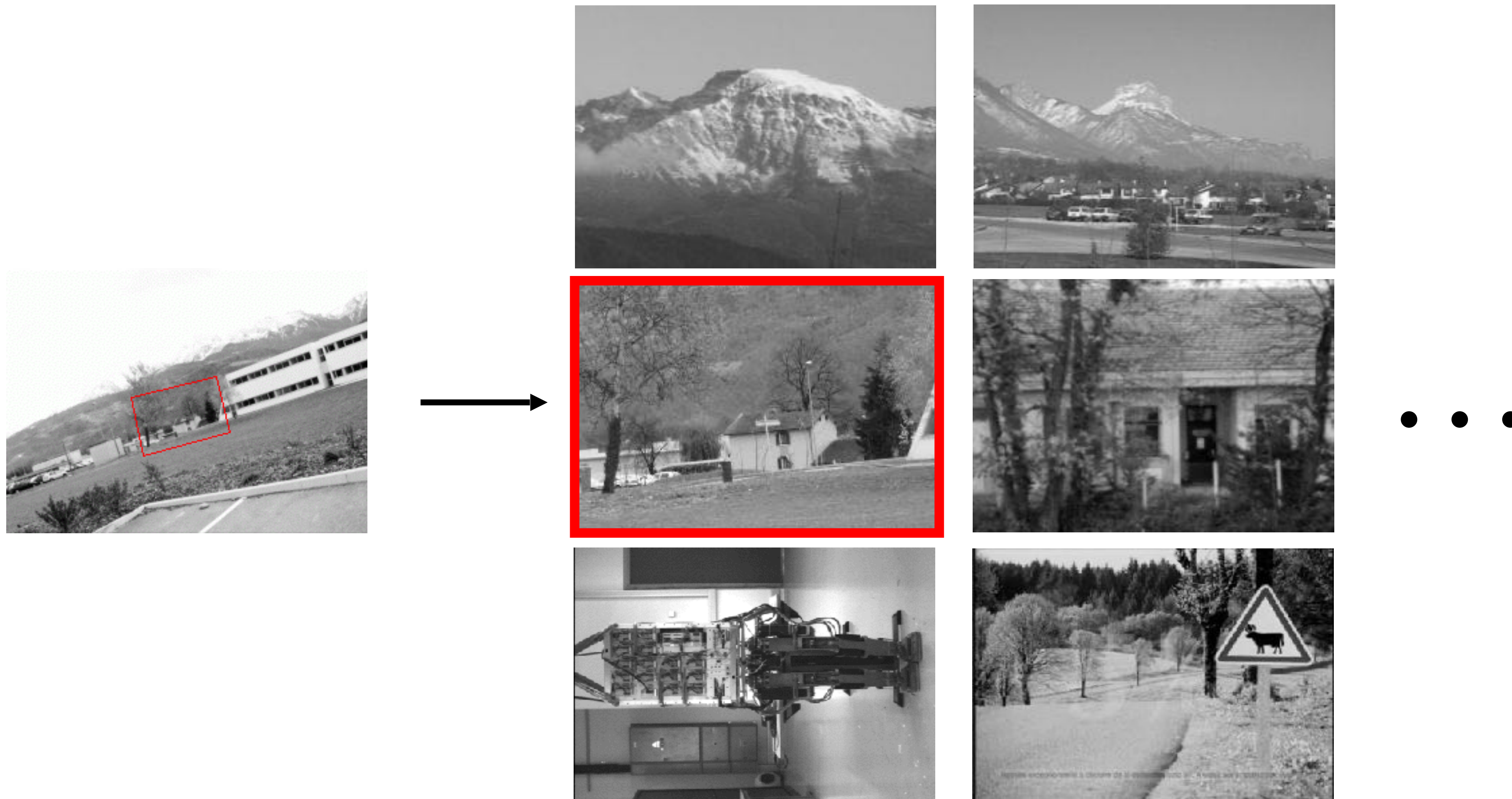
99 inliers



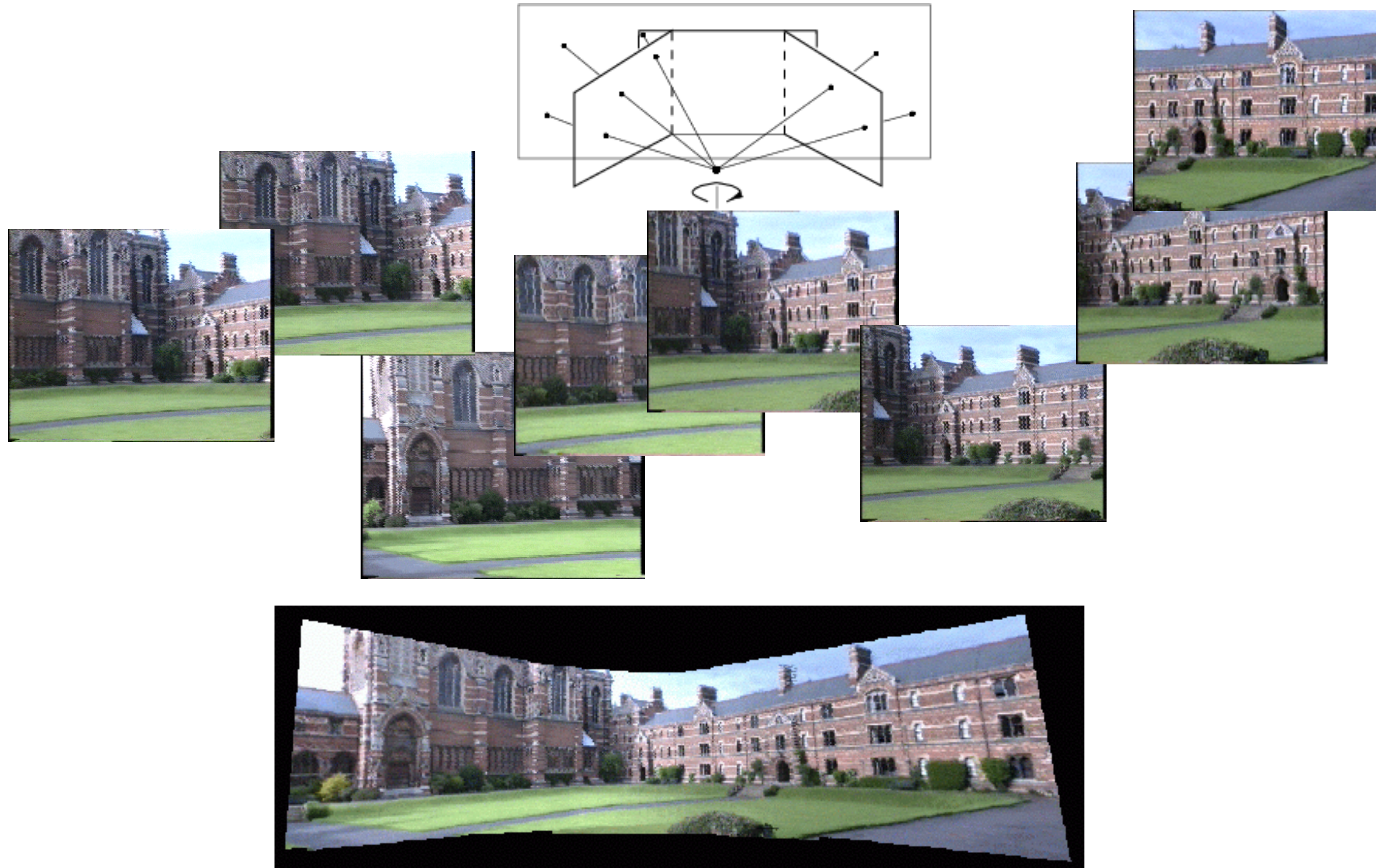
89 outliers

Application: Instance-level recognition

Search for particular objects and scenes in large databases



Application: Panorama stitching



Agenda: Instance-level recognition

1) Introduction to local features

2) Interest point detectors (e.g., Harris, scale invariance)

3) Comparison of patches (SSD, ZNCC on pixel values)

4) Feature descriptors (e.g., SIFT)

5) Matching and recognition with local features

6) Local feature aggregation for a single image-level description

Harris detector [Harris & Stephens'88]

Based on the idea of auto-correlation



Important difference in all directions => interest point

Harris detector

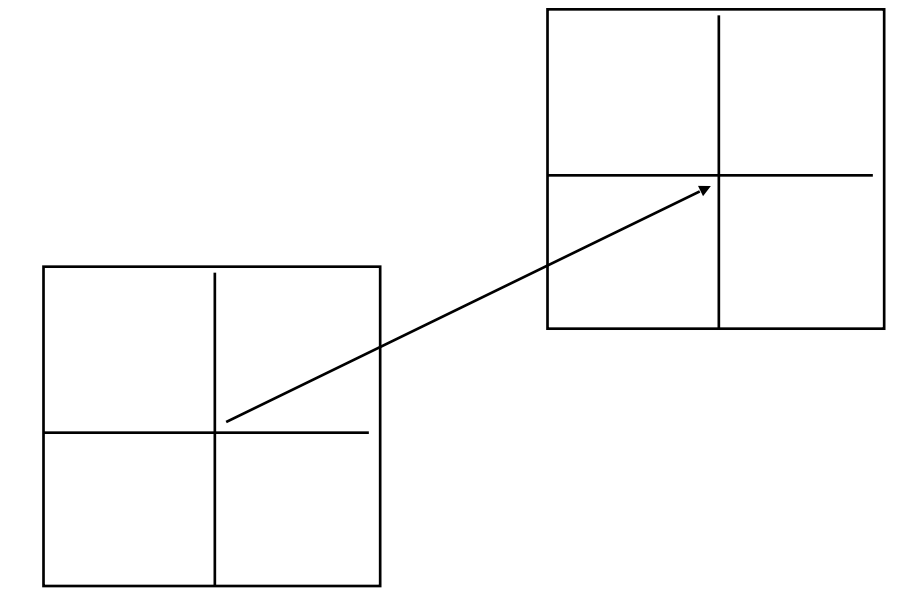
Auto-correlation function for a point $\mathbf{x} = (x, y)$ and a shift $\Delta\mathbf{u} = (\Delta x, \Delta y)$

$$E_{AC}(\Delta\mathbf{u}) = \sum_{i \in W} w(\mathbf{x}_i) (I(\mathbf{x}_i + \Delta\mathbf{u}) - I(\mathbf{x}_i))^2$$

*(spatially varying
weighting function)*

*(displacement
vector)*

$$\Delta\mathbf{u} = (\Delta x, \Delta y)$$



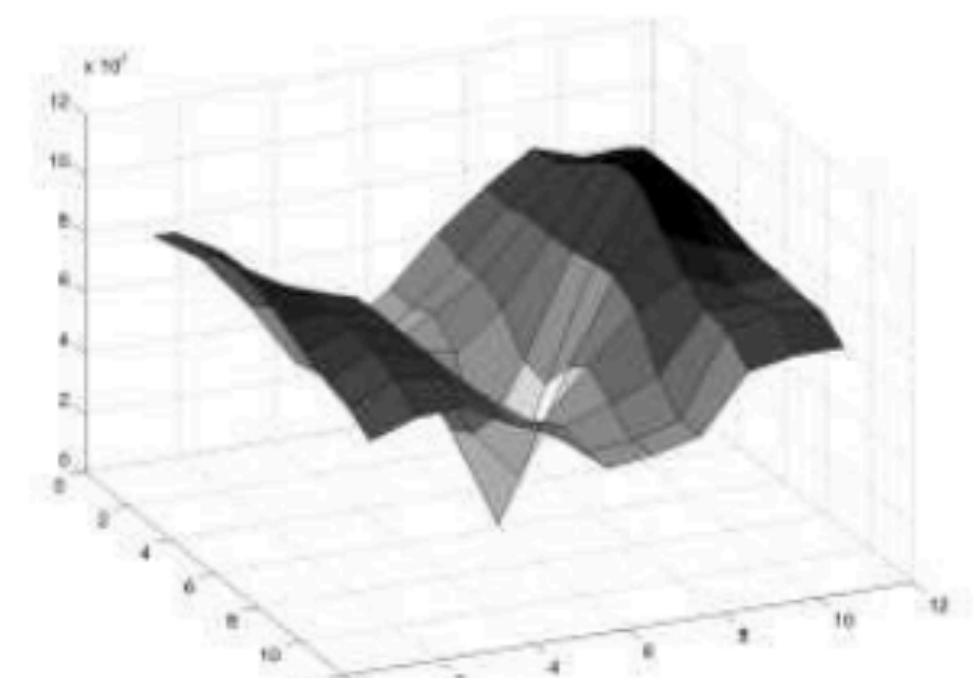
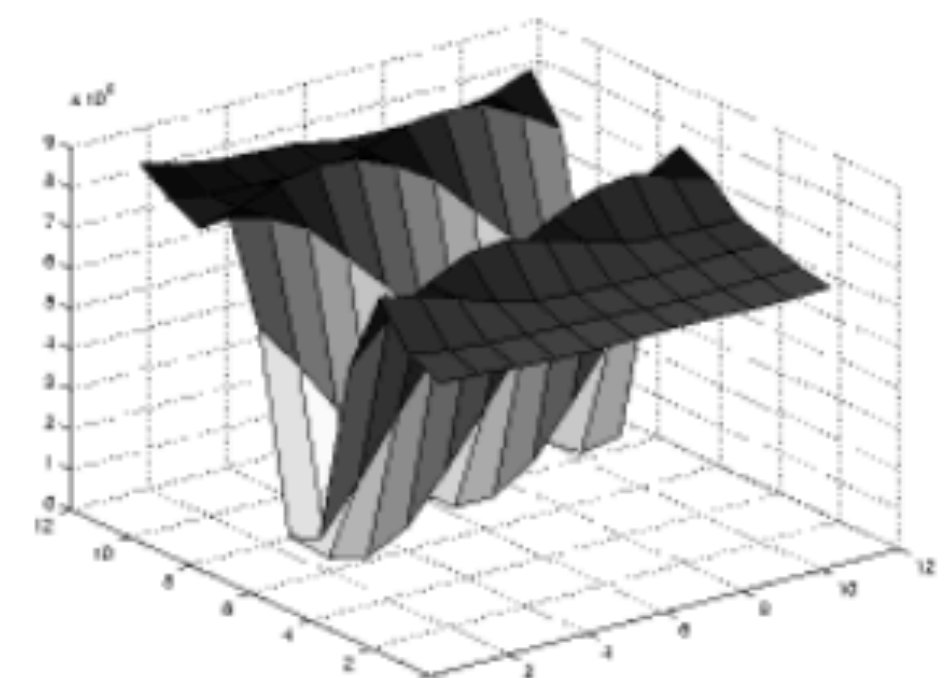
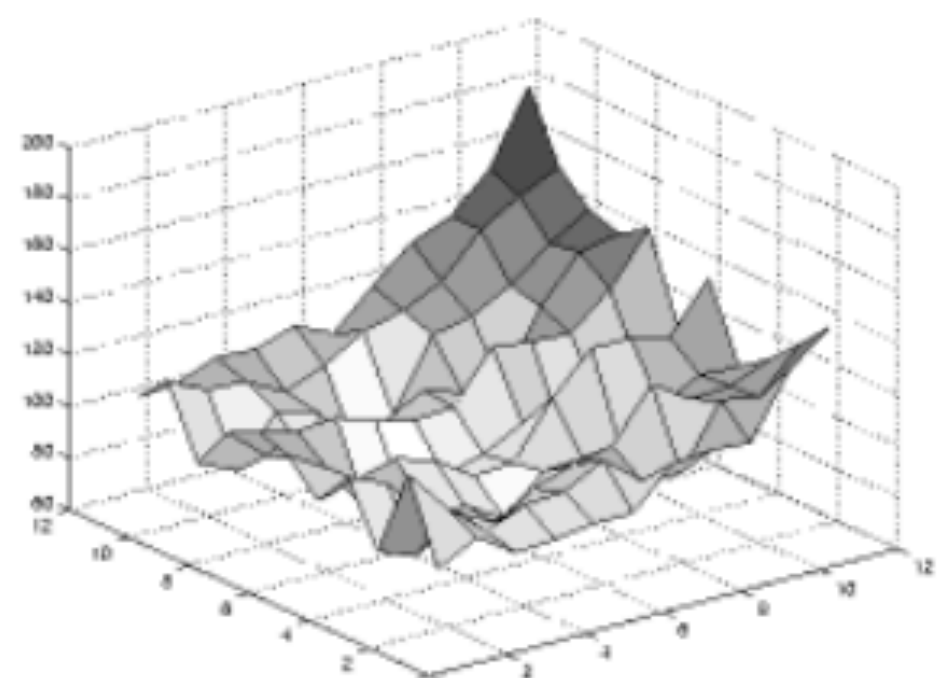
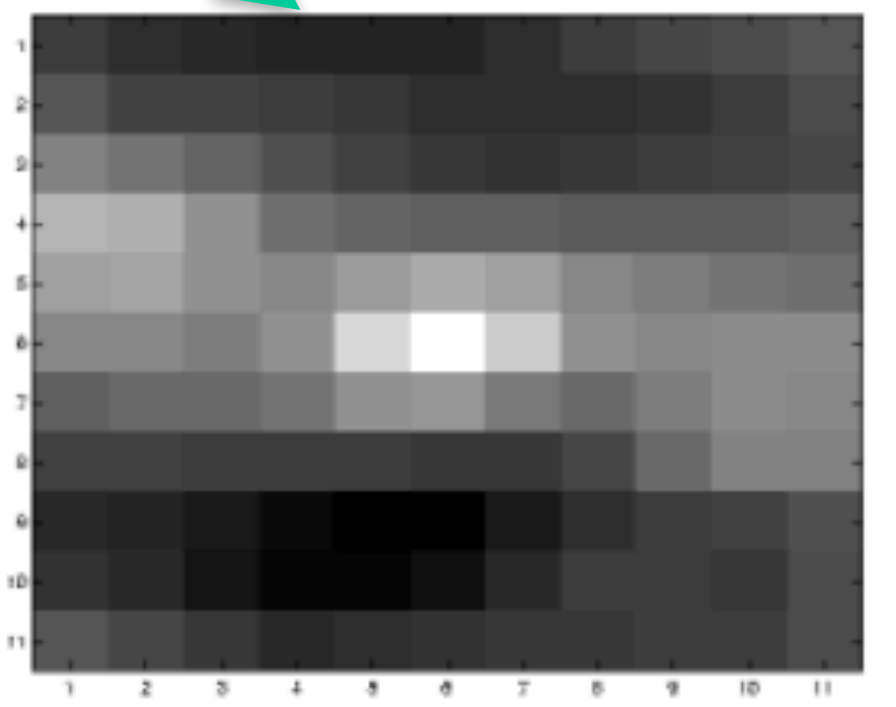
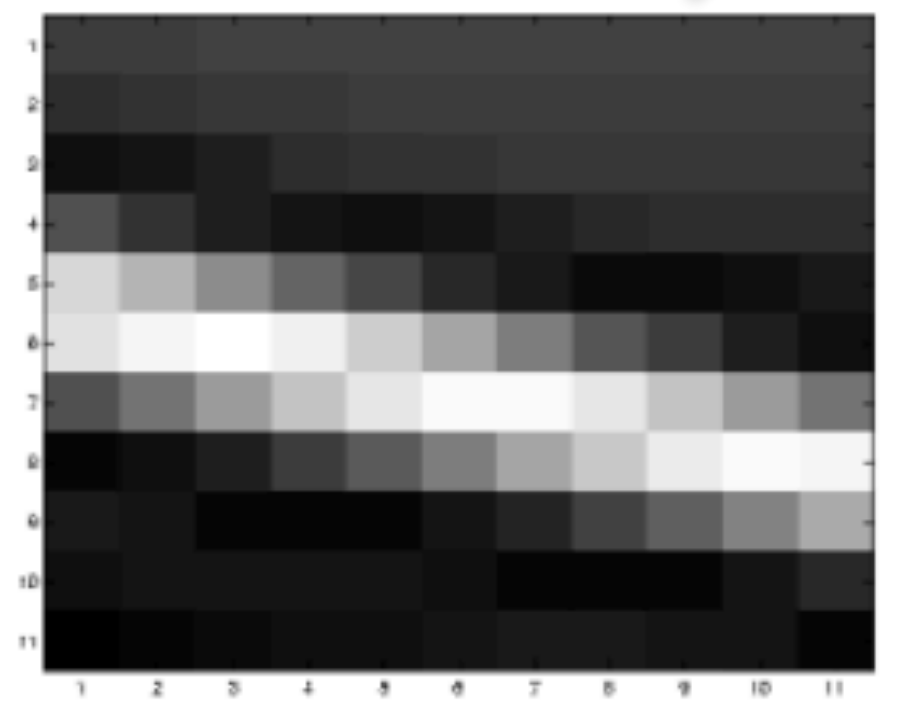
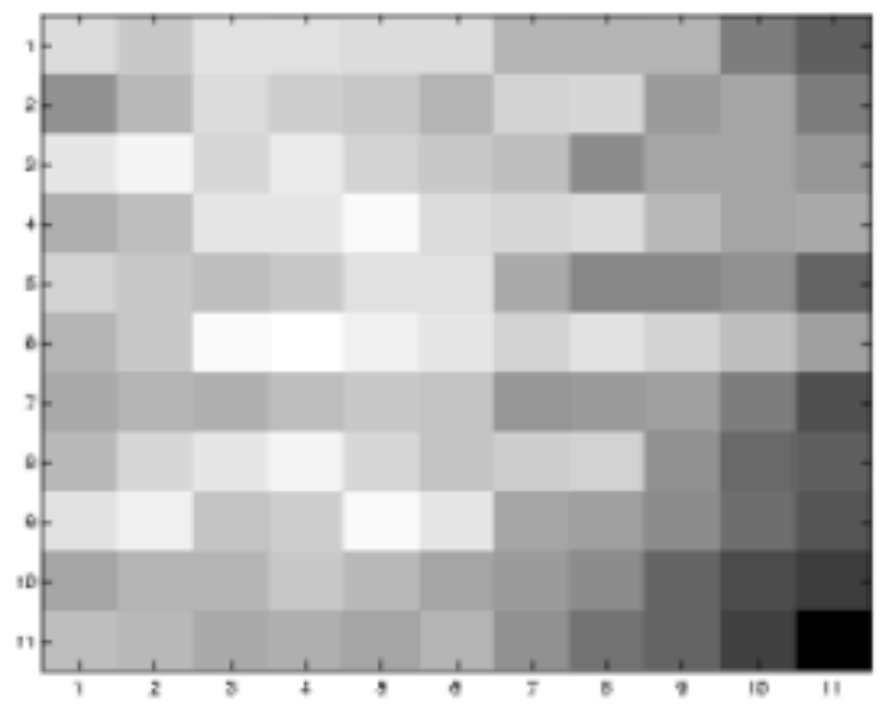
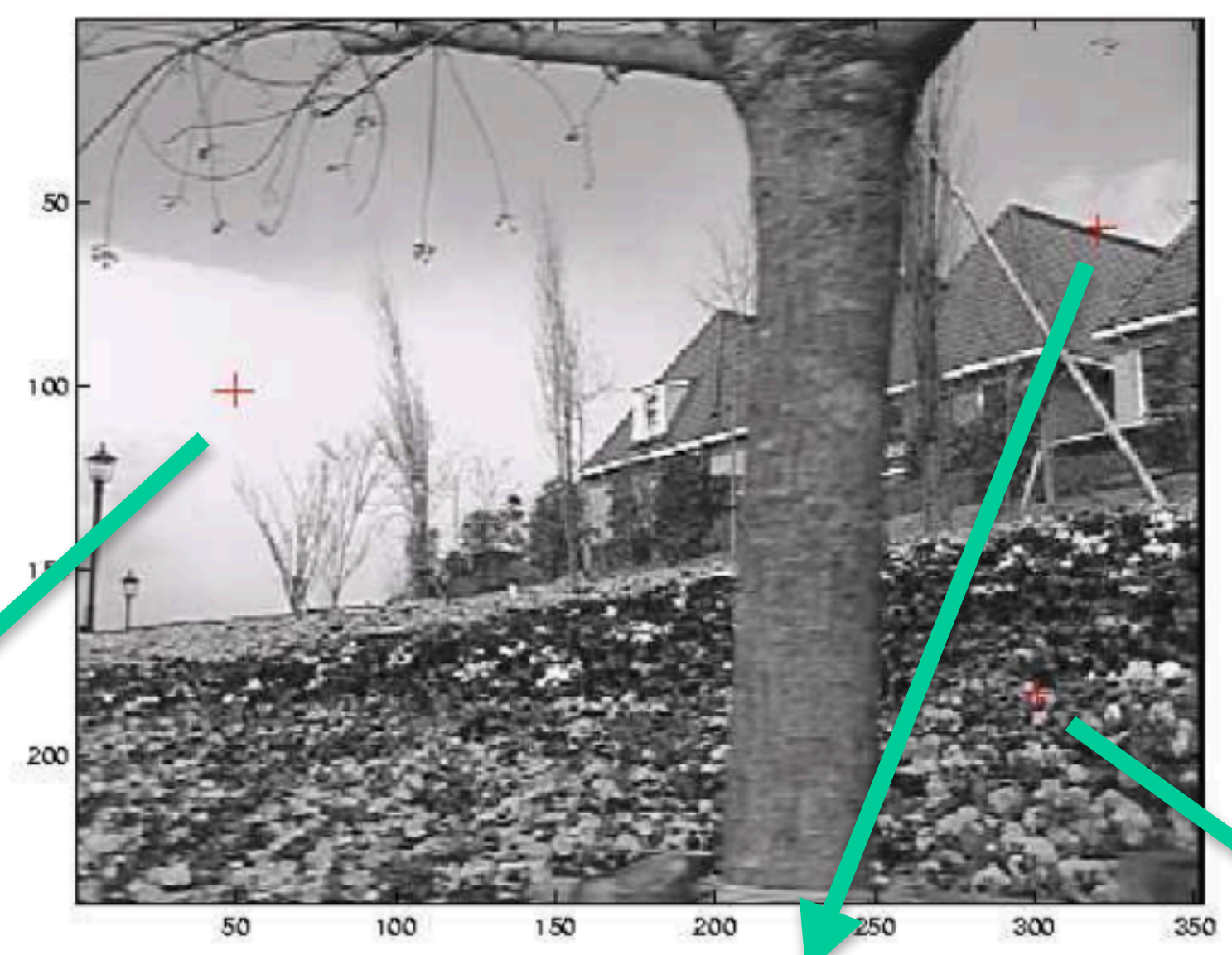
W
(window)

$E_{AC}(\Delta\mathbf{u})$ $\left\{ \begin{array}{ll} \text{small in all directions} & \rightarrow \text{uniform region} \\ \text{large in one directions} & \rightarrow \text{contour} \\ \text{large in all directions} & \rightarrow \text{interest point} \end{array} \right.$

“Strictly speaking, a correlation is the product of two patches [...] using the term here in a more qualitative sense.

The weighted **sum of squared differences** is often called an SSD surface.”

auto-correlation surfaces



Textureless

Edge

Corner

Figure 7.5 Szeliski

Harris detector

Taylor Series expansion:

$$E_{AC}(\Delta \mathbf{u}) = \sum_{i \in W} w(\mathbf{x}_i) (I(\mathbf{x}_i + \Delta \mathbf{u}) - I(\mathbf{x}_i))^2$$

$$\approx \sum_{i \in W} w(\mathbf{x}_i) (\cancel{I(\mathbf{x}_i)} + \nabla I(\mathbf{x}_i) \cdot \Delta \mathbf{u} - \cancel{I(\mathbf{x}_i)})^2$$

$$= \sum_{i \in W} w(\mathbf{x}_i) (\nabla I(\mathbf{x}_i) \cdot \Delta \mathbf{u})^2$$

$$= \Delta \mathbf{u}^T \mathbf{A} \Delta \mathbf{u}$$

replaced the weighted summations with discrete convolutions with the weighting kernel w

e.g., Harris detector uses a $[-2 \ -1 \ 0 \ 1 \ 2]$ filter.

Other variants convolving with horizontal/vertical derivatives of a Gaussian.

(image gradient)

$$\nabla I(\mathbf{x}_i) = \left(\frac{\partial I}{\partial x}, \frac{\partial I}{\partial y} \right) (\mathbf{x}_i)$$

(auto-correlation matrix)

$$\mathbf{A} = w * \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

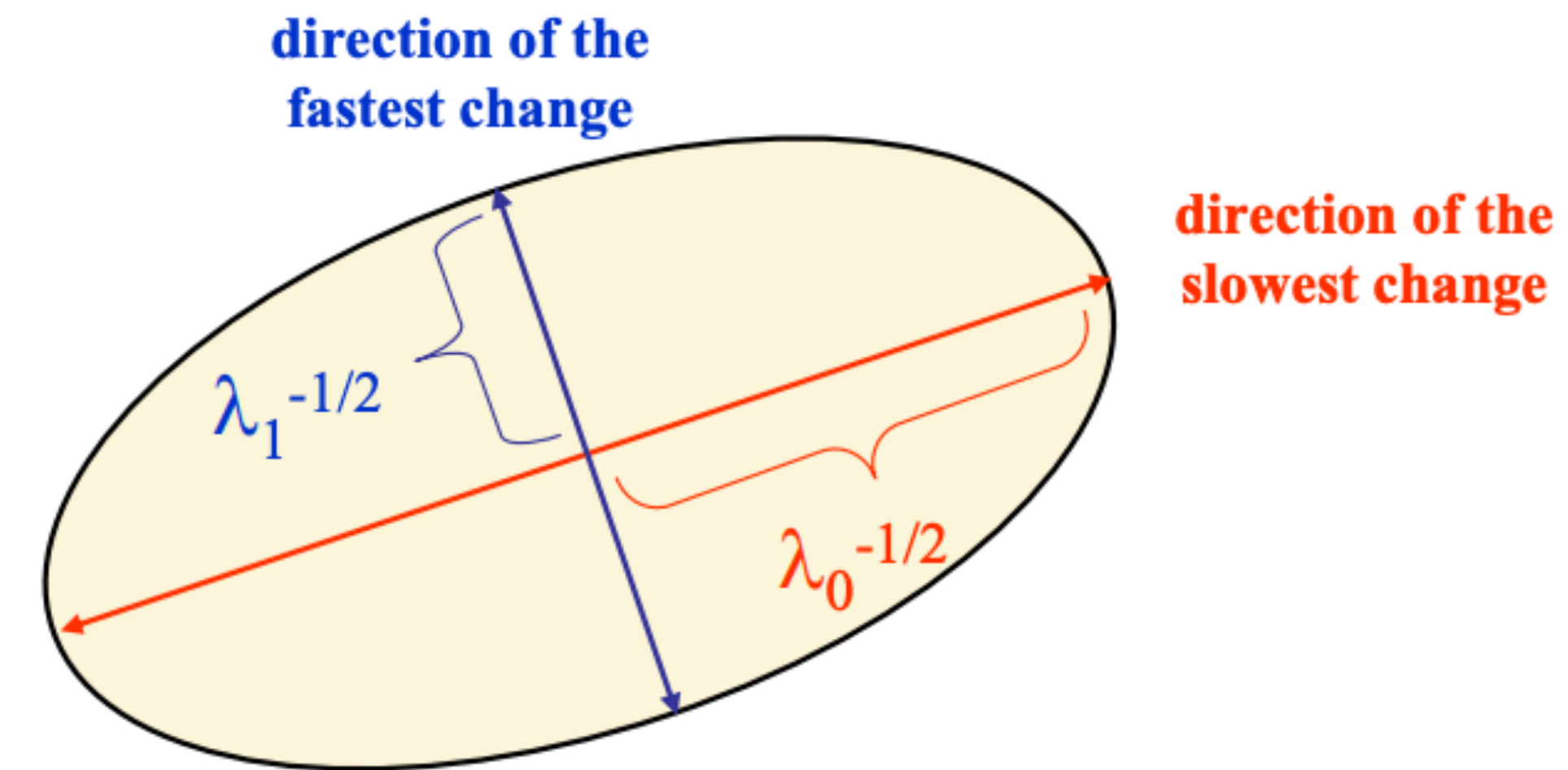
I_x (partial derivative in horizontal axis)

Harris detector

- The sum can be smoothed with a Gaussian
- Gaussian window instead of square window

$$\mathbf{A}(\mathbf{x}, \mathbf{y}) = G \otimes \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

- captures the structure of the local neighborhood
- measure based on eigenvalues of this matrix
 - 2 strong eigenvalues \Rightarrow interest point
 - 1 strong eigenvalue \Rightarrow contour
 - 0 eigenvalue \Rightarrow uniform region

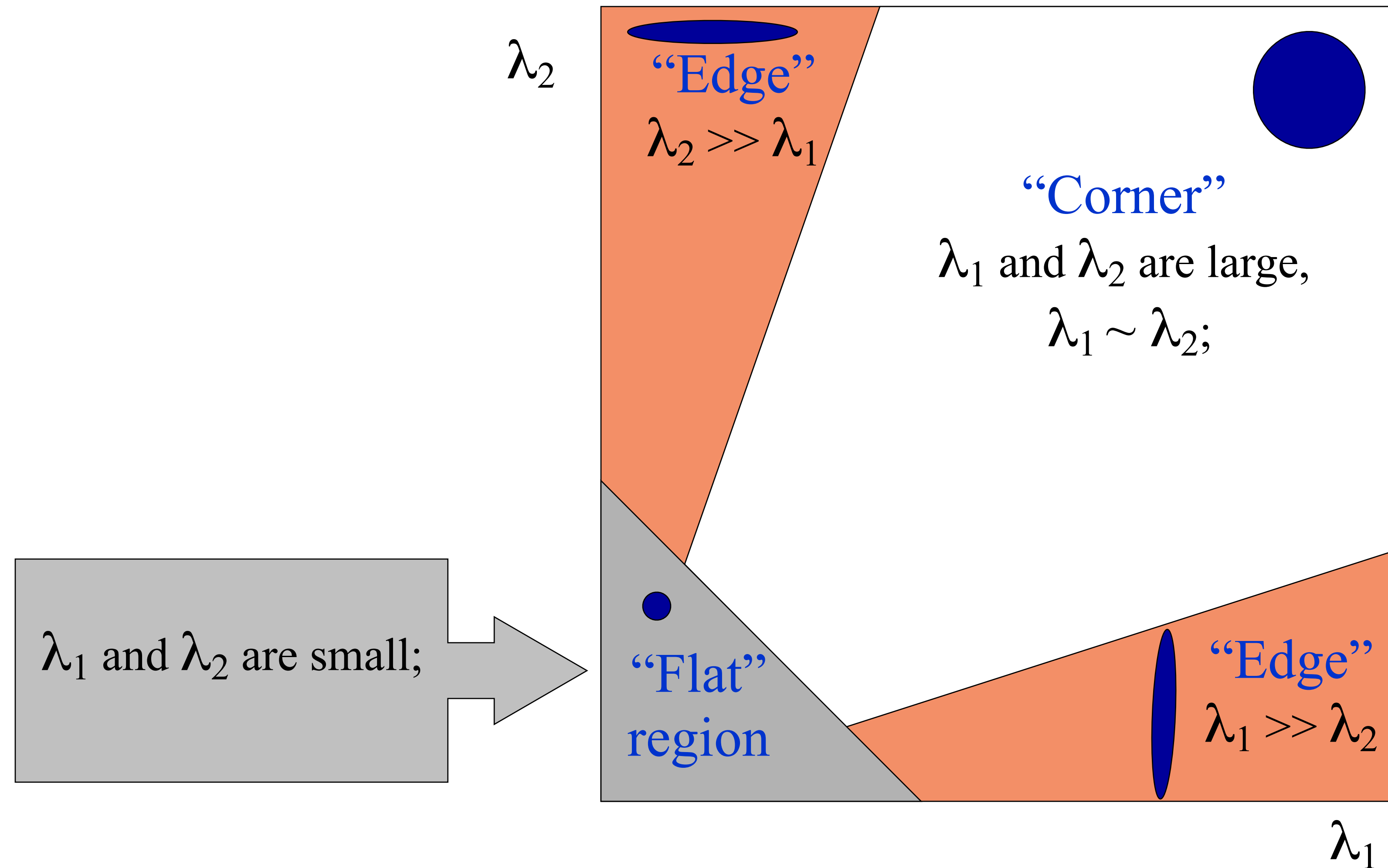


Uncertainty ellipse corresponding to an eigenvalue analysis of the autocorrelation matrix A.

Figure 7.6 Szeliski

Interpreting the eigenvalues

Classification of image points using eigenvalues of autocorrelation matrix

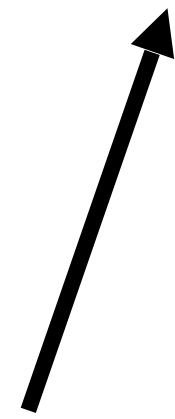


Corner response function

A simpler quantity, proposed by Harris and Stephens (1988)

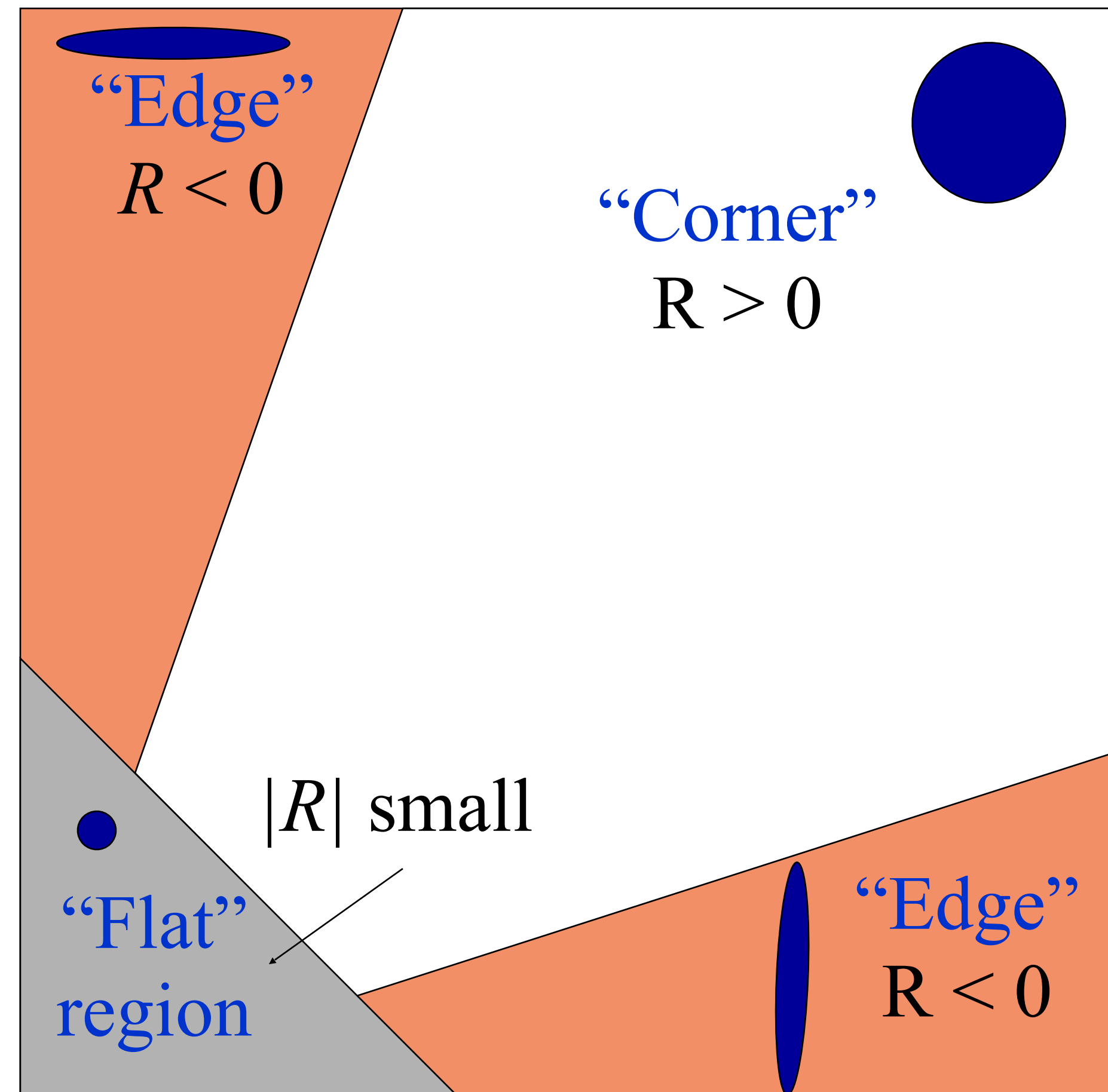
$$R = \det(\mathbf{A}) - \alpha \text{trace}(\mathbf{A})^2$$

$$= \lambda_1 \lambda_2 - \alpha (\lambda_1 + \lambda_2)^2$$



Reduces the effect of a strong contour
(constant)

$$\alpha = 0.06$$

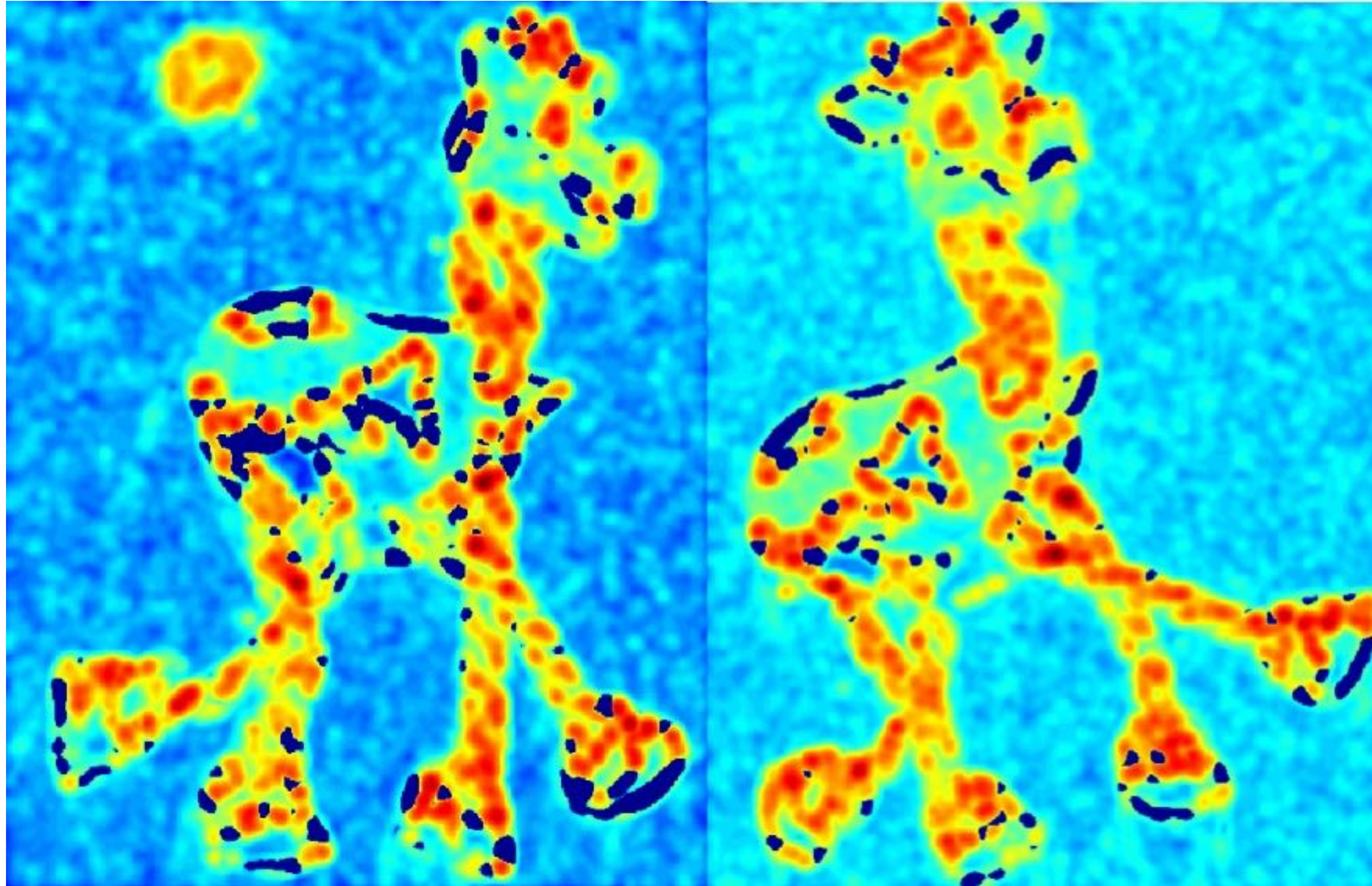


Harris Detector: Steps



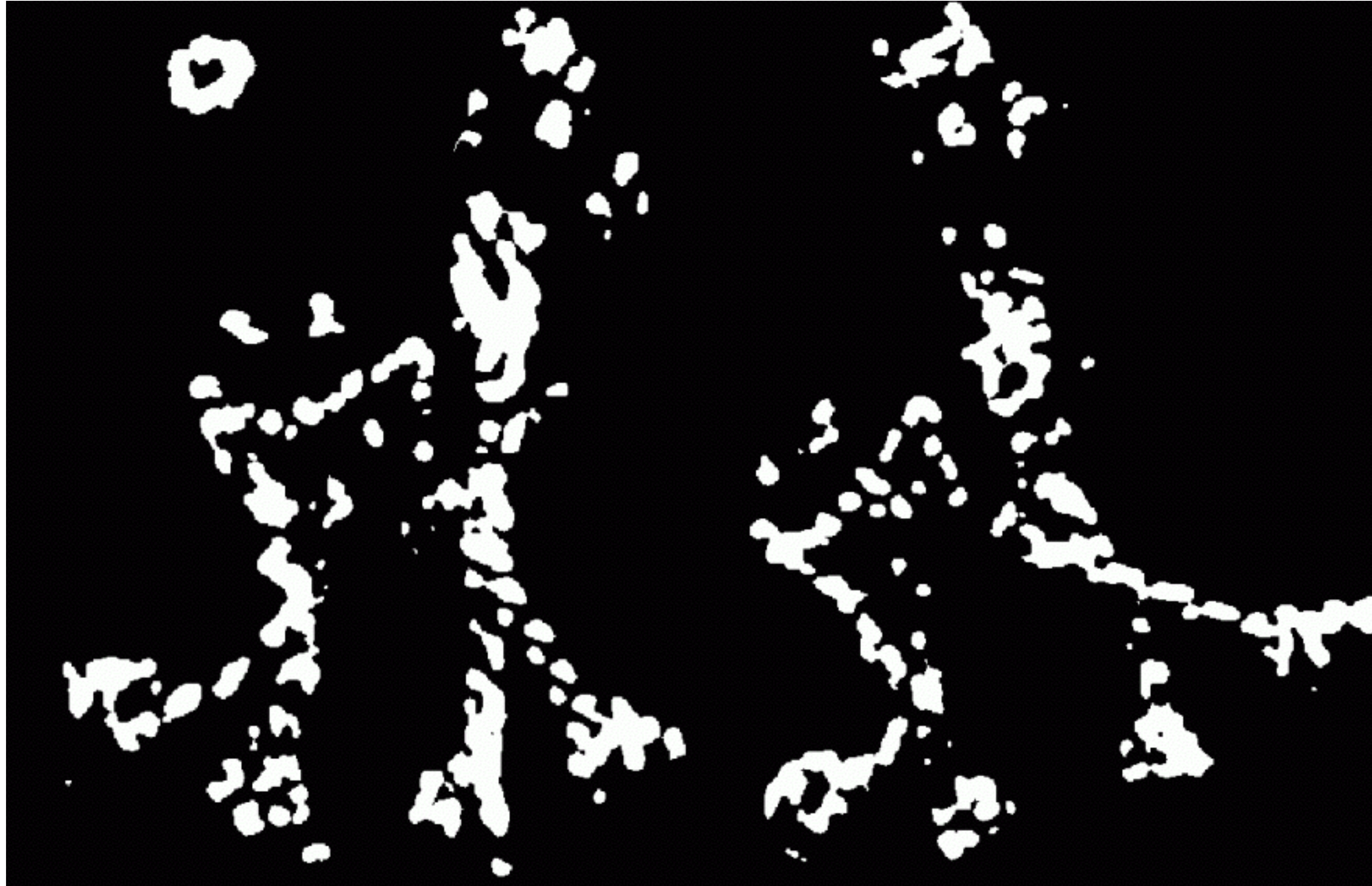
Harris Detector: Steps

Compute corner response R



Harris Detector: Steps

Find points with large corner response: $R > \text{threshold}$



Harris Detector: Steps

Take only the points of local maxima of R (*non-maximum suppression*)

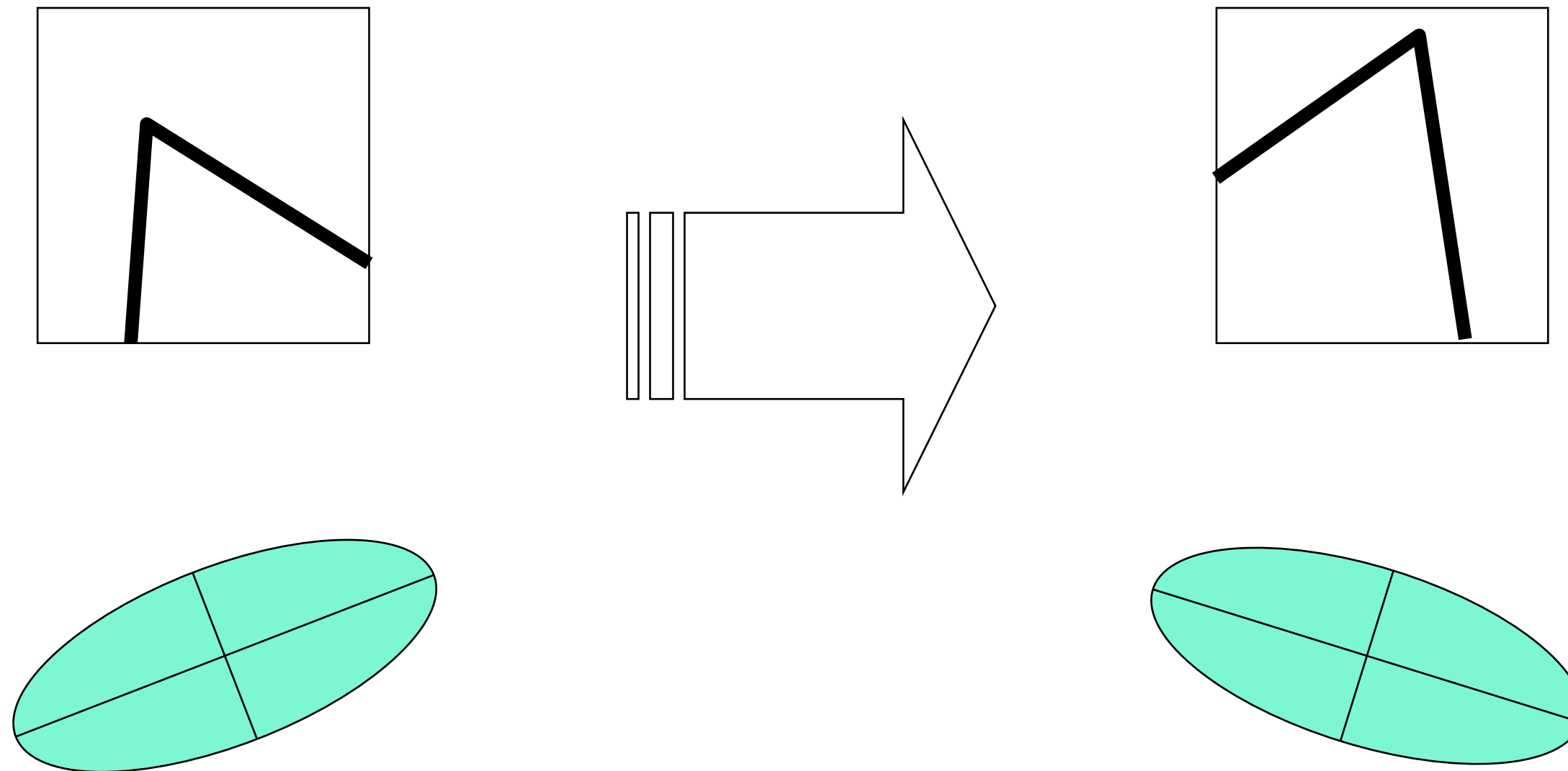


Harris detector: Summary of steps

1. Compute Gaussian derivatives at each pixel
2. Compute second moment matrix A in a Gaussian window around each pixel
3. Compute corner response function R
4. Threshold R
5. Find local maxima of response function (non-maximum suppression)

Harris Detector: Invariance Properties

- Rotation



Ellipse rotates but its shape (i.e. eigenvalues)
remains the same

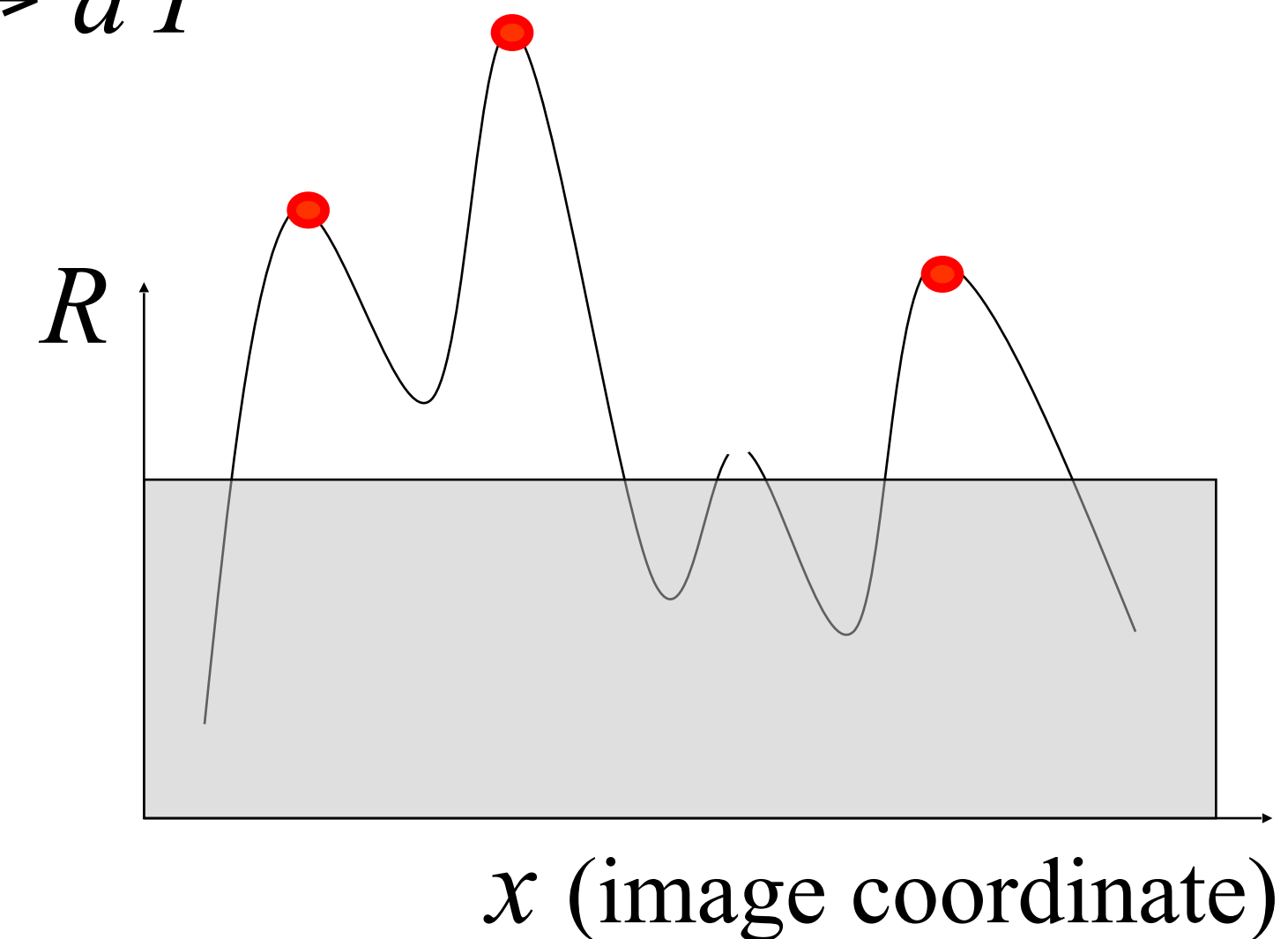
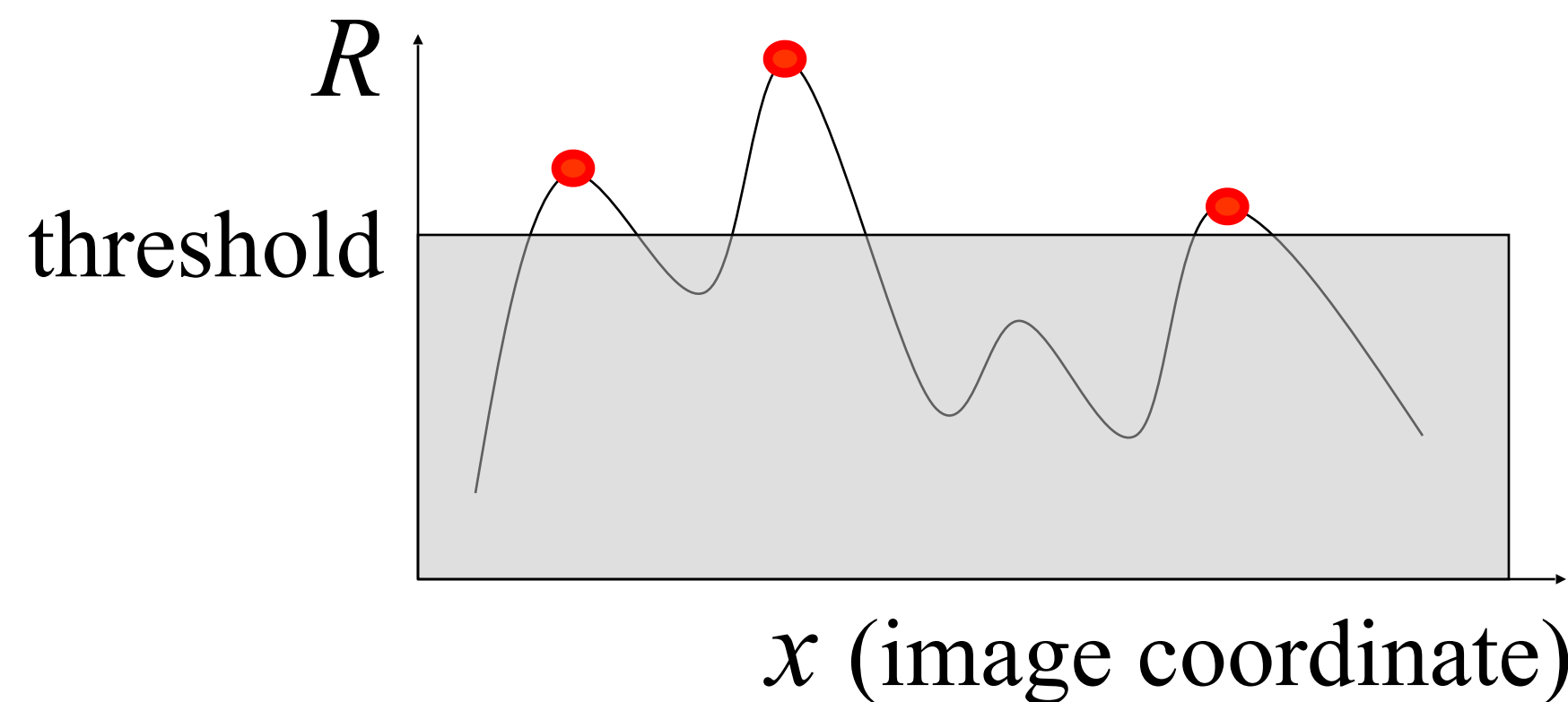
Corner response R is invariant to image rotation

Harris Detector: Invariance Properties

- Affine intensity change

- ✓ Only derivatives are used \Rightarrow invariance to intensity shift $I \rightarrow I + b$

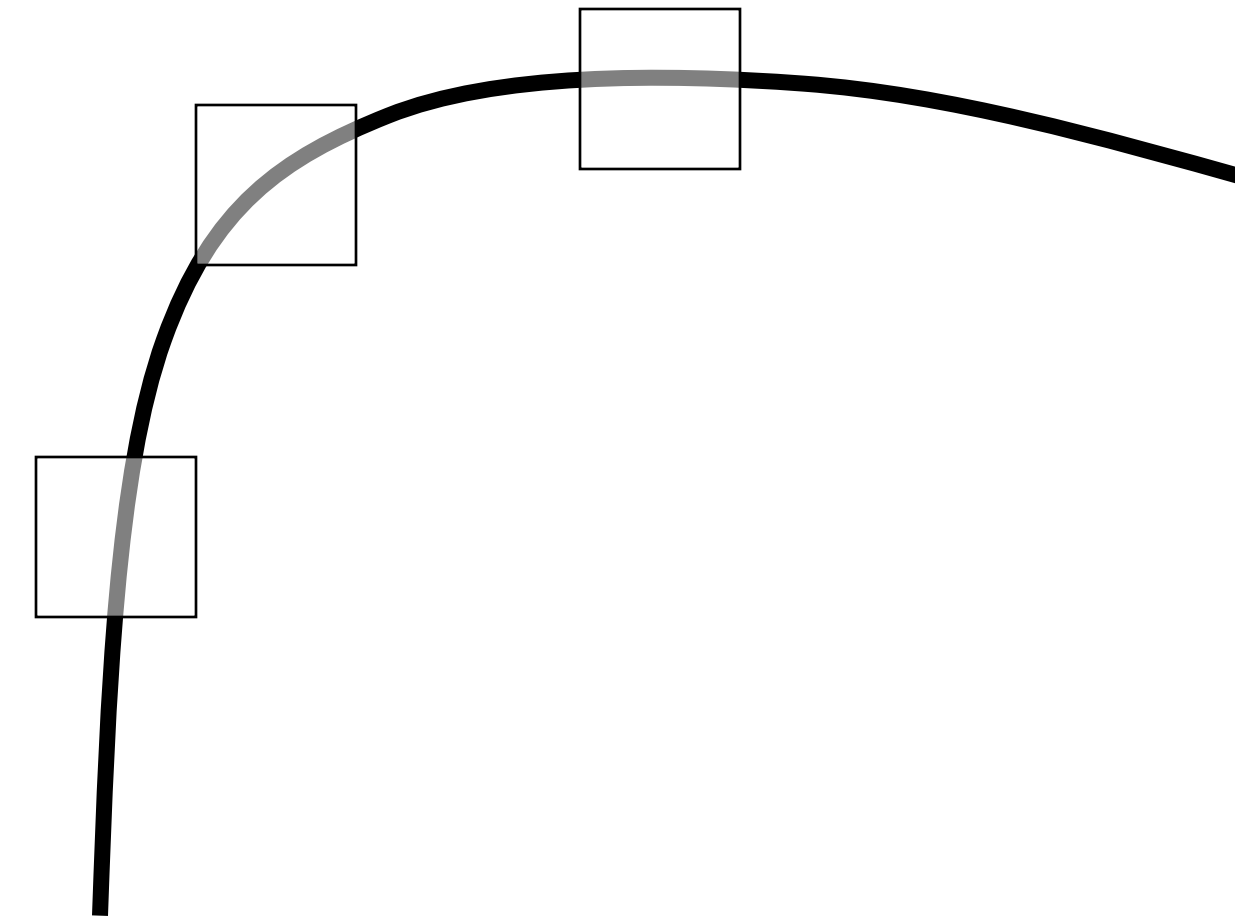
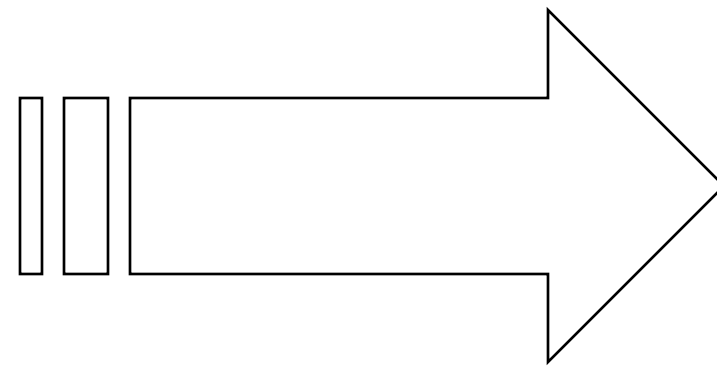
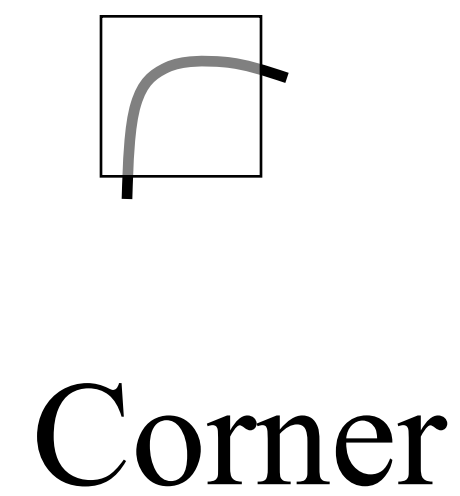
- ✓ Intensity scale: $I \rightarrow a I$



Partially invariant to affine intensity change,
dependent on type of threshold

Harris Detector: Invariance Properties

- Scaling



All points will
be classified as
edges

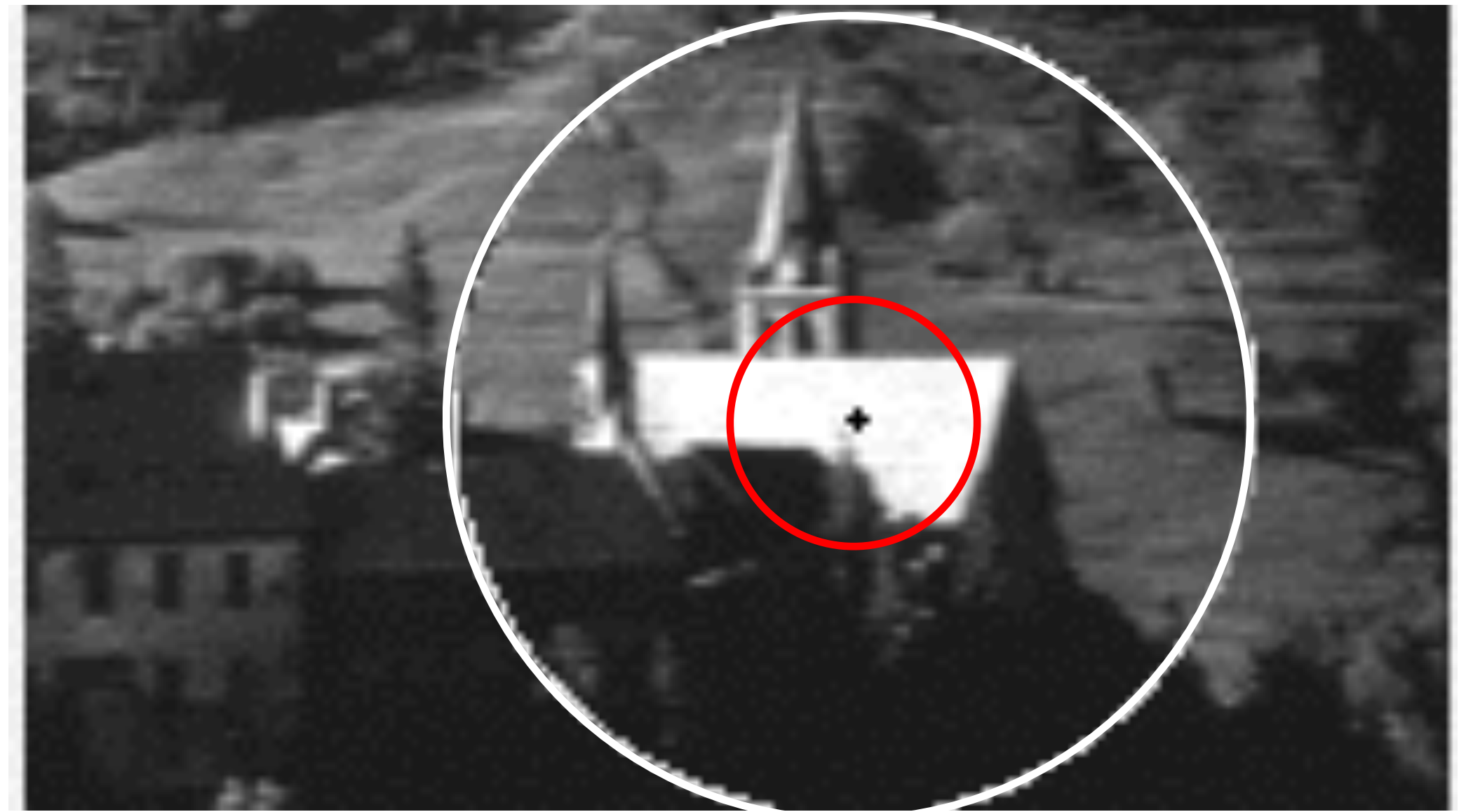
Not invariant to scaling

Agenda: Instance-level recognition

- 1) Introduction to local features
- 2) Interest point detectors (e.g., Harris, **scale invariance**)
- 3) Comparison of patches (SSD, ZNCC on pixel values)
- 4) Feature descriptors (e.g., SIFT)
- 5) Matching and recognition with local features
- 6) Local feature aggregation for a single image-level description

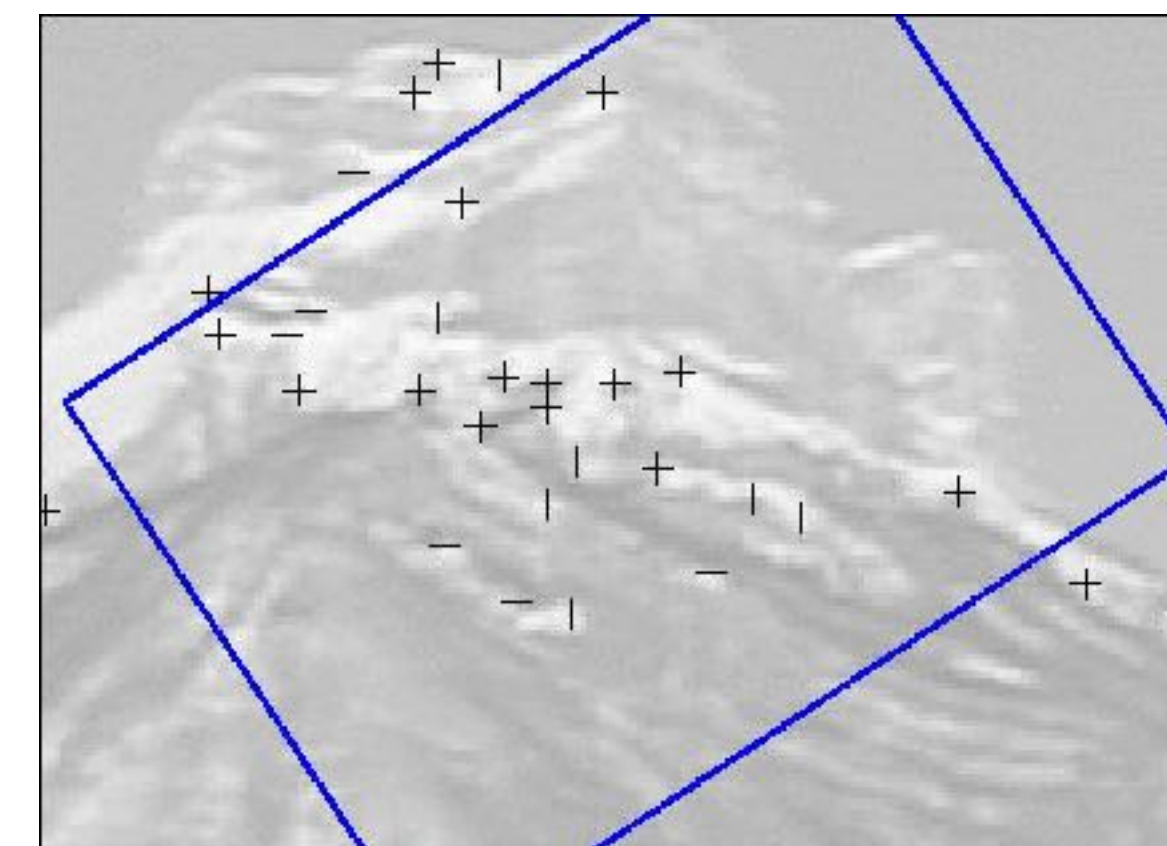
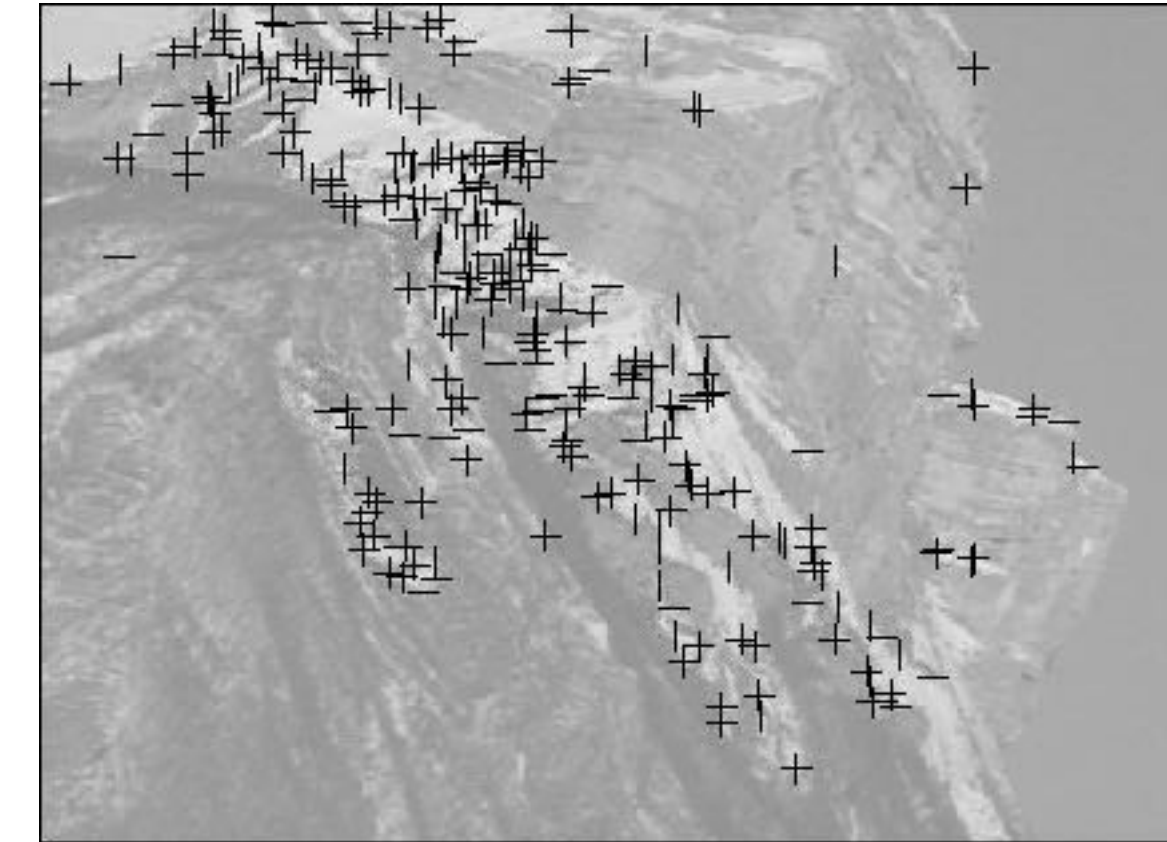
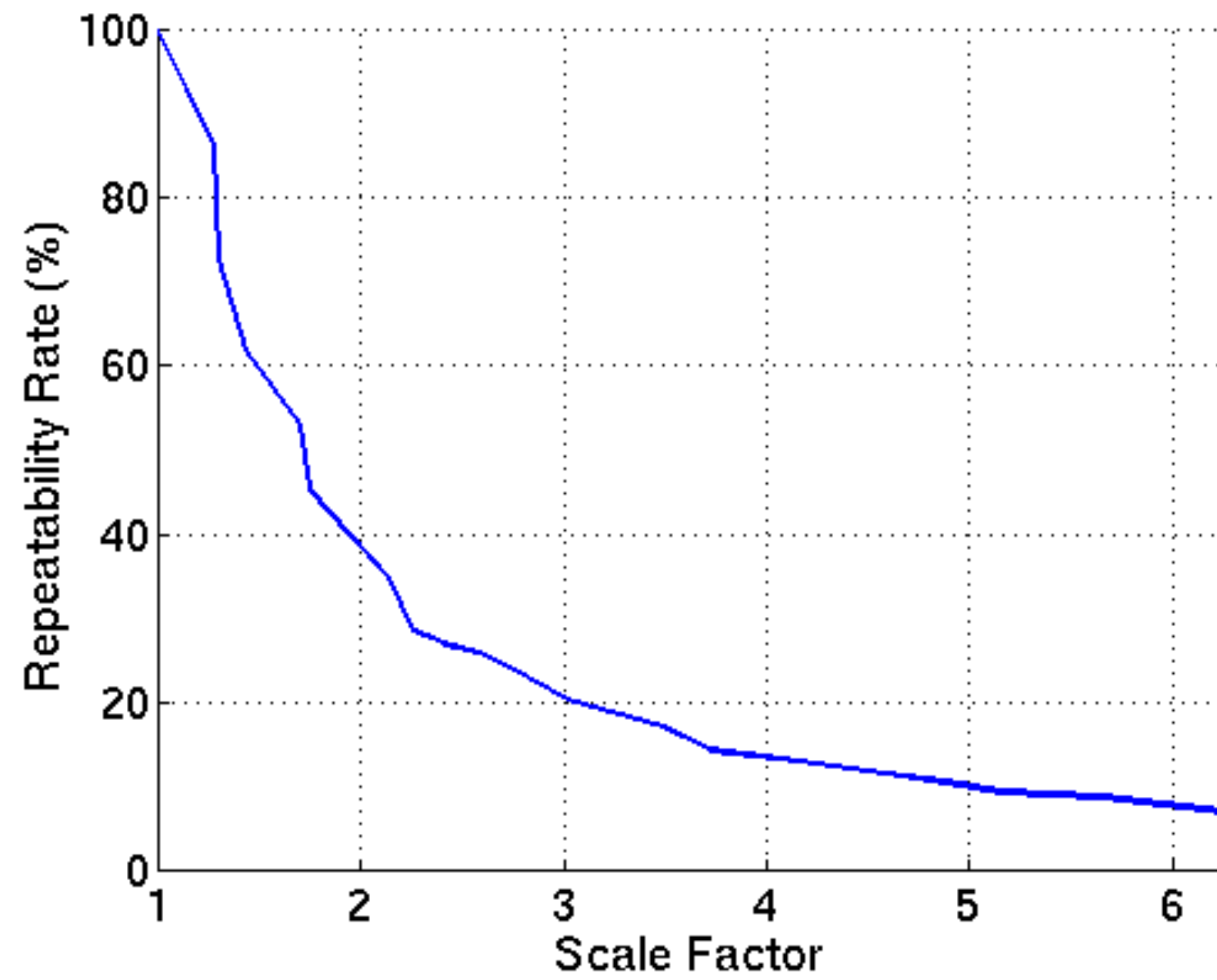
Scale invariance - motivation

- Description regions have to be adapted to scale changes



- Interest points have to be repeatable for scale changes

Harris detector + scale changes

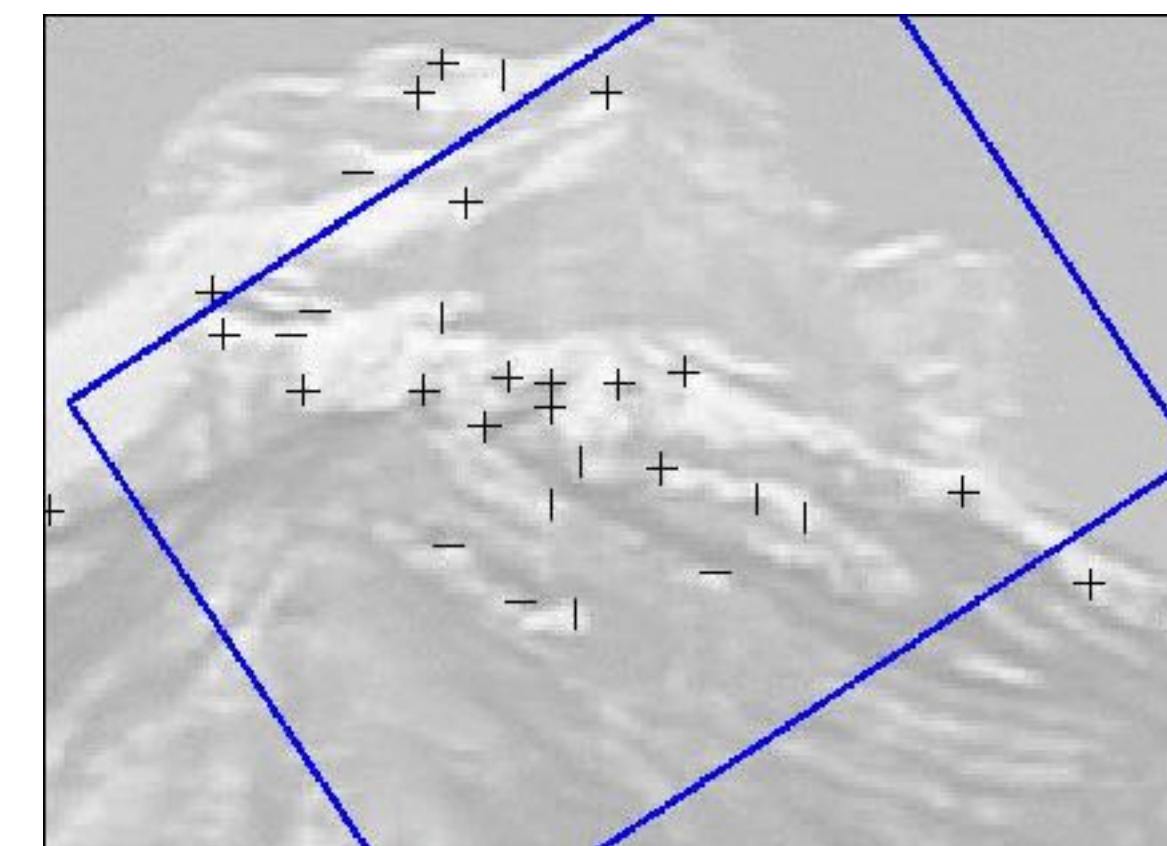
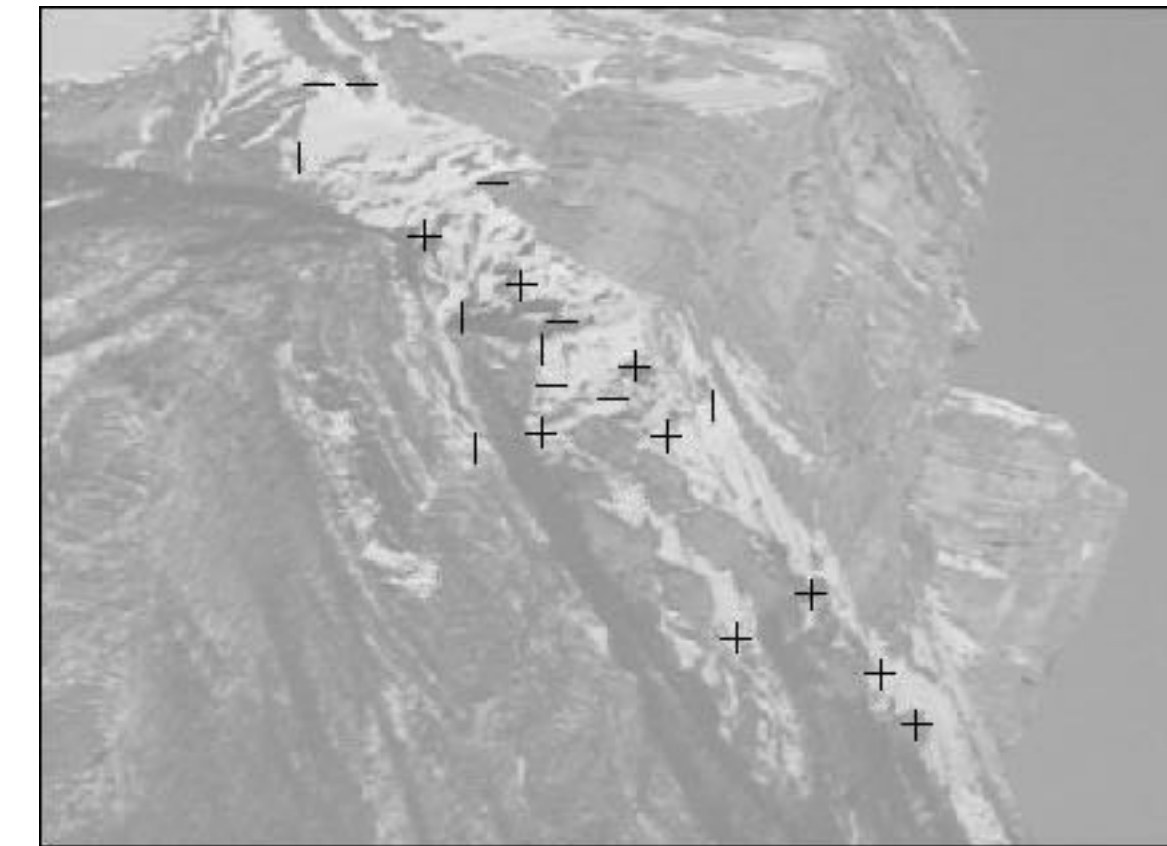
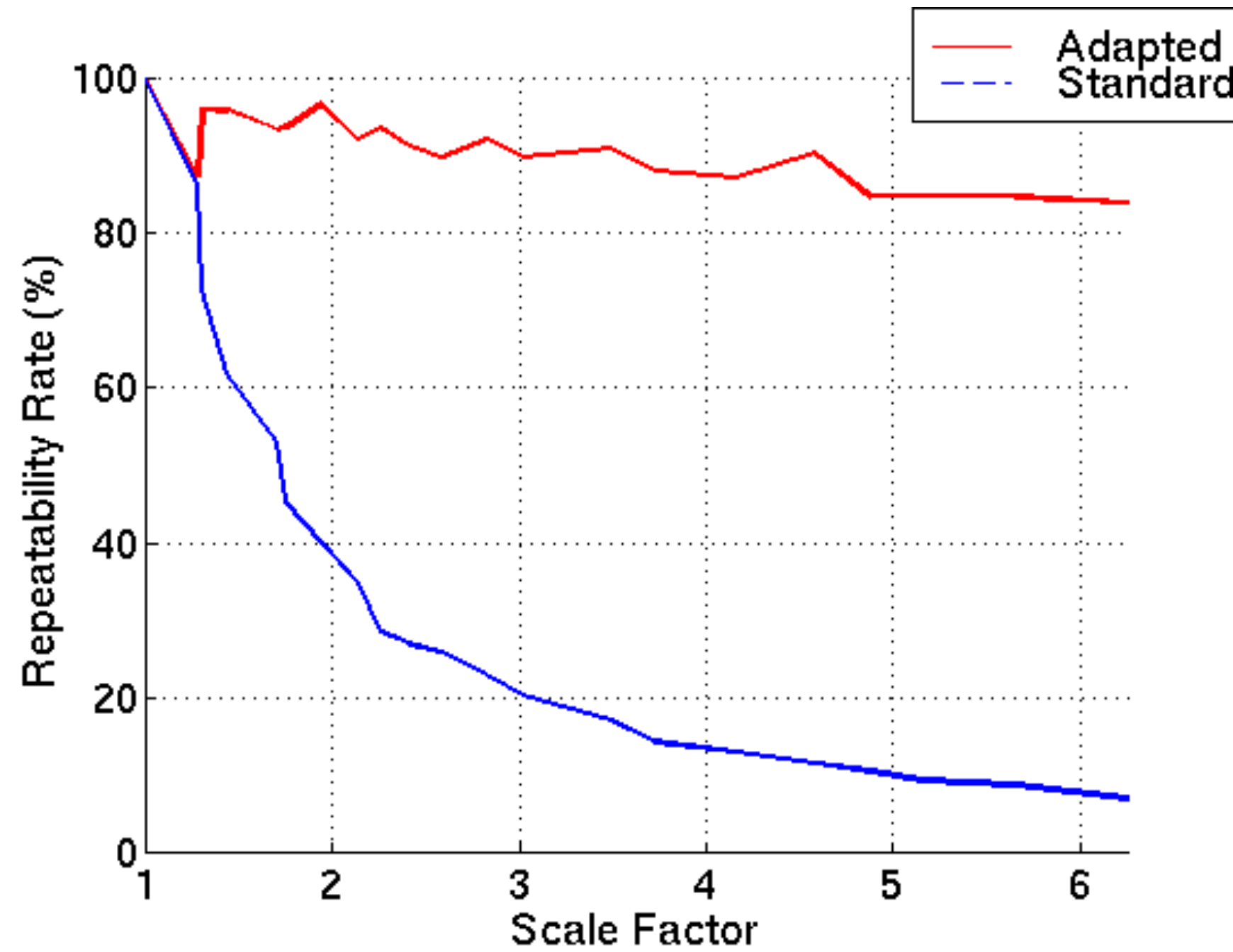


Repeatability rate

$$R(\varepsilon) = \frac{|\{(\mathbf{a}_i, \mathbf{b}_i) \mid \text{dist}(H(\mathbf{a}_i), \mathbf{b}_i) < \varepsilon\}|}{\max(|\mathbf{a}_i|, |\mathbf{b}_i|)}$$

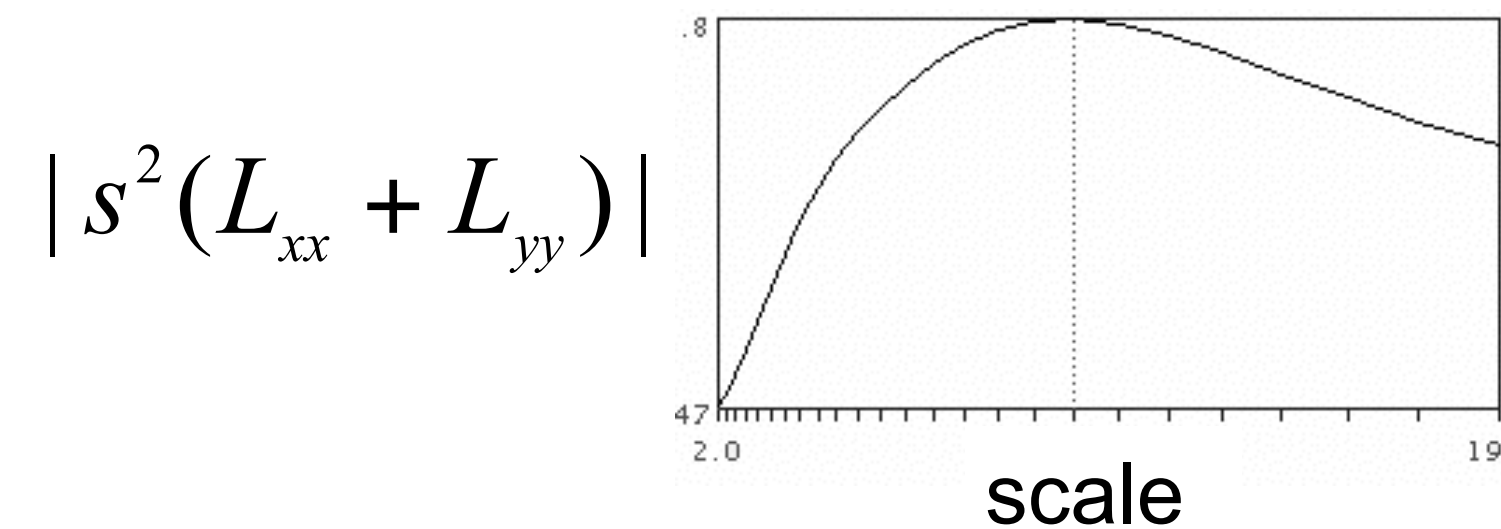
Harris detector with adaptation to scale

Scale-adapted derivative calculation



Scale selection

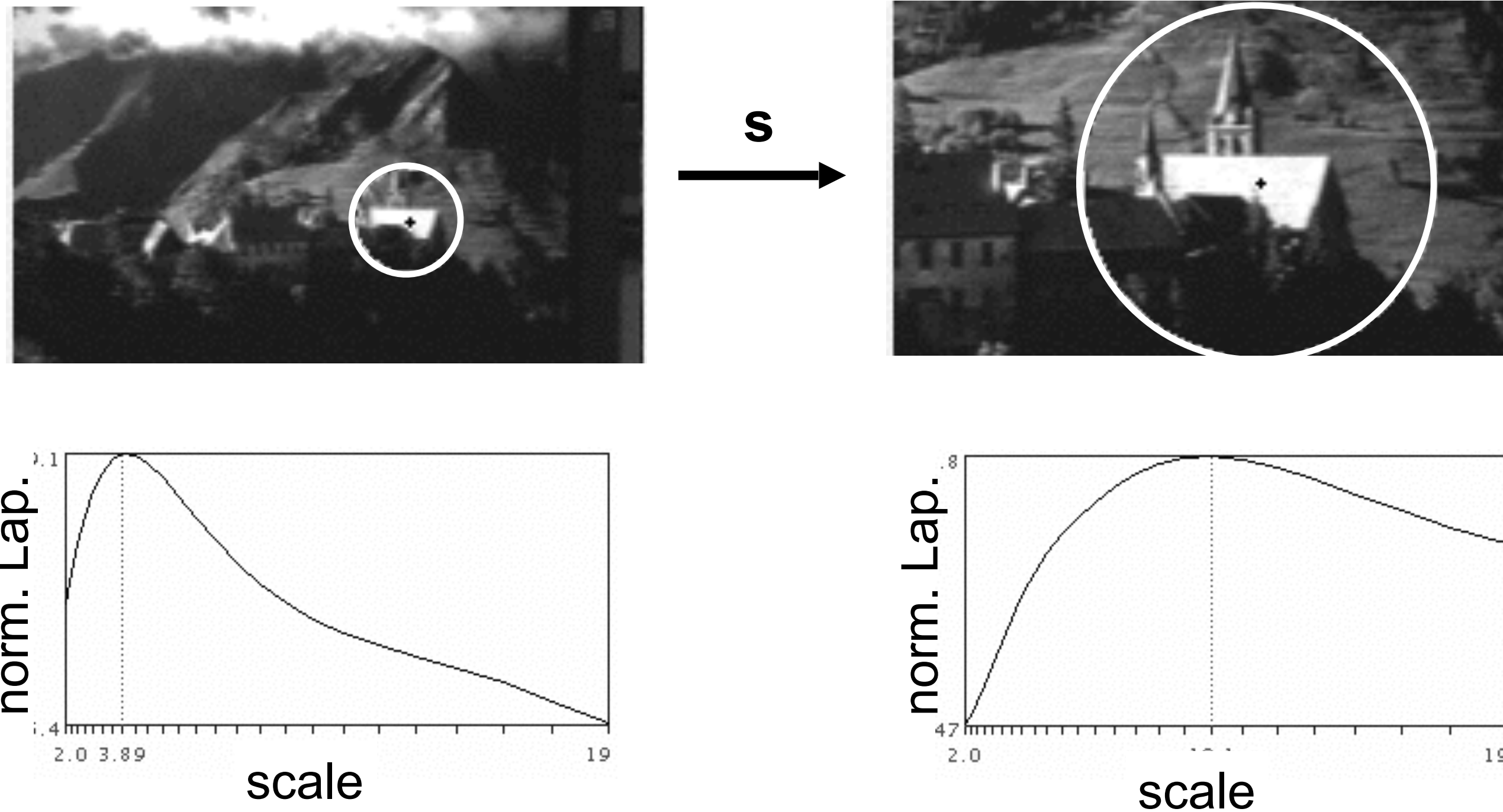
- For a point, compute a value (gradient, Laplacian etc.) at several scales
- Normalization of the values with the scale factor e.g., Laplacian $|s^2(L_{xx} + L_{yy})|$
- Select scale s^* at the maximum \rightarrow characteristic scale



- Experimental results show that the Laplacian gives best results

Scale selection

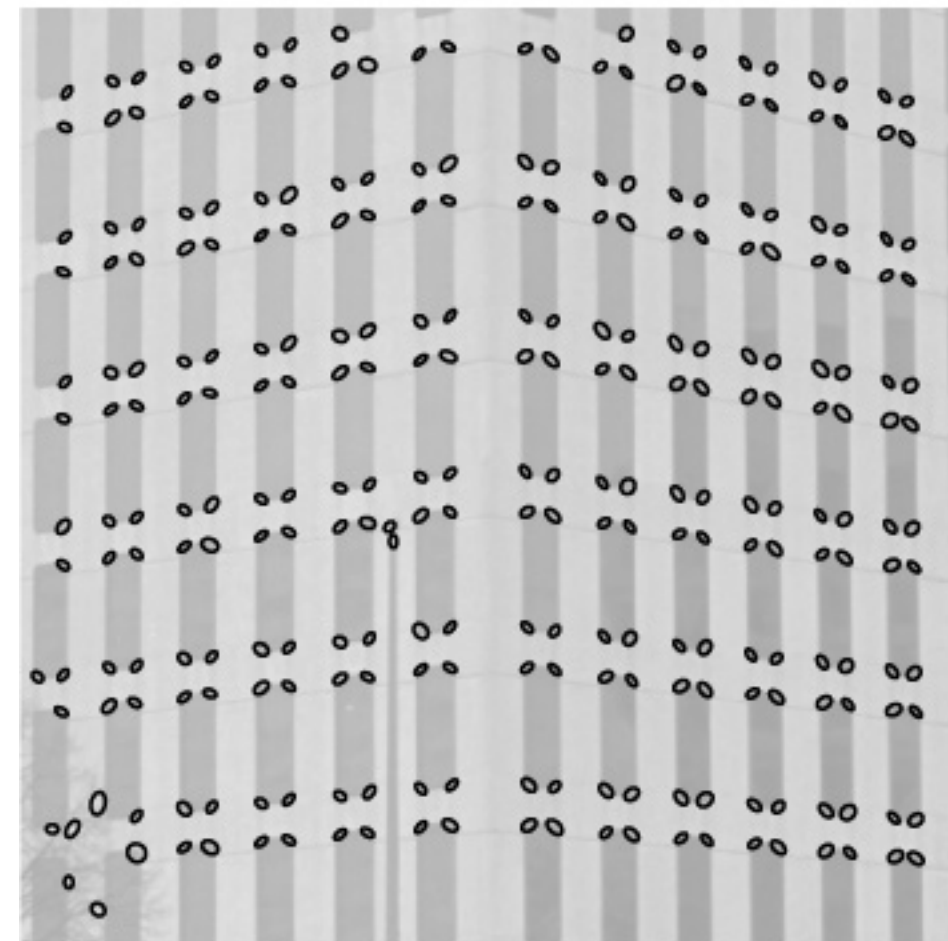
- Scale invariance of the characteristic scale



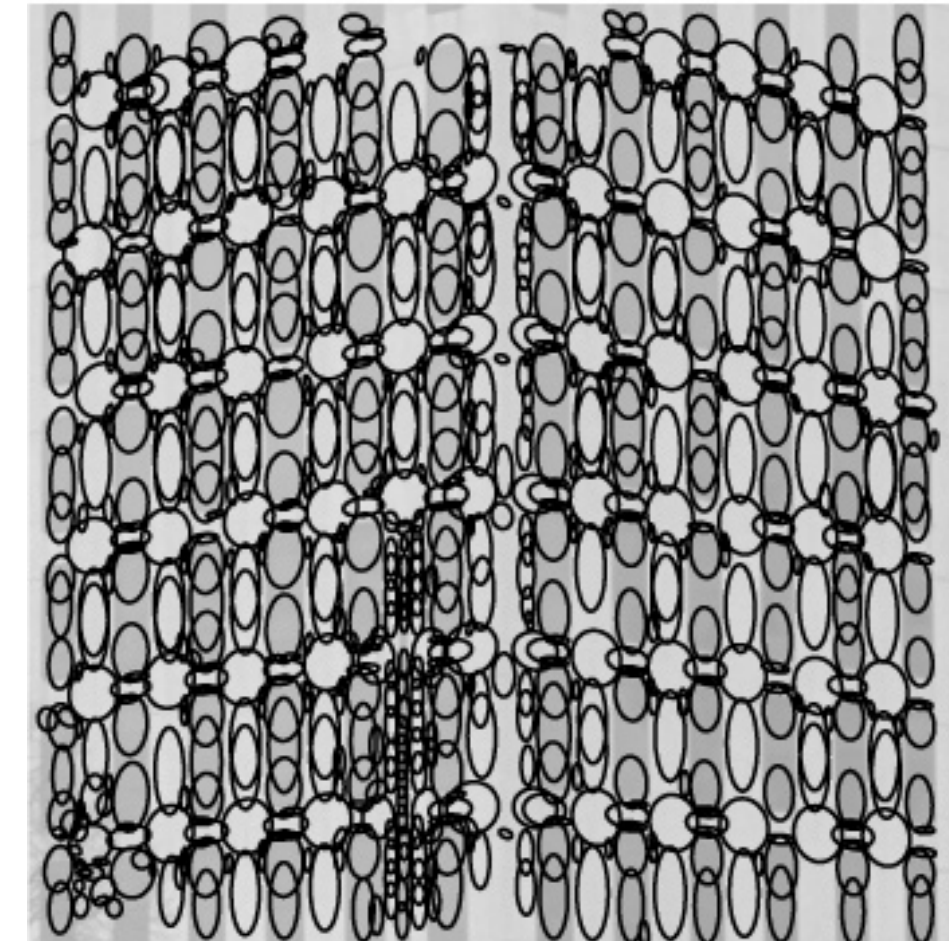
- Relation between characteristic scales $s \cdot s_1^* = s_2^*$

Scale-invariant detectors

- Harris-Laplace (Mikolajczyk & Schmid'01)
- Laplacian detector (Lindeberg'98)
- Difference of Gaussian (SIFT detector, Lowe'99)



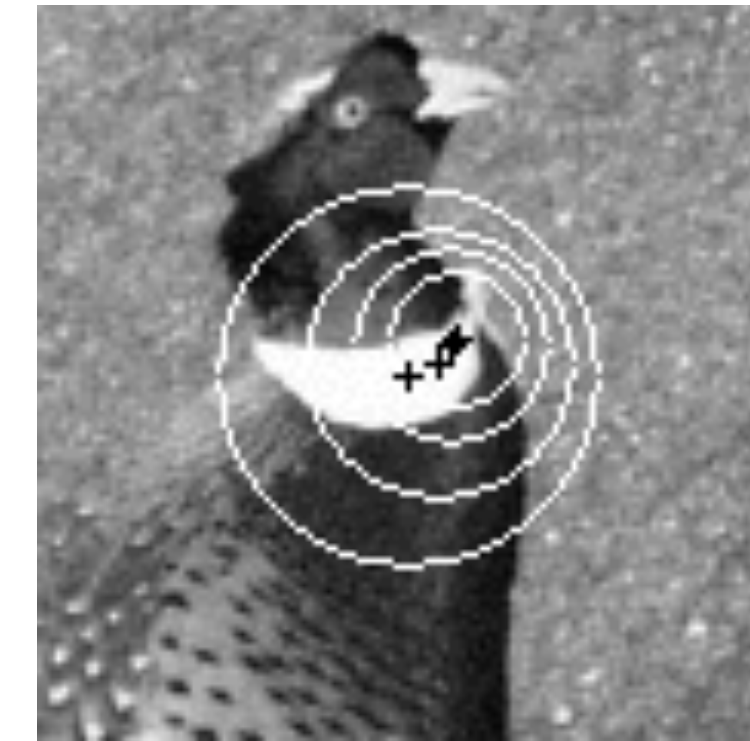
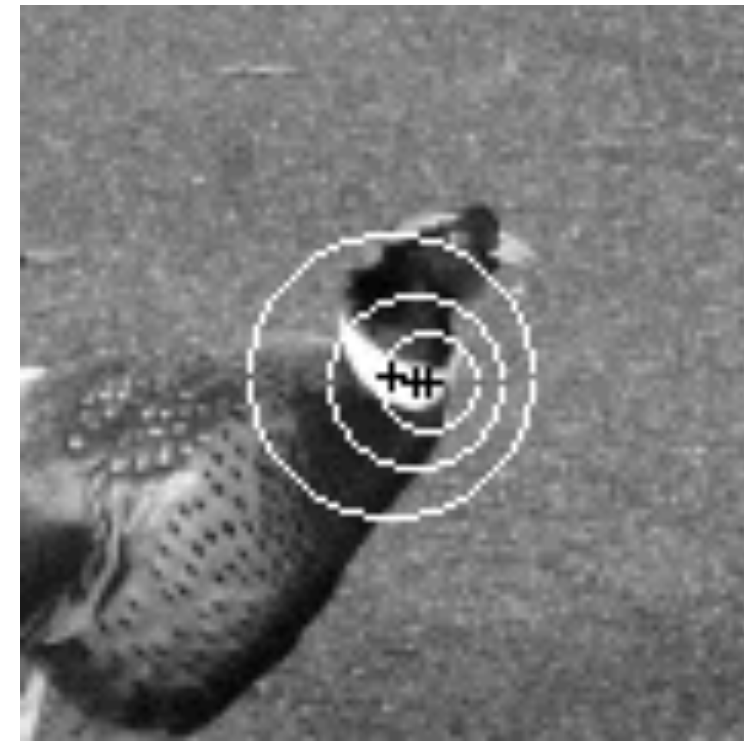
Harris-Laplace



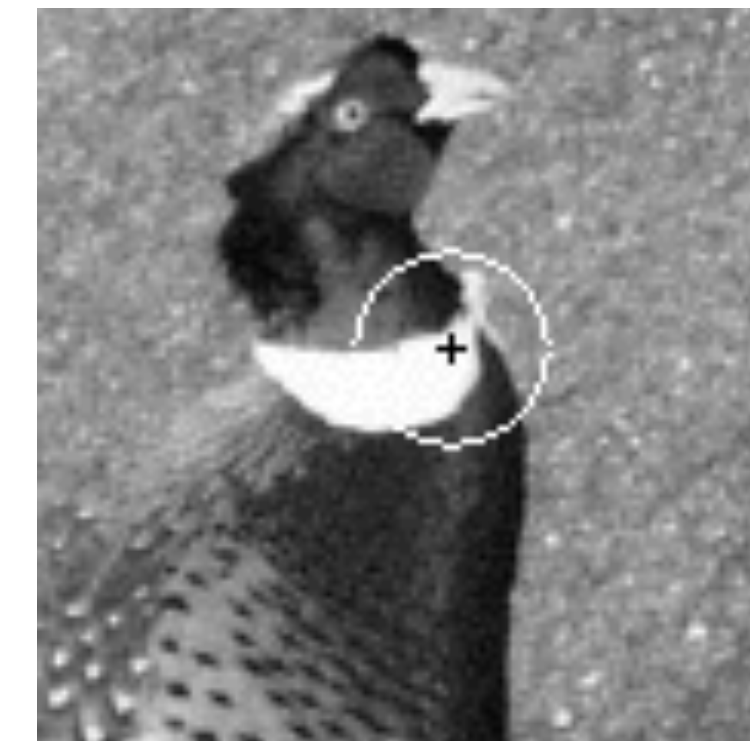
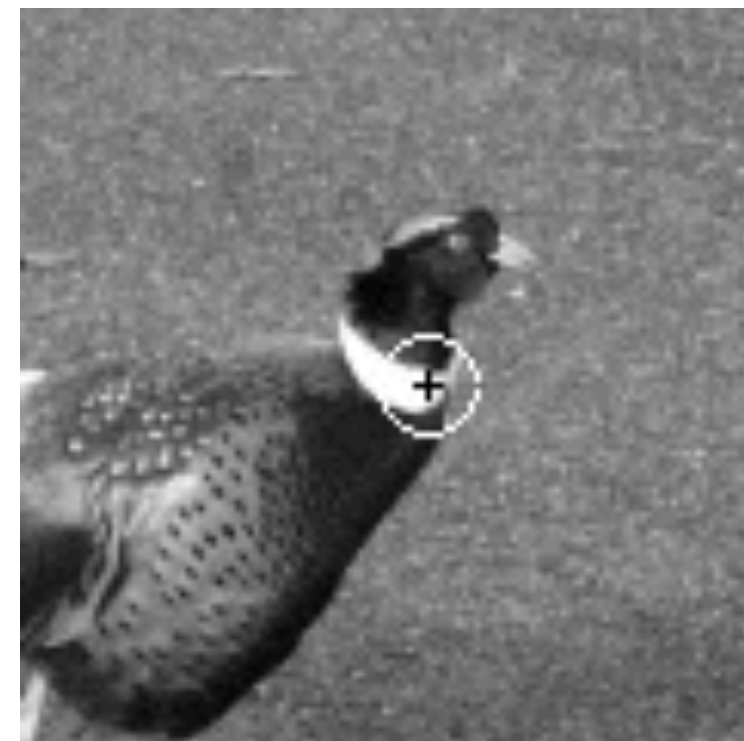
Laplacian

Harris-Laplace

multi-scale Harris points



selection of points at
maximum of Laplacian



➔ invariant points + associated regions [Mikolajczyk & Schmid'01]

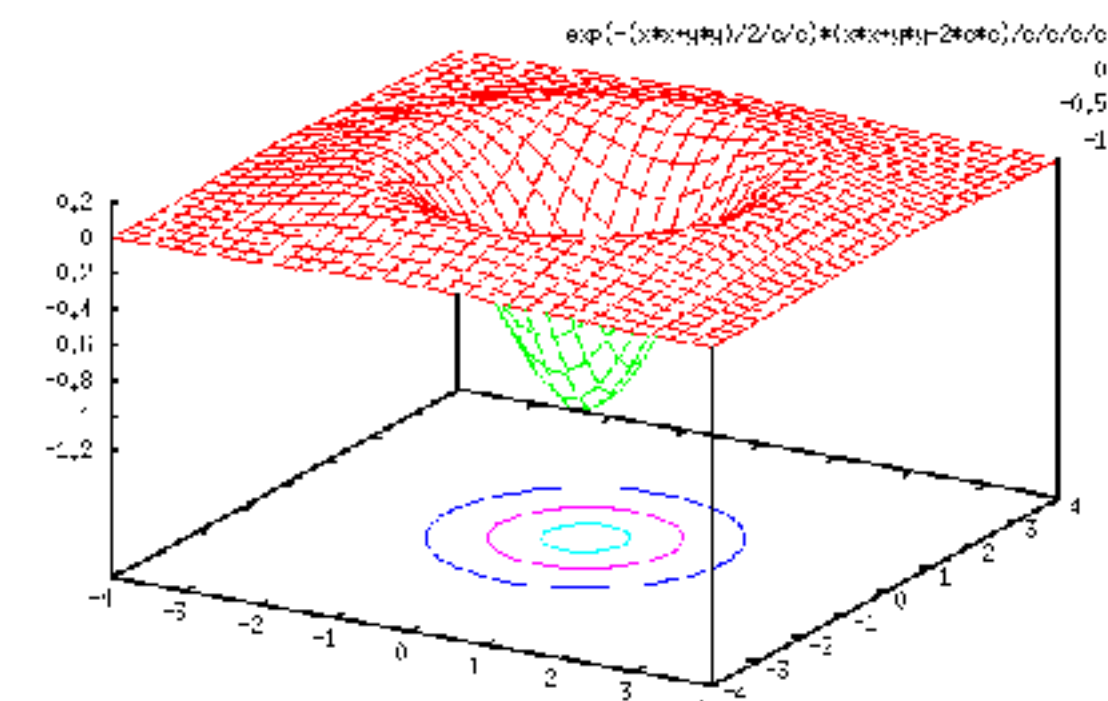
LOG detector

Laplacian of Gaussian (LOG): Circularly symmetric operator for **blob detection in 2D**

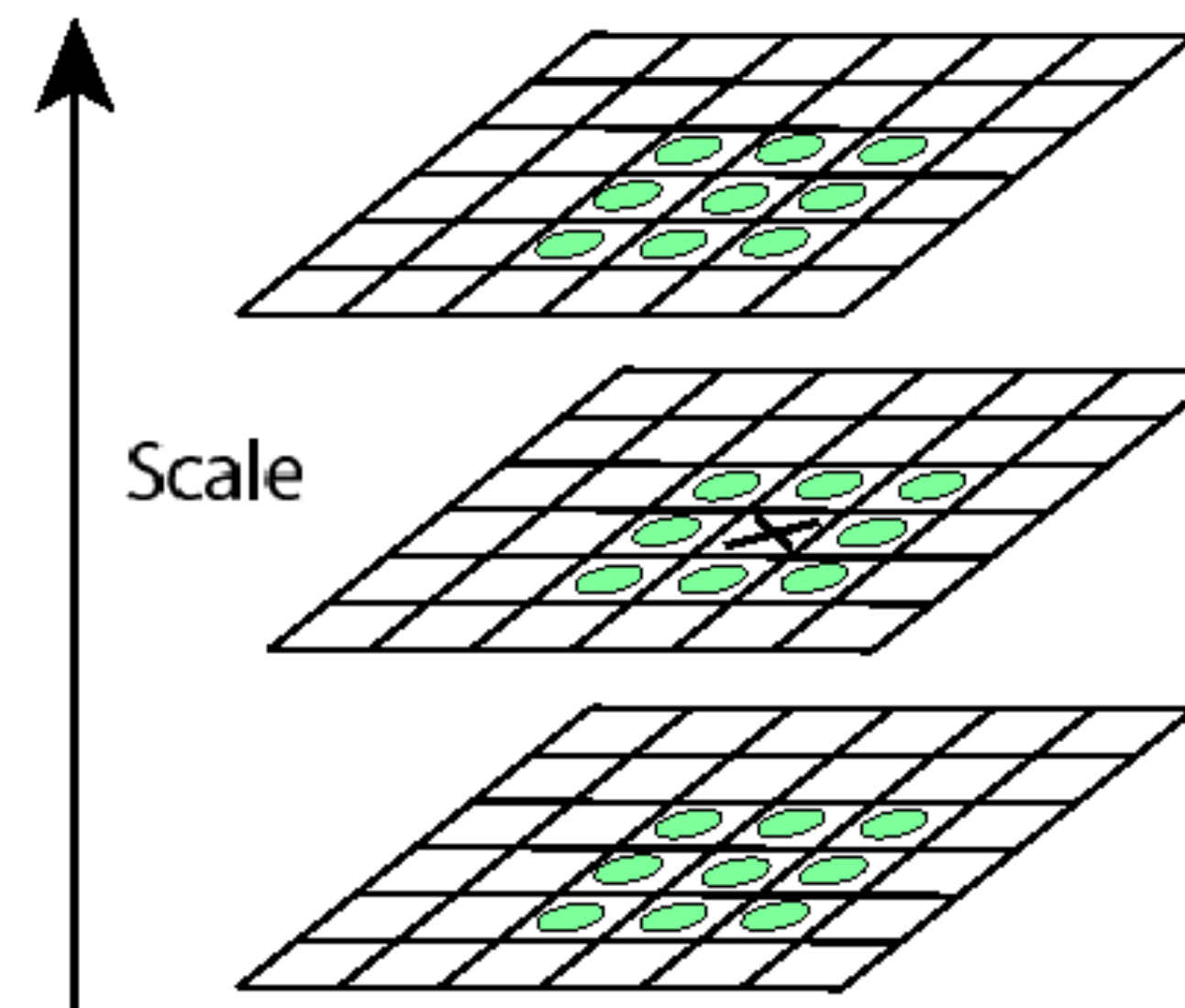
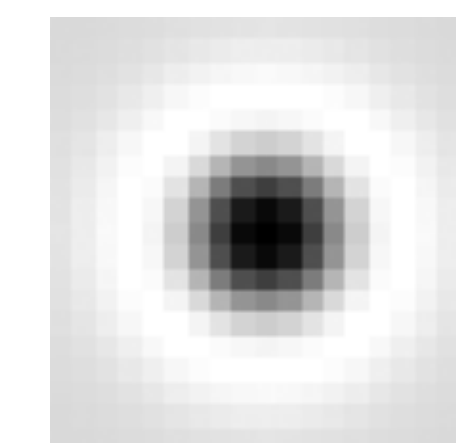
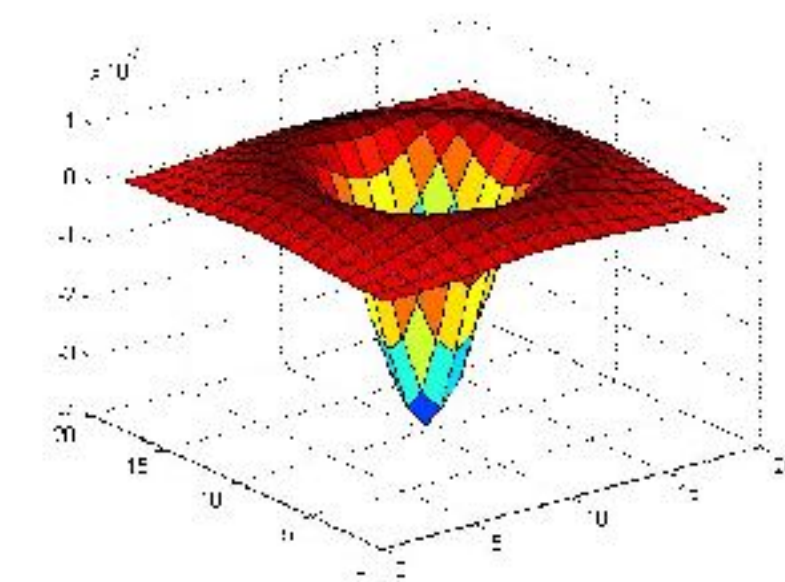
Convolve image with scale-normalized Laplacian at several scales

Detection of maxima and minima of Laplacian in scale space

$$\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$$



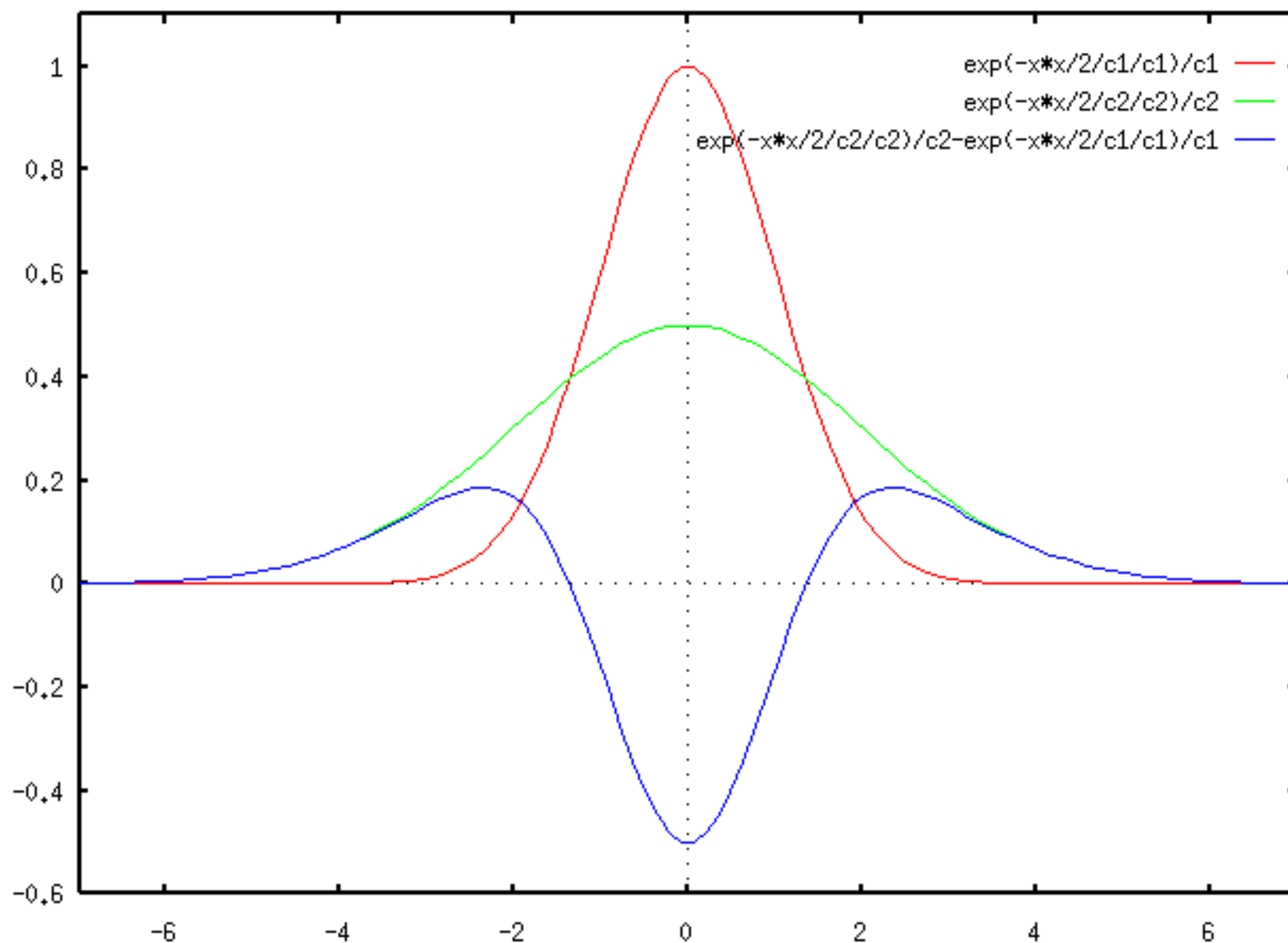
$$LOG = s^2 (G_{xx}(\sigma) + G_{yy}(\sigma))$$



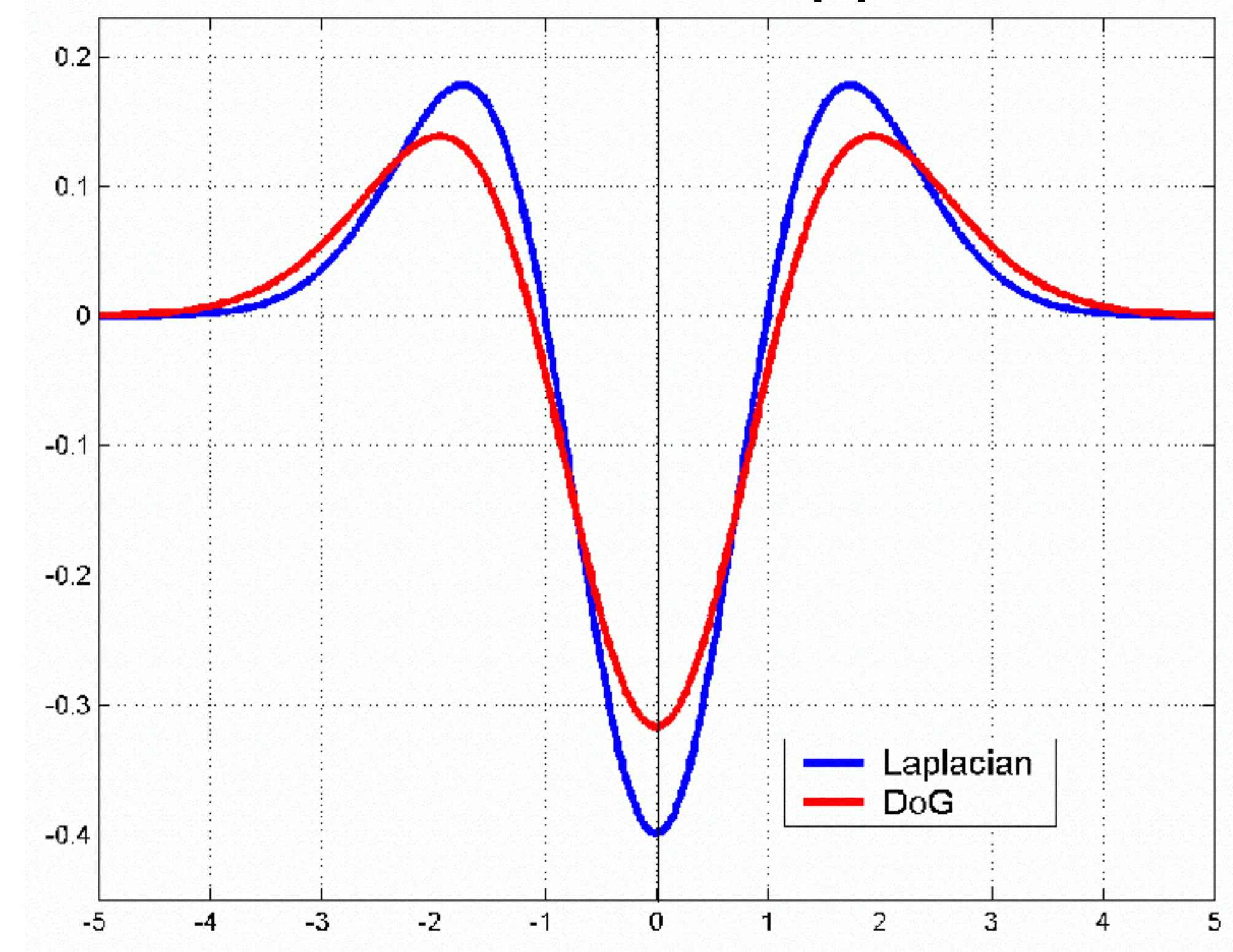
Efficient implementation: DOG (SIFT) detector

- Difference of Gaussian (DOG) approximates the Laplacian

$$DOG = G(k\sigma) - G(\sigma)$$

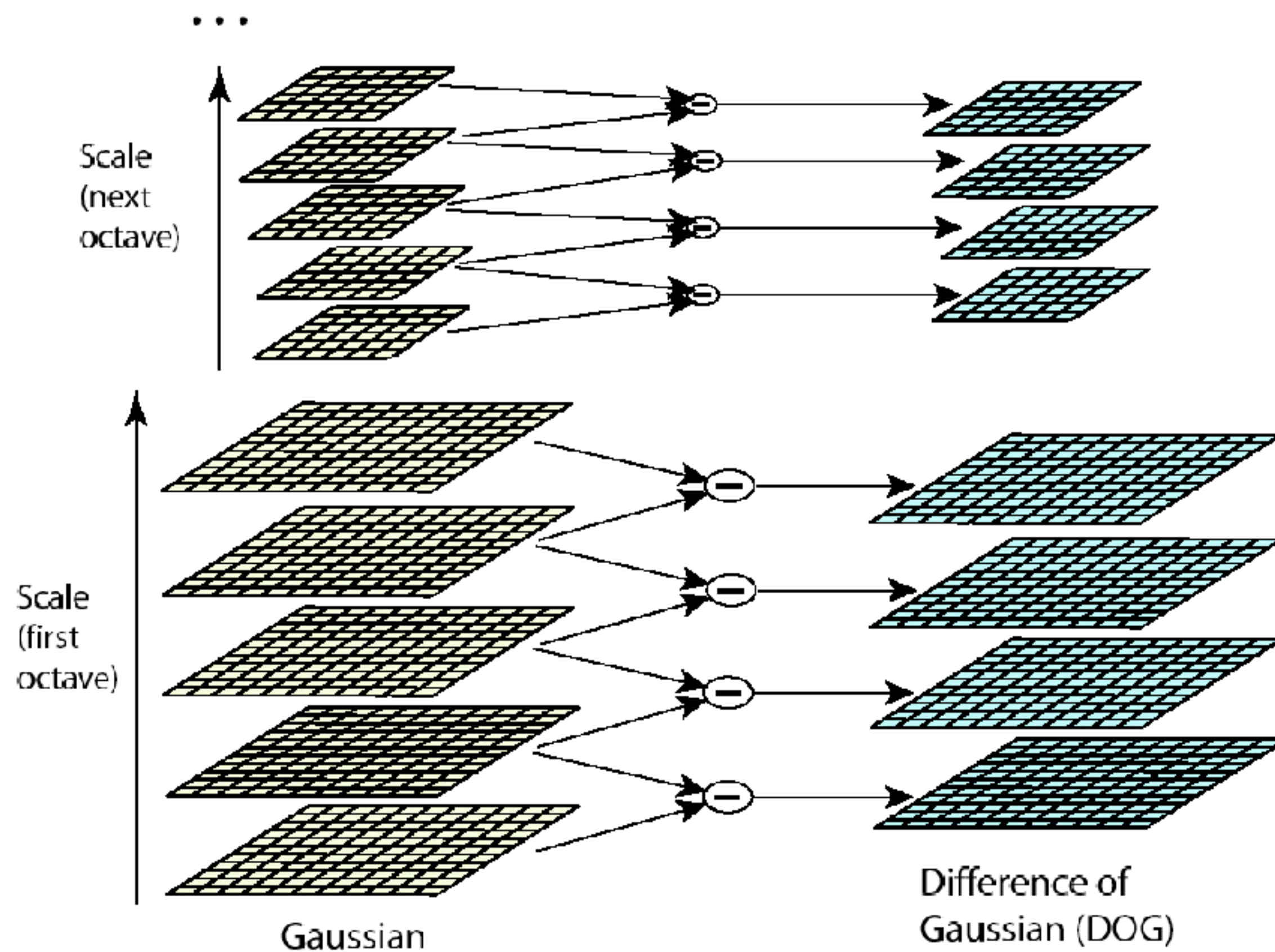


- Error due to the approximation



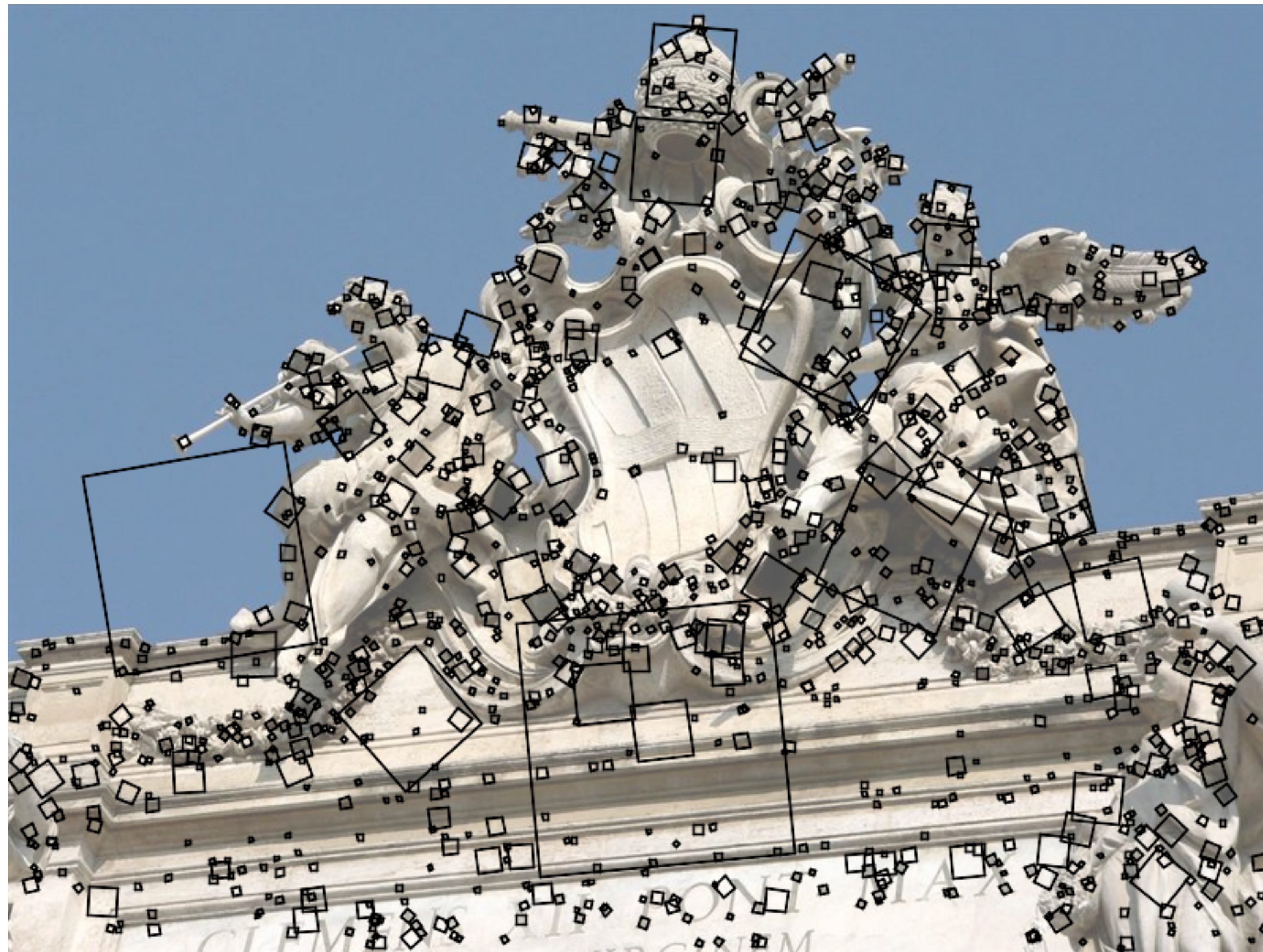
Efficient implementation: DOG (SIFT) detector

- Fast computation, scale space processed one octave at a time



David G. Lowe. "Distinctive image features from scale-invariant keypoints." *IJCV* 60 (2), 2004.

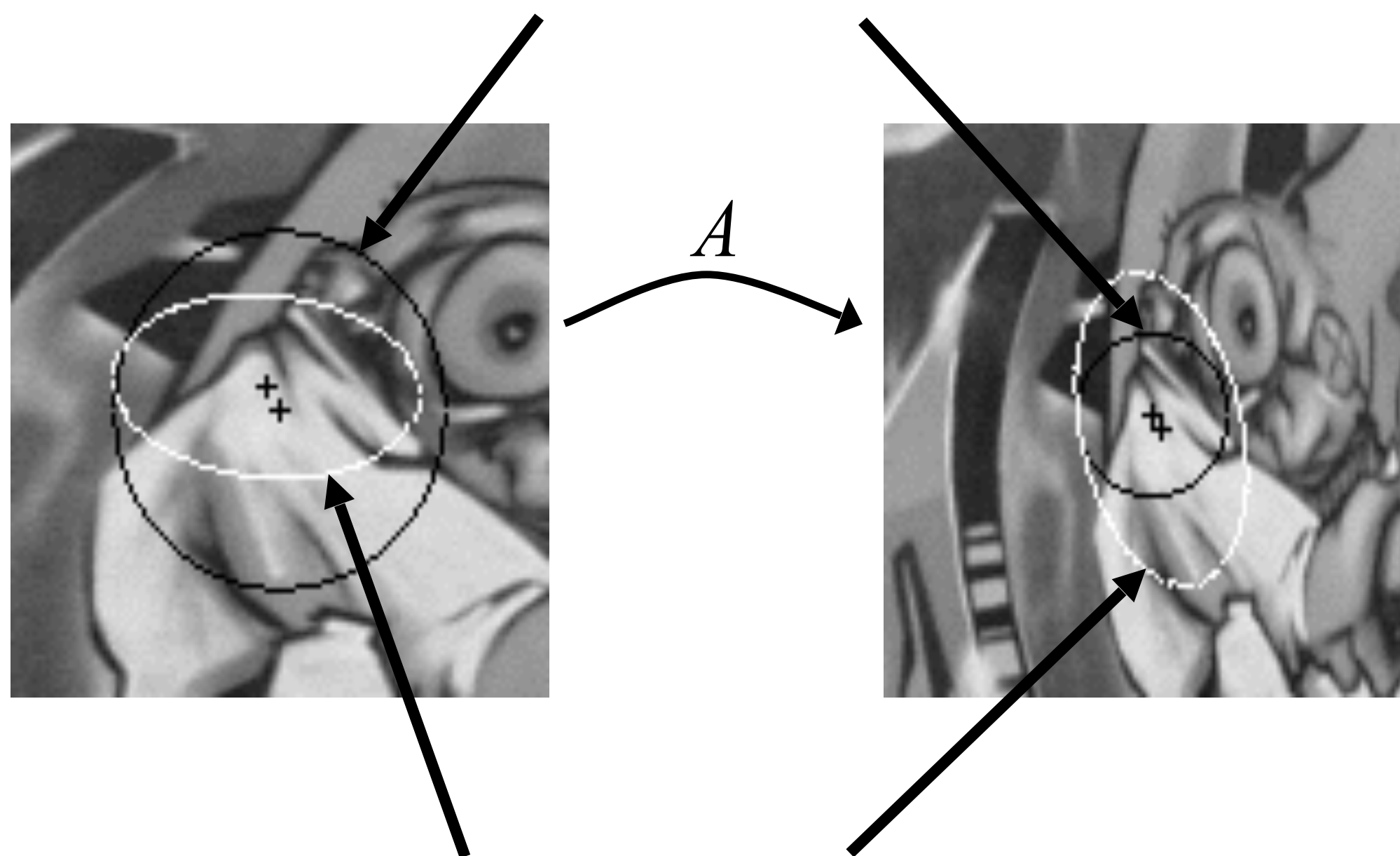
Efficient implementation: DOG (SIFT) detector



Not covered: Affine invariant regions

- Scale invariance is not sufficient for large baseline changes

detected scale invariant region



projected regions, viewpoint changes can locally be approximated by an affine transformation A

We have detected interest points, let's now
compare patches around those points.

Agenda: Instance-level recognition

- 1) Introduction to local features
- 2) Interest point detectors (e.g., Harris, scale invariance)
- 3) Comparison of patches (SSD, ZNCC on pixel values)
- 4) Feature descriptors (e.g., SIFT)
- 5) Matching and recognition with local features
- 6) Local feature aggregation for a single image-level description

Comparison of patches - SSD (sum of squared differences)

Comparison of the intensities in the neighborhood of two interest points

$$\frac{1}{(2N+1)^2} \sum_{i=-N}^N \sum_{j=-N}^N (I_1(x_1 + i, y_1 + j) - I_2(x_2 + i, y_2 + j))^2$$

Small difference values \rightarrow similar patches

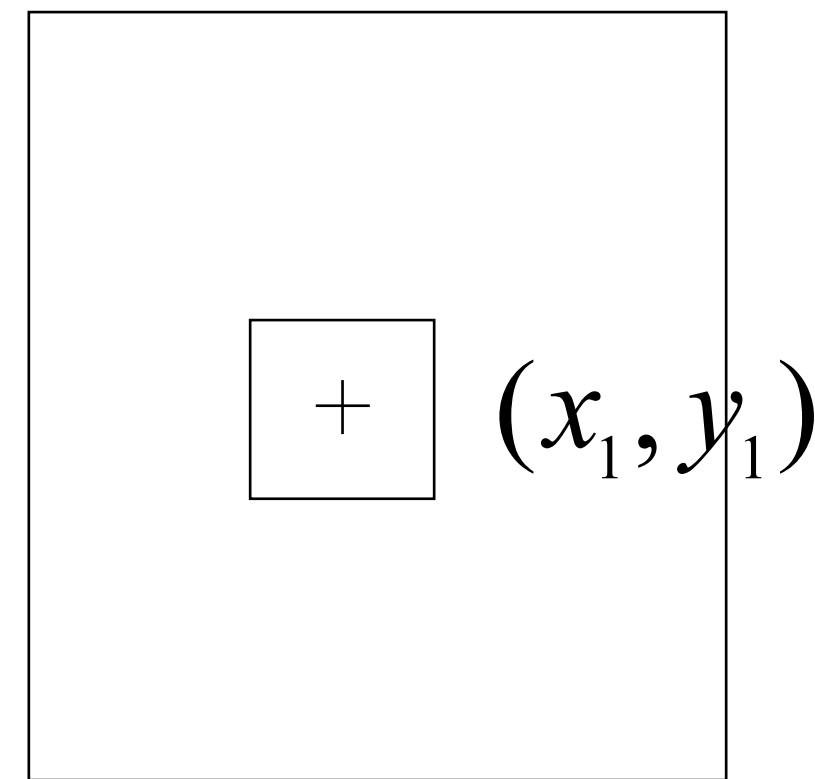


image 1

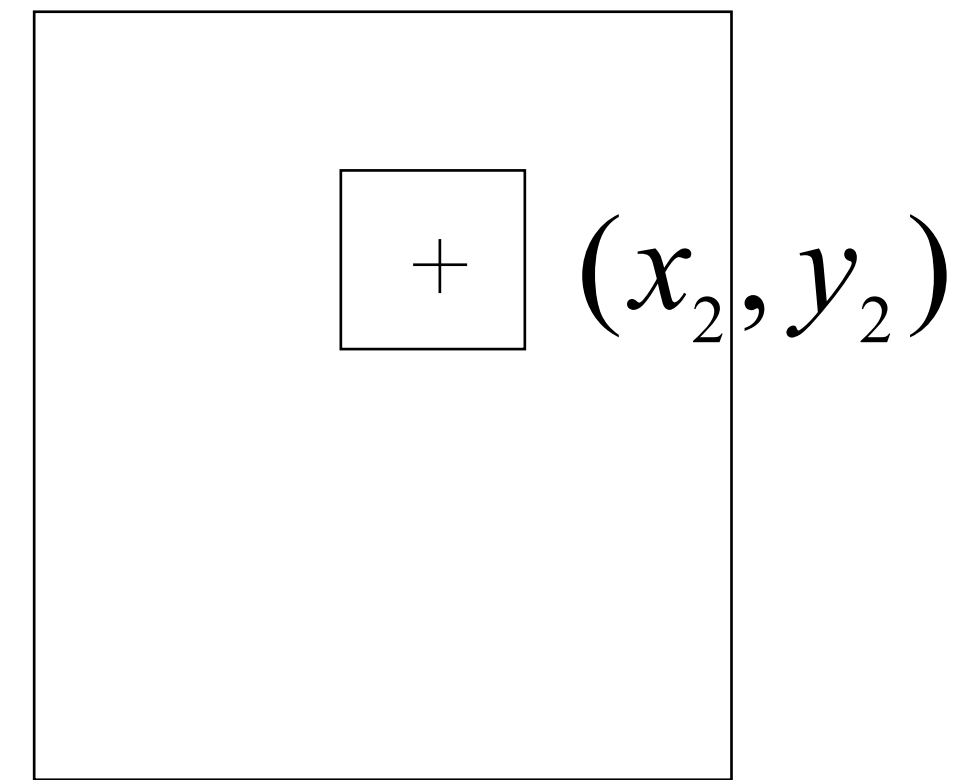


image 2

Comparison of patches - Zero-normalized SSD

$$\text{SSD} : \frac{1}{(2N+1)^2} \sum_{i=-N}^N \sum_{j=-N}^N (I_1(x_1 + i, y_1 + j) - I_2(x_2 + i, y_2 + j))^2$$

Invariance to photometric transformations?

Intensity changes ($I \rightarrow I + b$)

=> Normalizing with the mean of each patch

$$\frac{1}{(2N+1)^2} \sum_{i=-N}^N \sum_{j=-N}^N ((I_1(x_1 + i, y_1 + j) - m_1) - (I_2(x_2 + i, y_2 + j) - m_2))^2$$

Intensity changes ($I \rightarrow aI + b$)

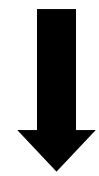
=> Normalizing with the mean and standard deviation of each patch

$$\frac{1}{(2N+1)^2} \sum_{i=-N}^N \sum_{j=-N}^N \left(\frac{I_1(x_1 + i, y_1 + j) - m_1}{\sigma_1} - \frac{I_2(x_2 + i, y_2 + j) - m_2}{\sigma_2} \right)^2$$

Zero-normalized cross correlation (ZNCC)

Zero-normalized SSD (sum of squared differences)

$$\frac{1}{(2N+1)^2} \sum_{i=-N}^N \sum_{j=-N}^N \left(\frac{I_1(x_1 + i, y_1 + j) - m_1}{\sigma_1} - \frac{I_2(x_2 + i, y_2 + j) - m_2}{\sigma_2} \right)^2$$



ZNCC

$$\frac{1}{(2N+1)^2} \sum_{i=-N}^N \sum_{j=-N}^N \left(\frac{I_1(x_1 + i, y_1 + j) - m_1}{\sigma_1} \right) \cdot \left(\frac{I_2(x_2 + i, y_2 + j) - m_2}{\sigma_2} \right)$$

ZNCC values between -1 and 1, 1 when identical patches
in practice threshold around 0.5

Invariance to rotation?

Agenda: Instance-level recognition

- 1) Introduction to local features
- 2) Interest point detectors (e.g., Harris, scale invariance)
- 3) Comparison of patches (SSD, ZNCC on pixel values)
- 4) Feature descriptors (e.g., SIFT)
- 5) Matching and recognition with local features
- 6) Local feature aggregation for a single image-level description

Local descriptors (patch representation)

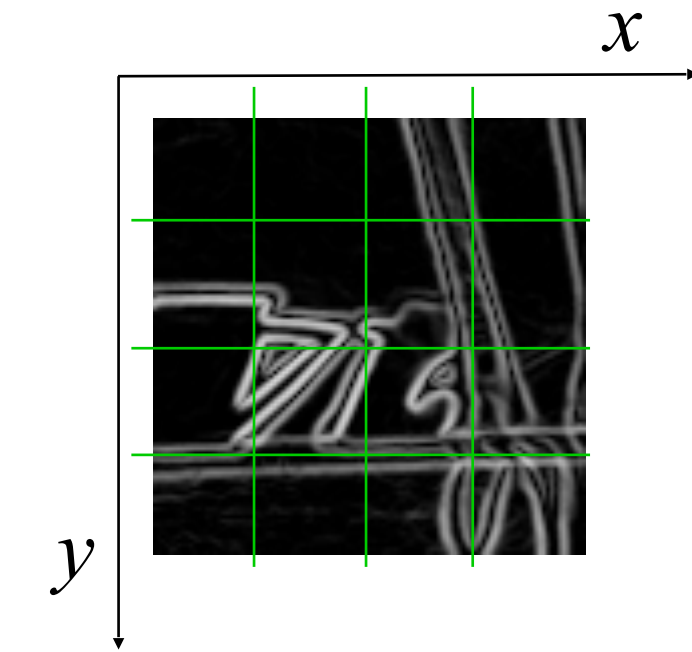
- Pixel values
- Greyvalue derivatives, differential invariants [Koenderink'87]
- SIFT descriptor [Lowe'99]
- SURF descriptor [Bay et al.'08]
- DAISY descriptor [Tola et al.'08, Windler et al.'09]
- LIOP descriptor [Wang et al.'11]
- Patch descriptors based on CNN features [Brox et al.'15, Paulin et al.'15, Zagoruyko'15...]
- ...

SIFT descriptor [Lowe'99]

image patch



gradient

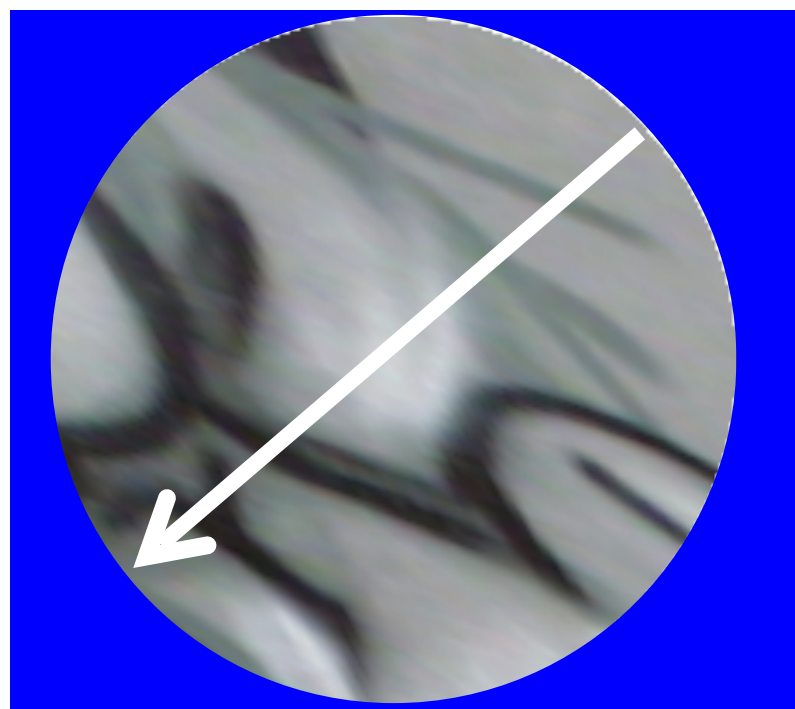
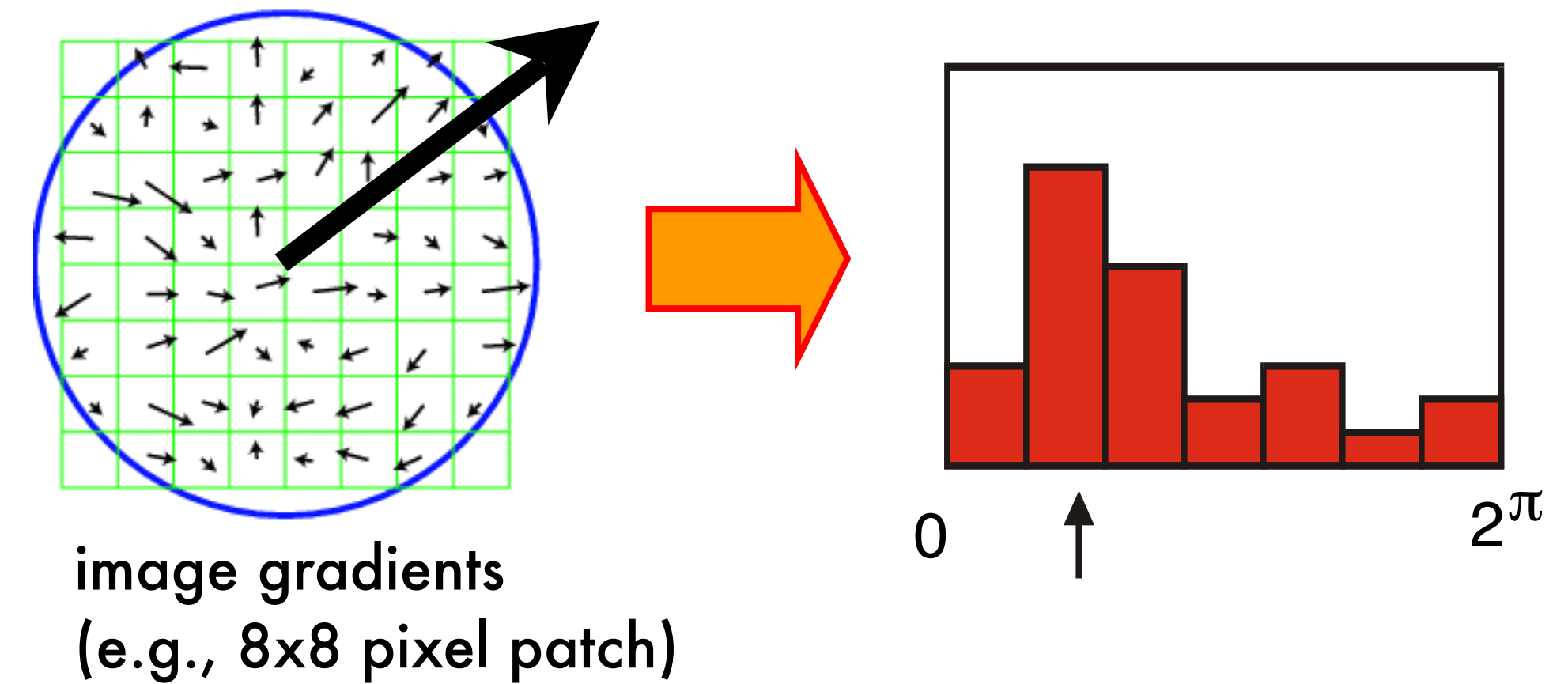


- Descriptor computation:
 - Divide patch into 4x4 sub-patches
 - Compute histogram of gradient orientations (8 reference angles) inside each sub-patch
 - Resulting descriptor: $4 \times 4 \times 8 = 128$ dimensions
- Advantage over raw vectors of pixel values
 - Gradients less sensitive to illumination change
 - Pooling of gradients over the sub-patches achieves robustness to small shifts, but still preserves some spatial information
- Soft-assignment to spatial bins
- Normalization of the descriptor to norm one
 - Robustness to illumination changes
- Comparison with Euclidean distance

SIFT descriptor - rotation invariance

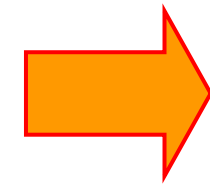
(Rotational normalization)

- Estimation of the dominant orientation
 - Extract gradient orientations
 - Create histogram over gradient orientations in the patch
 - Assign canonical orientation at peak of this histogram
- Rotate patch in dominant direction

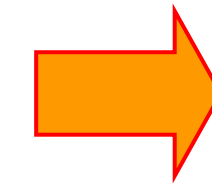
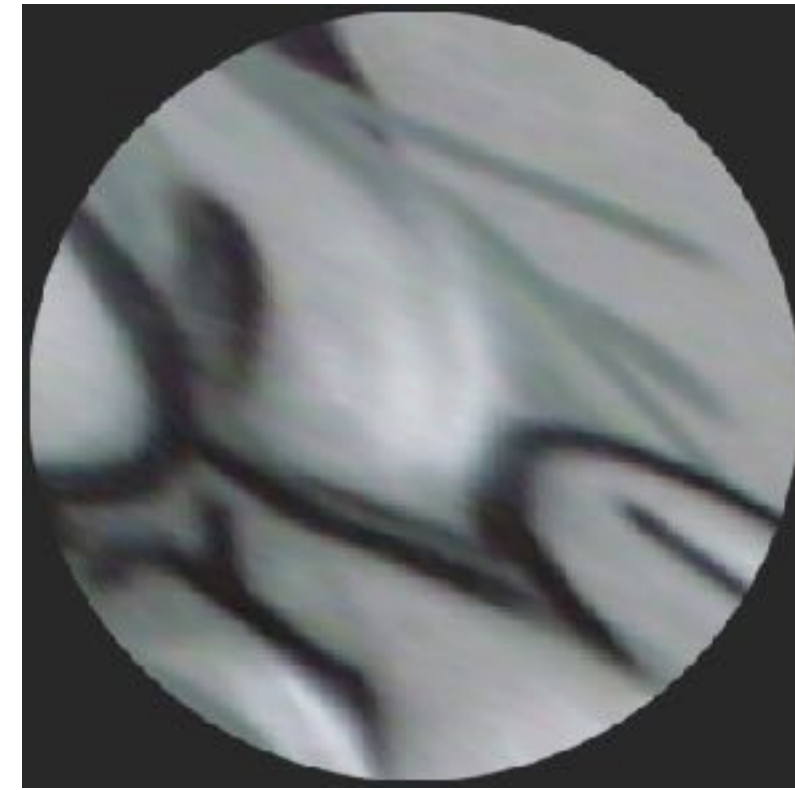


SIFT descriptor - rotation invariance

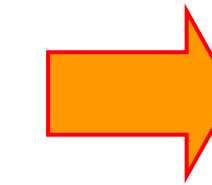
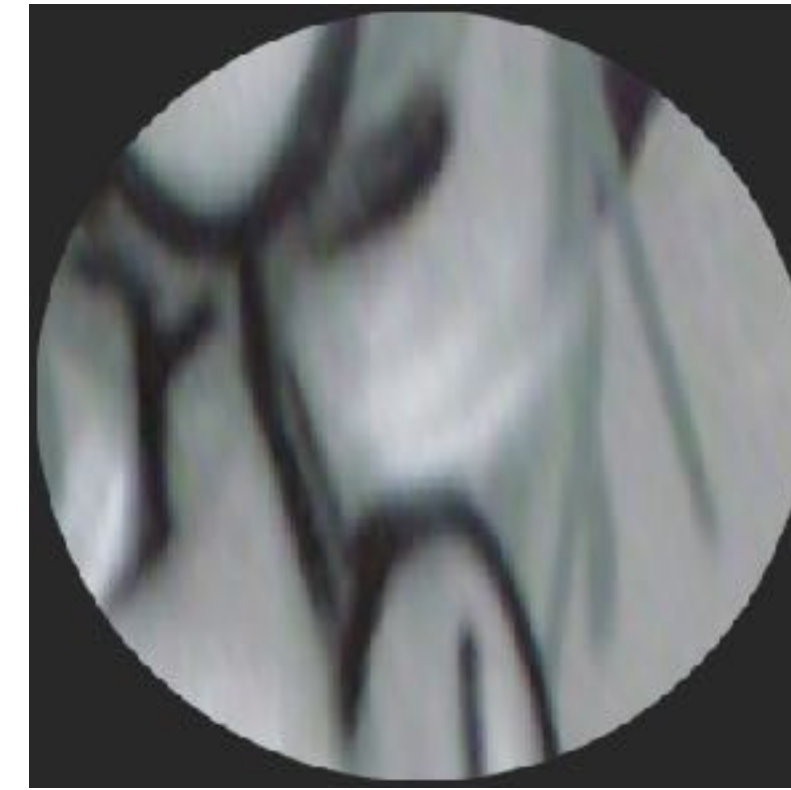
Extract affine regions



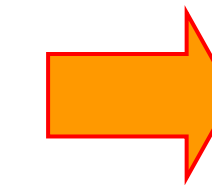
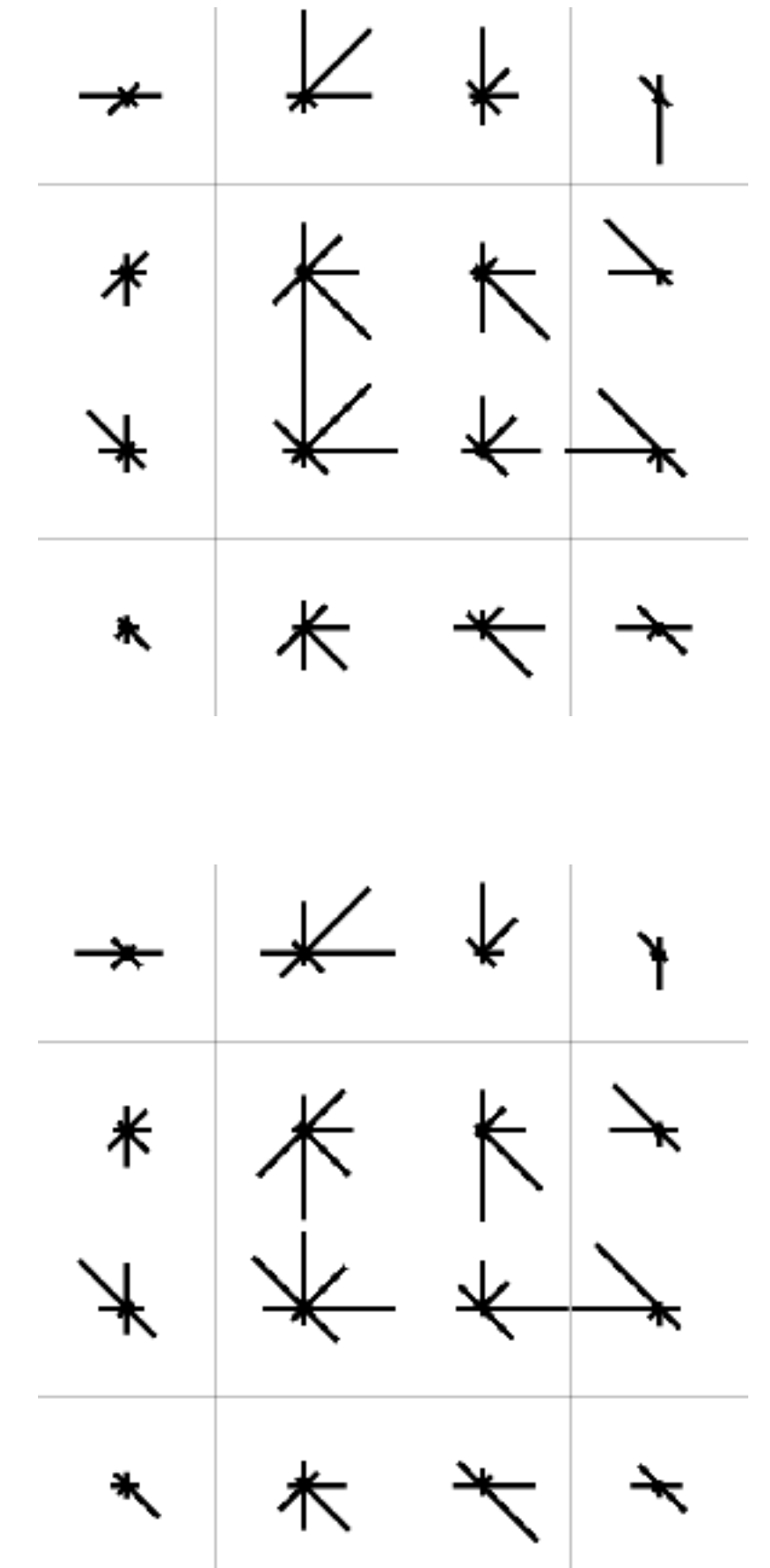
Normalize regions



Eliminate rotational ambiguity



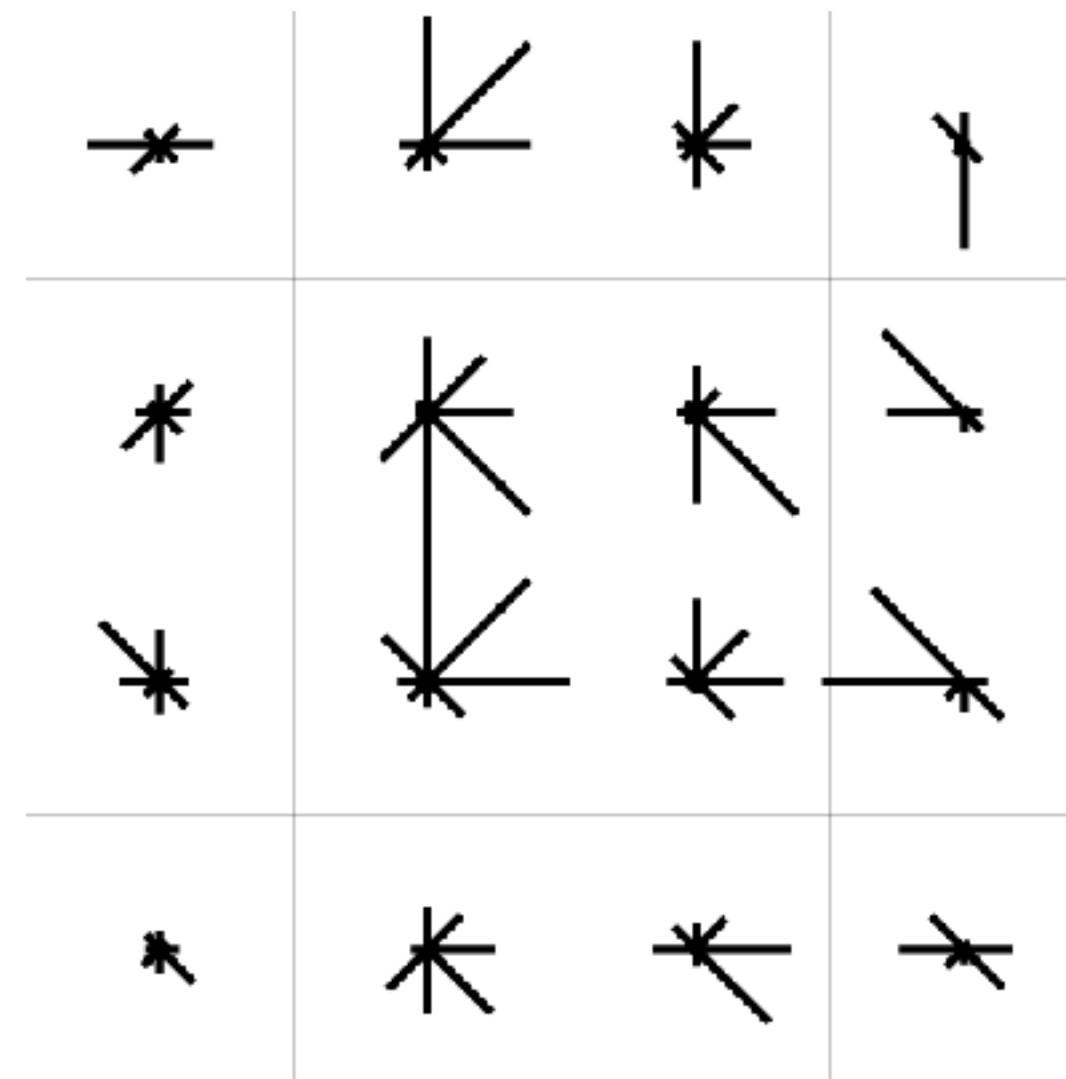
Compute appearance descriptors



SIFT detector and SIFT descriptor

SIFT detector
Interest points

SIFT descriptor
128-d representation of the patch



(Parenthesis: CNN based descriptors)

“Learned” features in upcoming lectures

- **Based on global / full image features**

- Does not find patch-level matches

- More compact

- Example: Deep Image Retrieval: Learning global representations for image search (DIR) [ECCV 2016]

- **Based on local features**

- Patch-level matches possible

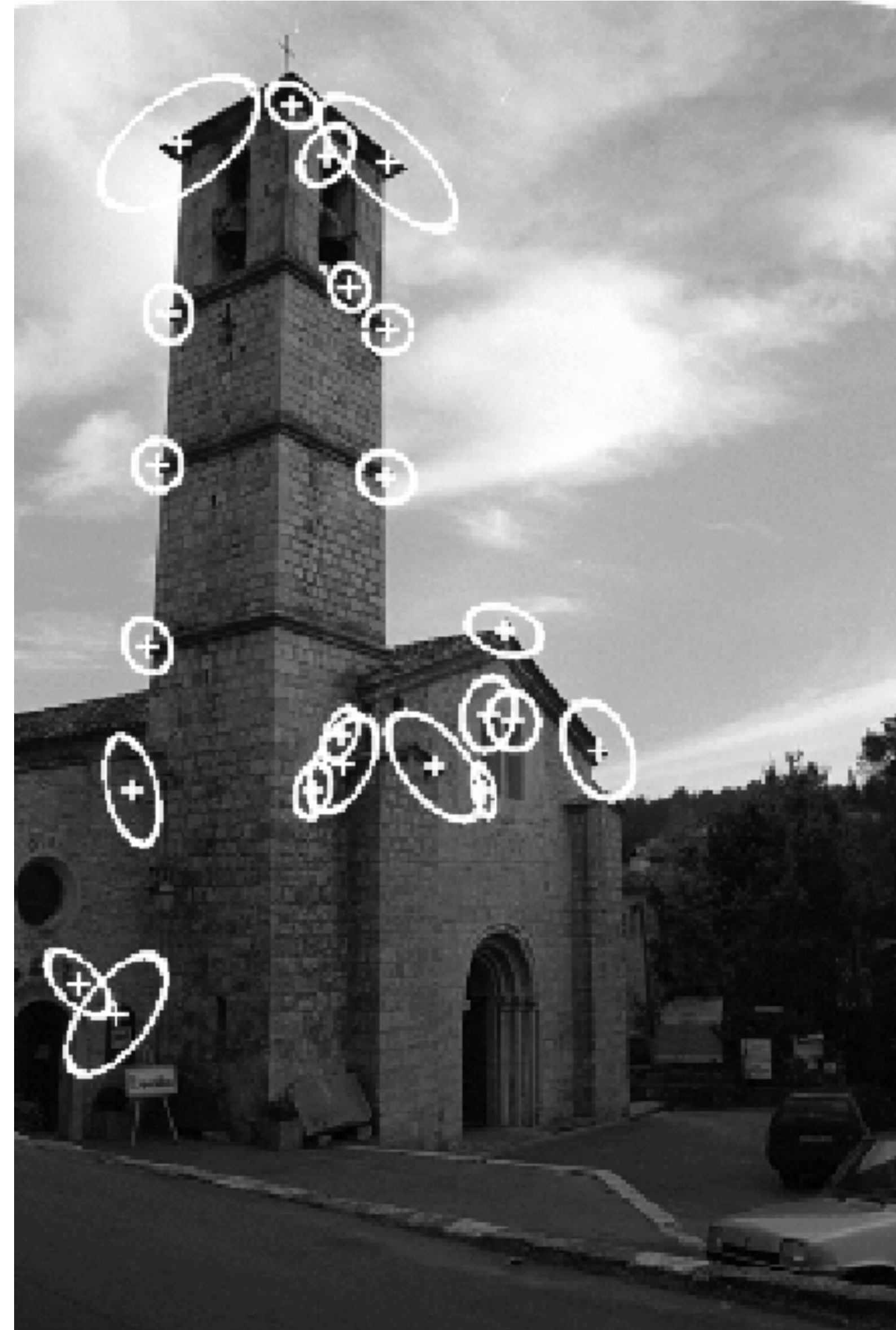
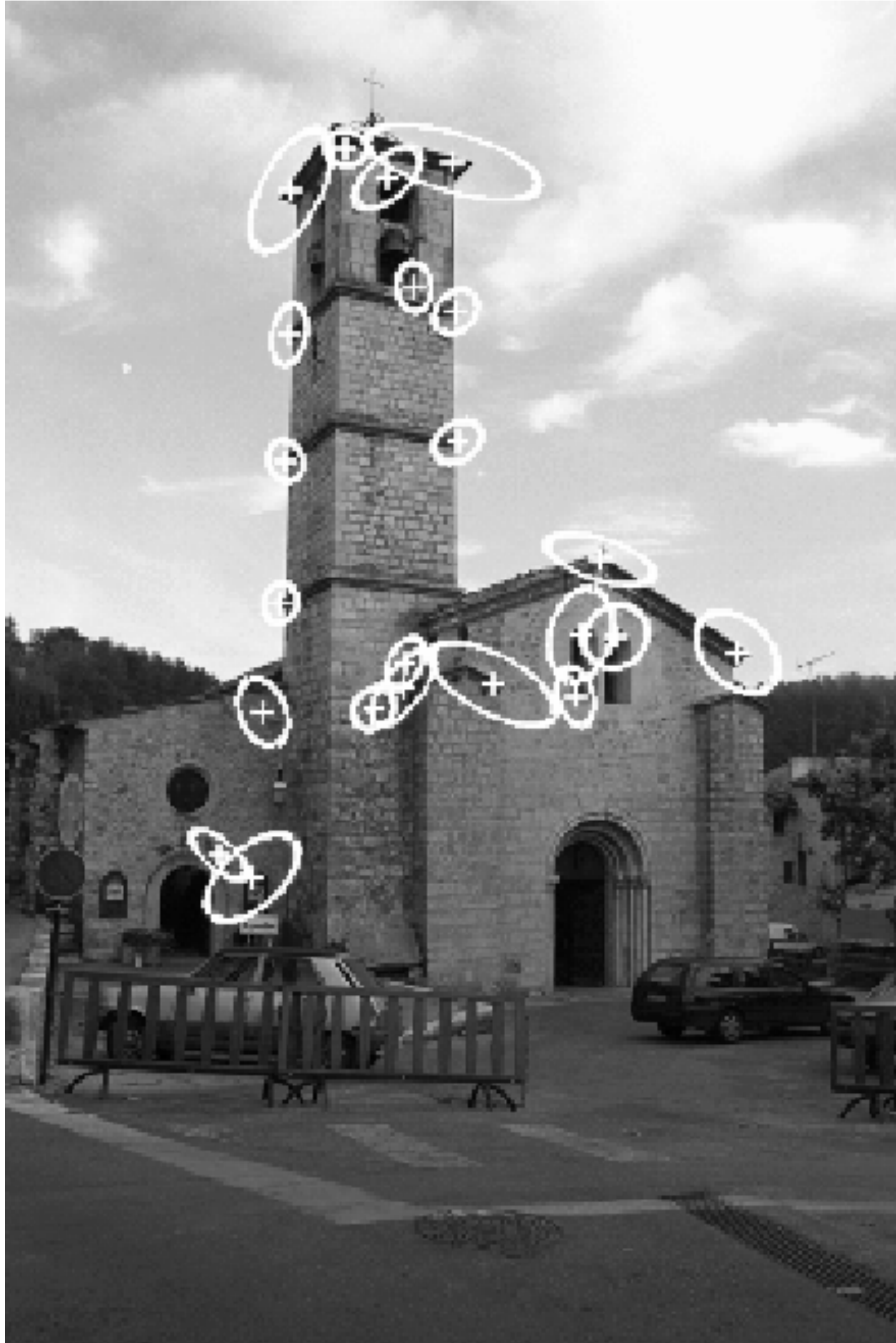
- Indexing scheme necessary

- Example: Large-Scale Image Retrieval with Attentive Deep Local Features (DELF) [ICCV 2017]

Agenda: Instance-level recognition

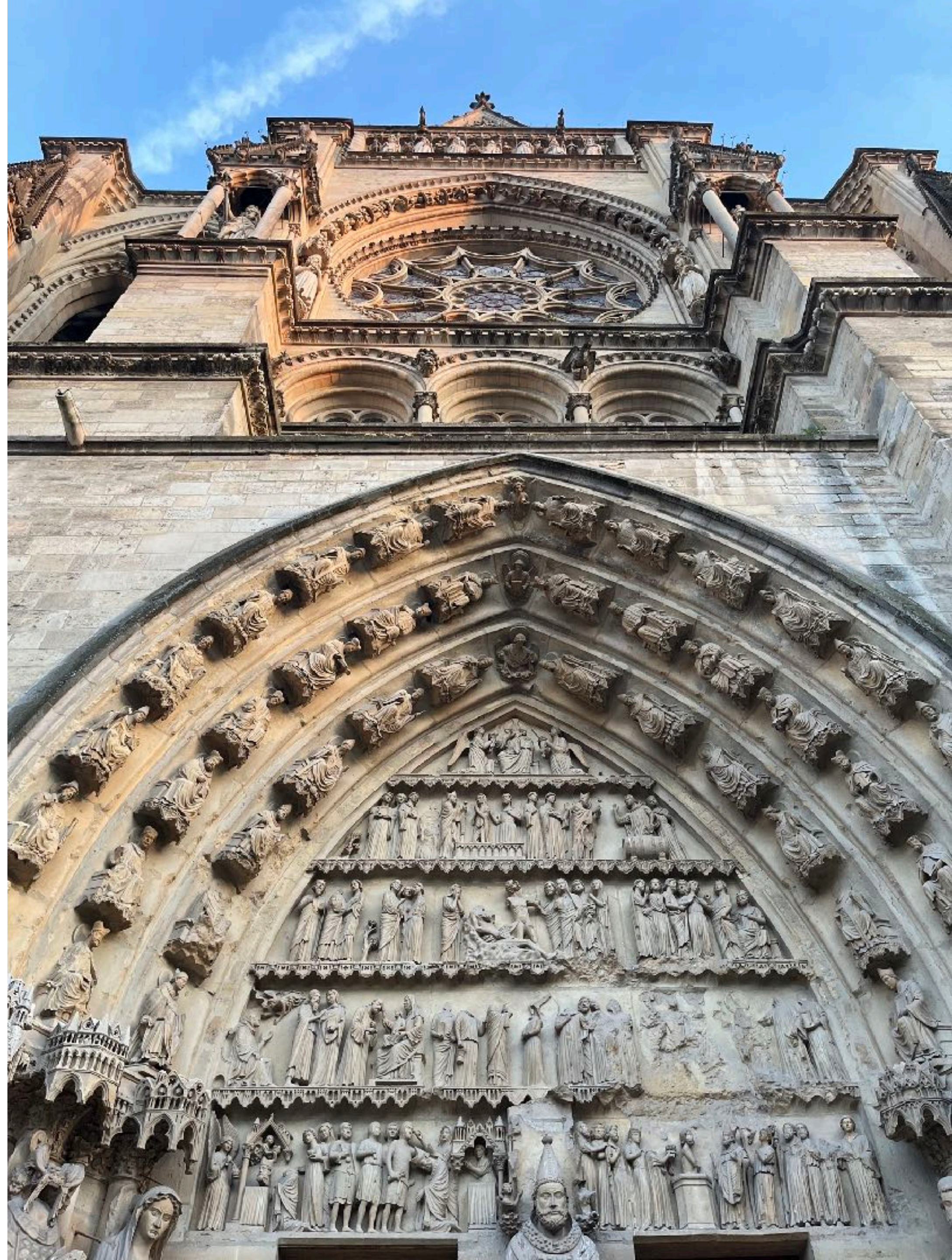
- 1) Introduction to local features
- 2) Interest point detectors (e.g., Harris, scale invariance)
- 3) Comparison of patches (SSD, ZNCC on pixel values)
- 4) Feature descriptors (e.g., SIFT)
- 5) Matching and recognition with local features
- 6) Local feature aggregation for a single image-level description

Matching of descriptors



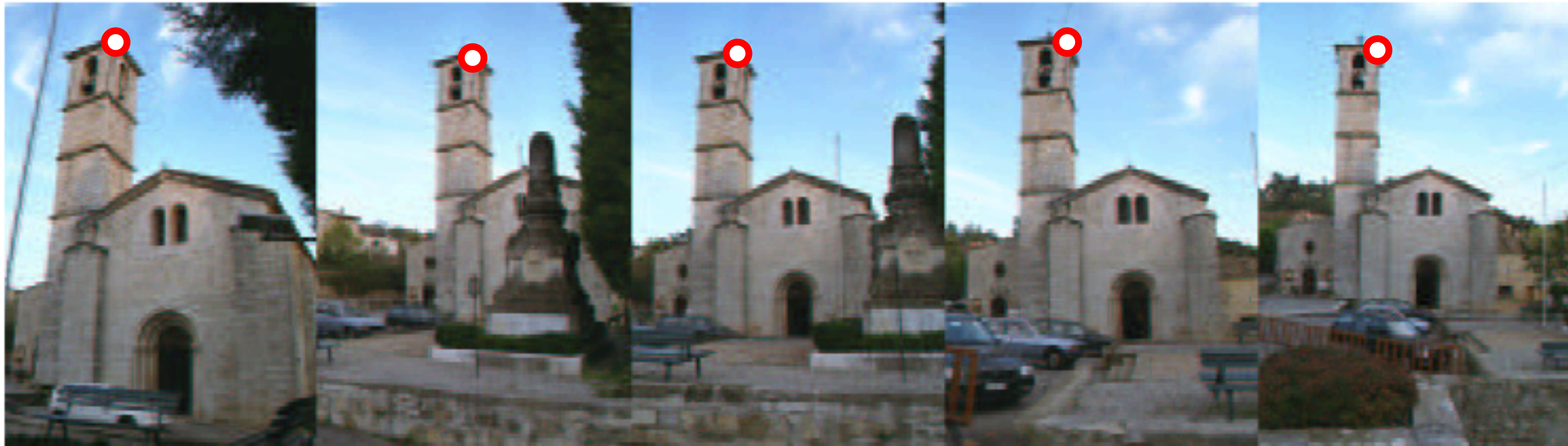
Matching of descriptors





Matching and 3D reconstruction

- Establish correspondence between two (or more) images



[Schaffalitzky and Zisserman ECCV 2002]

Matching and 3D reconstruction

- Establish correspondence between two (or more) images



[Schaffalitzky and Zisserman ECCV 2002]

Building Rome in a Day

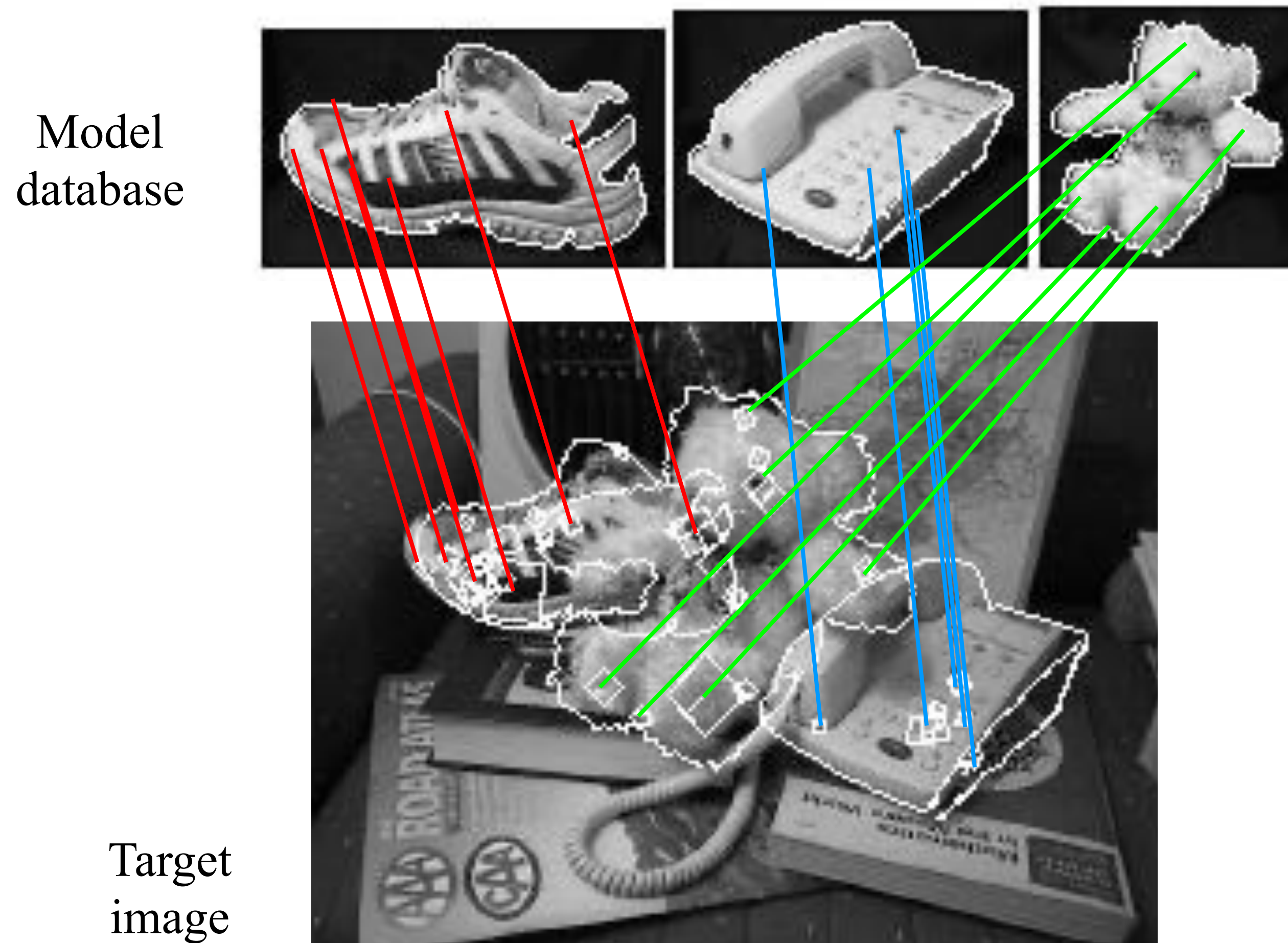
57,845 downloaded images, 11,868 registered images



[Agarwal, Snavely, Simon, Seitz, Szeliski, ICCV'09]

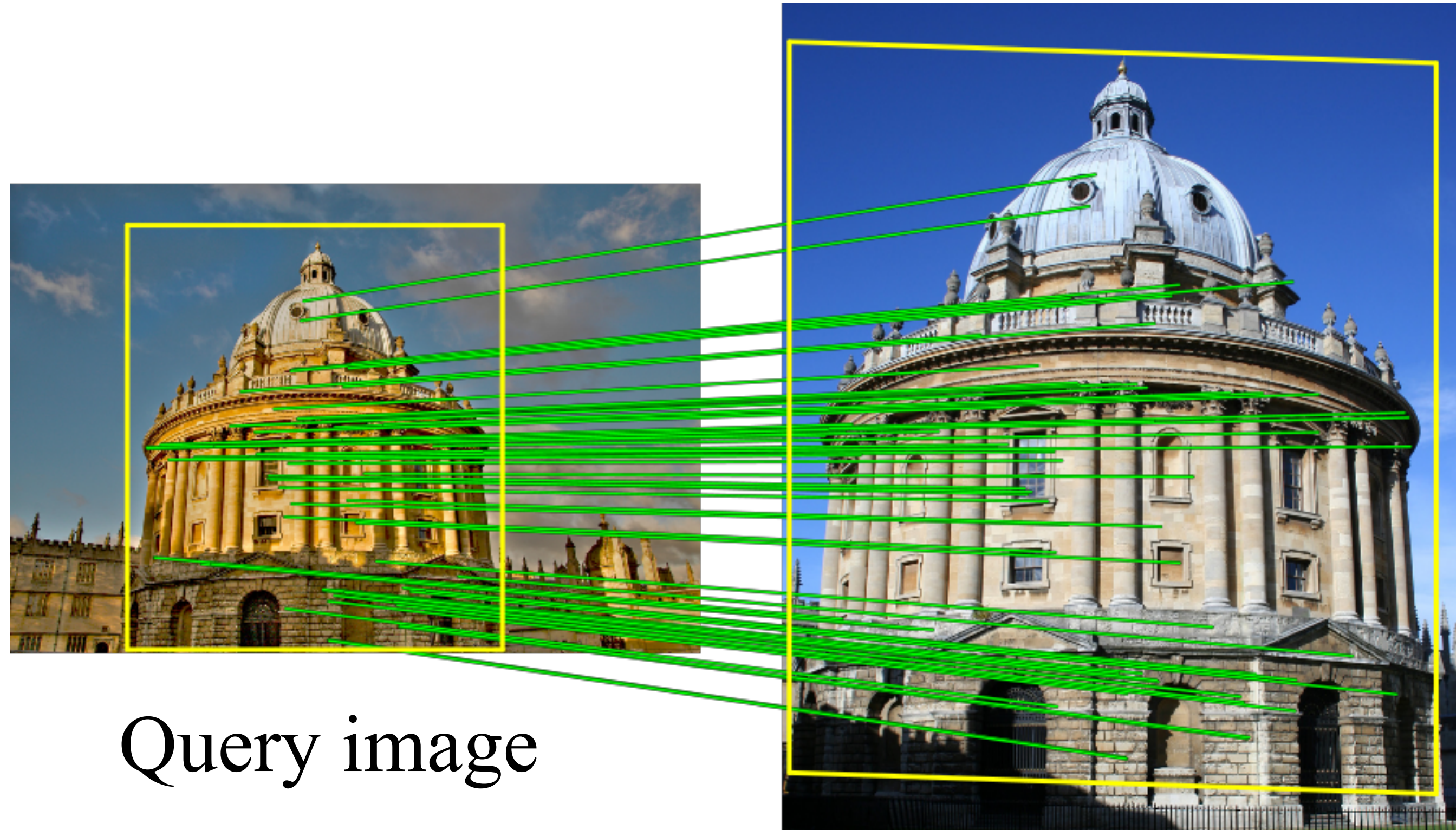
Object recognition

- Establish correspondence between the target image and (multiple) images in the model database



Visual search

- Establish correspondence between the query image and all images from the database depicting the same object or scene

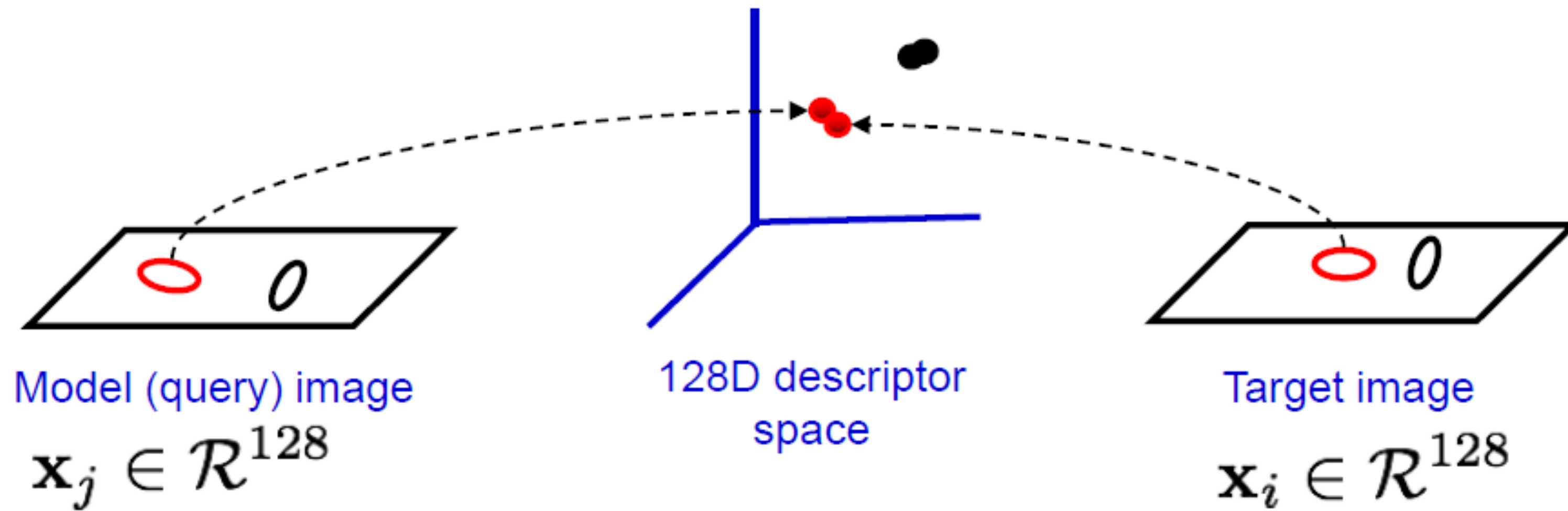


Query image

Database image(s)

Matching of descriptors

- Find the nearest neighbor in the second image for each descriptor, for example SIFT



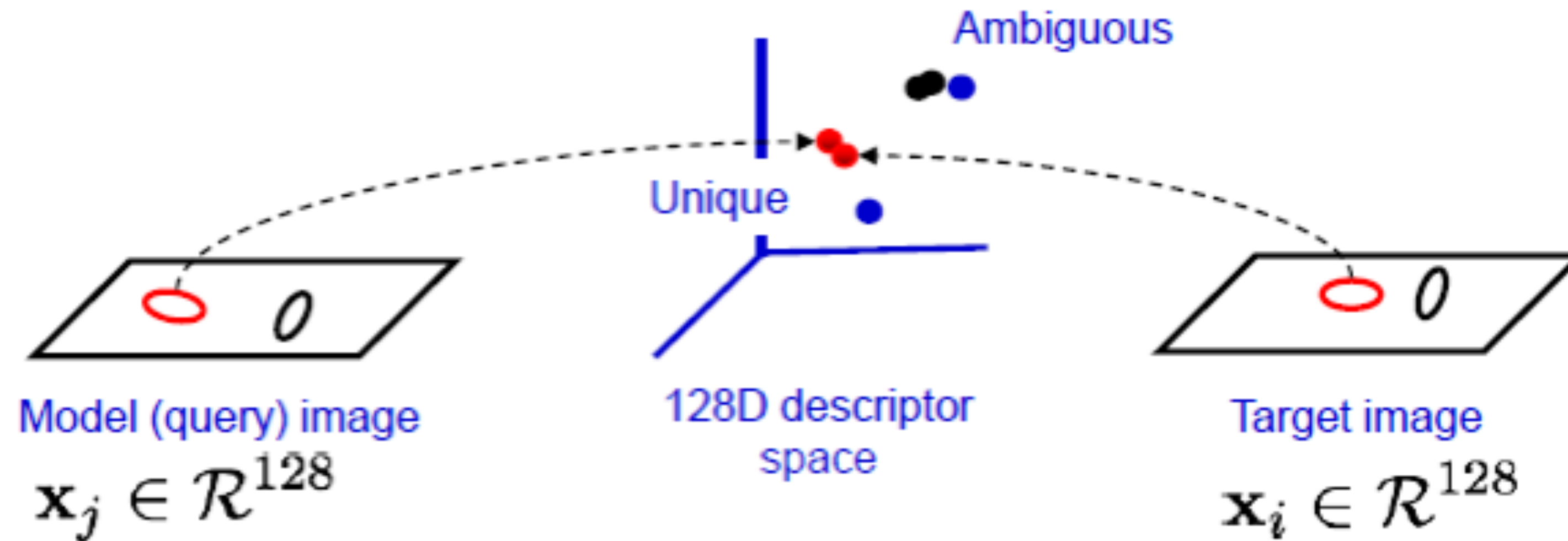
Need to solve some variant of the “nearest neighbor problem” for all feature vectors, $\mathbf{x}_j \in \mathcal{R}^{128}$, in the query image:

$$\forall j \text{ NN}(j) = \arg \min_i \|\mathbf{x}_i - \mathbf{x}_j\|,$$

where, $\mathbf{x}_i \in \mathcal{R}^{128}$, are features in the target image.

Matching of descriptors

- Pruning strategies
 - Ratio with respect to the second best match ($d_1/d_2 \ll 1$) [Lowe, '04]



If the 2nd nearest neighbour is much further than the 1st nearest neighbour, the match is more “unique” or discriminative.

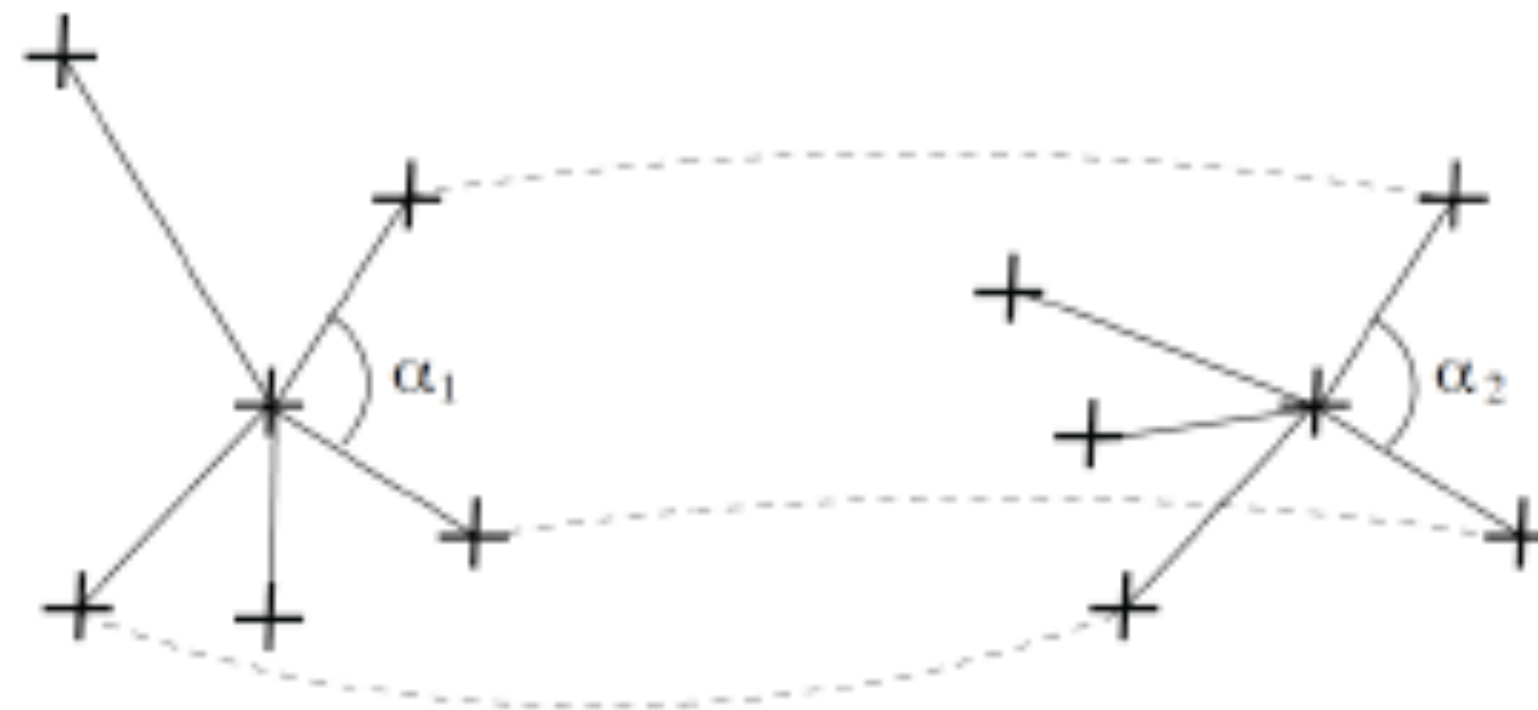
Measure this by the ratio: $r = d_{1NN} / d_{2NN}$

r is between 0 and 1

r is small the match is more unique.

Matching of descriptors

- Pruning strategies
 - Ratio with respect to the second best match ($d_1/d_2 \ll 1$)
 - Local neighborhood constraints (semi-local constraints)



Neighbors of the point have to match and angles have to correspond.
Note that in practice not all neighbors have to be matched correctly.

Matching of descriptors

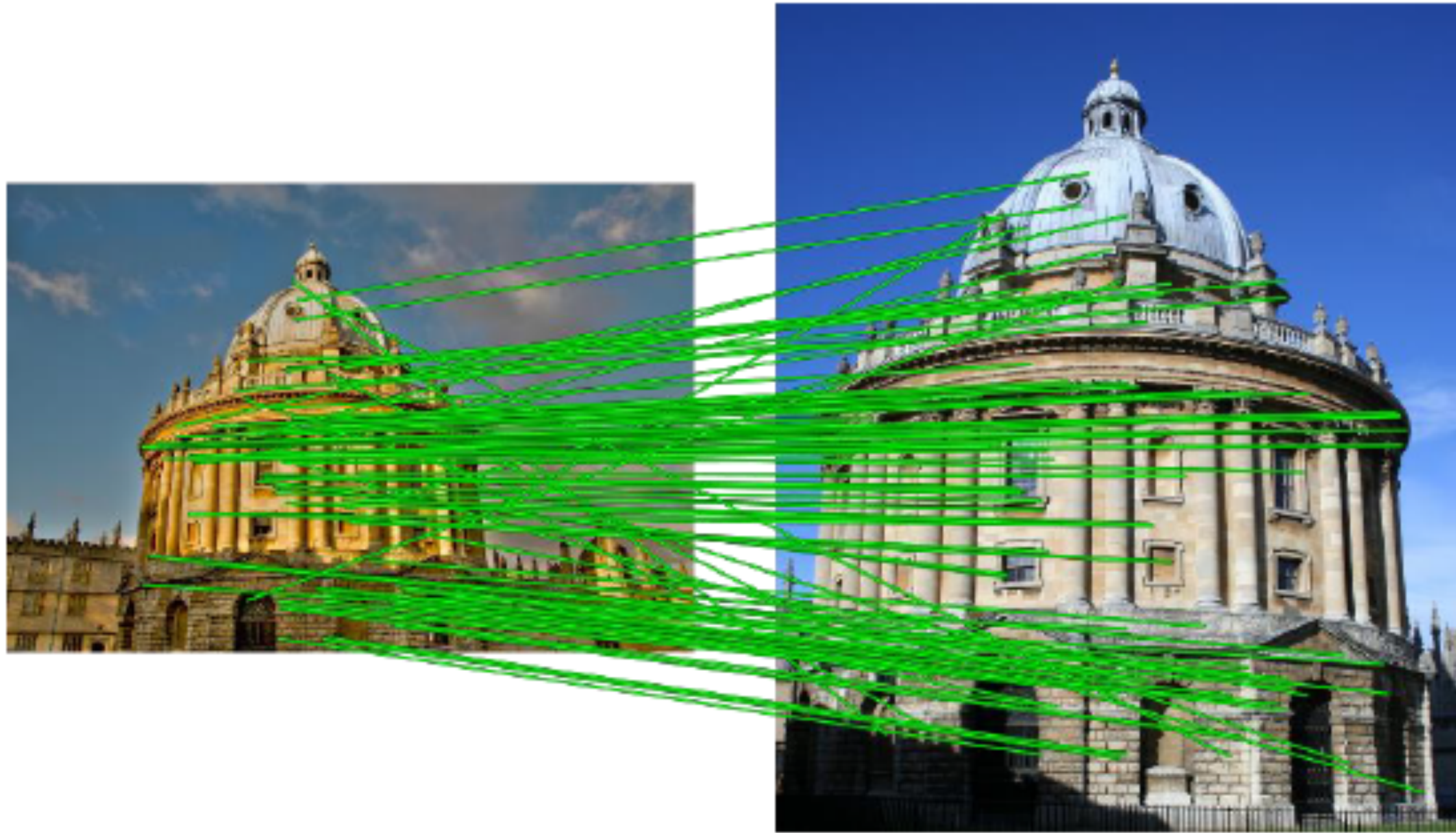
- Pruning strategies
 - Ratio with respect to the second best match ($d_1/d_2 \ll 1$)
 - Local neighborhood constraints (semi-local constraints)
 - Backwards matching (matches are NN in both directions)

Matching of descriptors

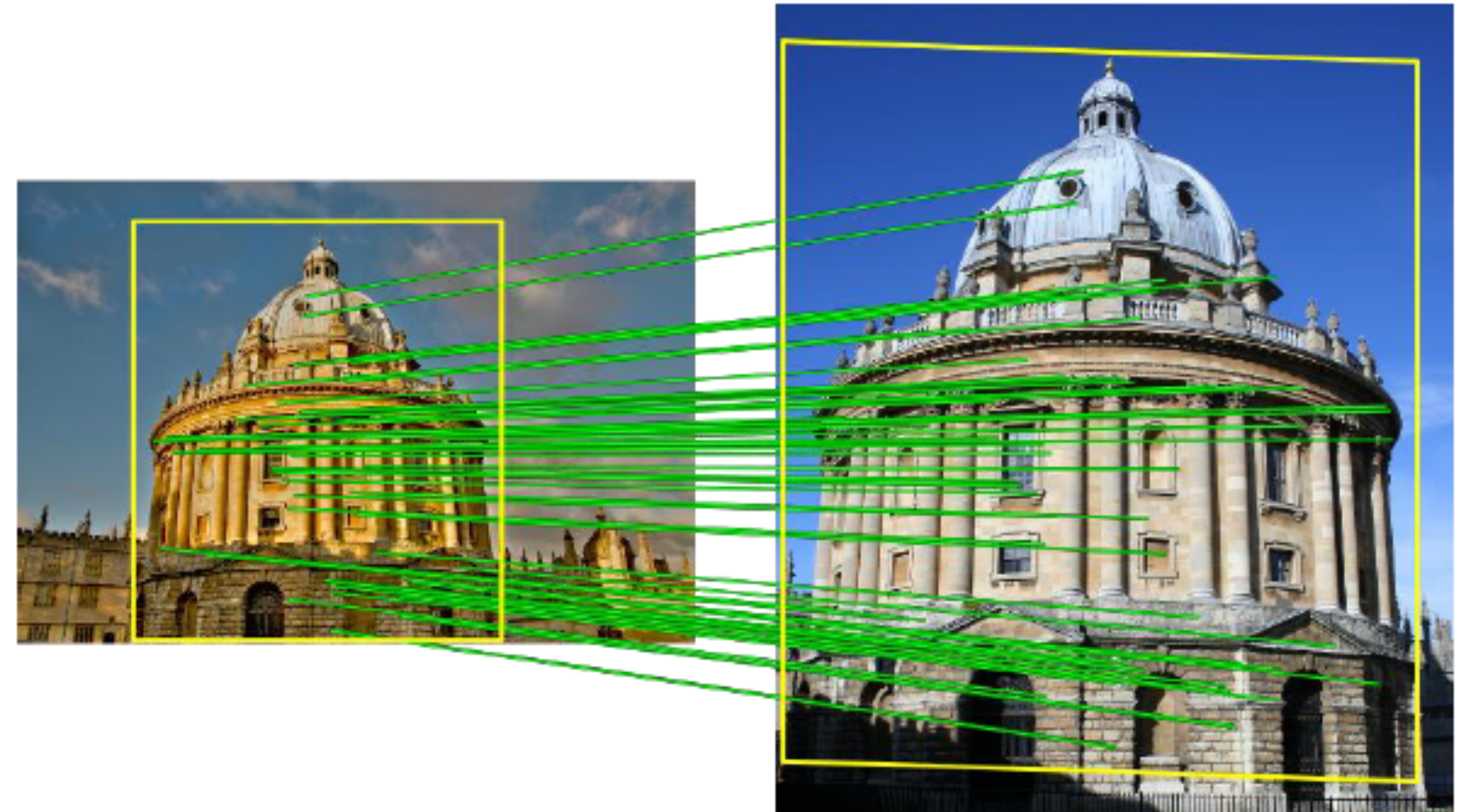
- Pruning strategies
 - Ratio with respect to the second best match ($d_1/d_2 \ll 1$)
 - Local neighborhood constraints (semi-local constraints)
 - Backwards matching (matches are NN in both directions)
- Geometric verification with global constraint
 - All matches must be consistent with a global geometric transformation
 - However, there are many incorrect matches
 - **Need to estimate simultaneously the geometric transformation and the set of consistent matches**

Geometric verification with global constraint

- Example of a geometric verification



Tentative matches



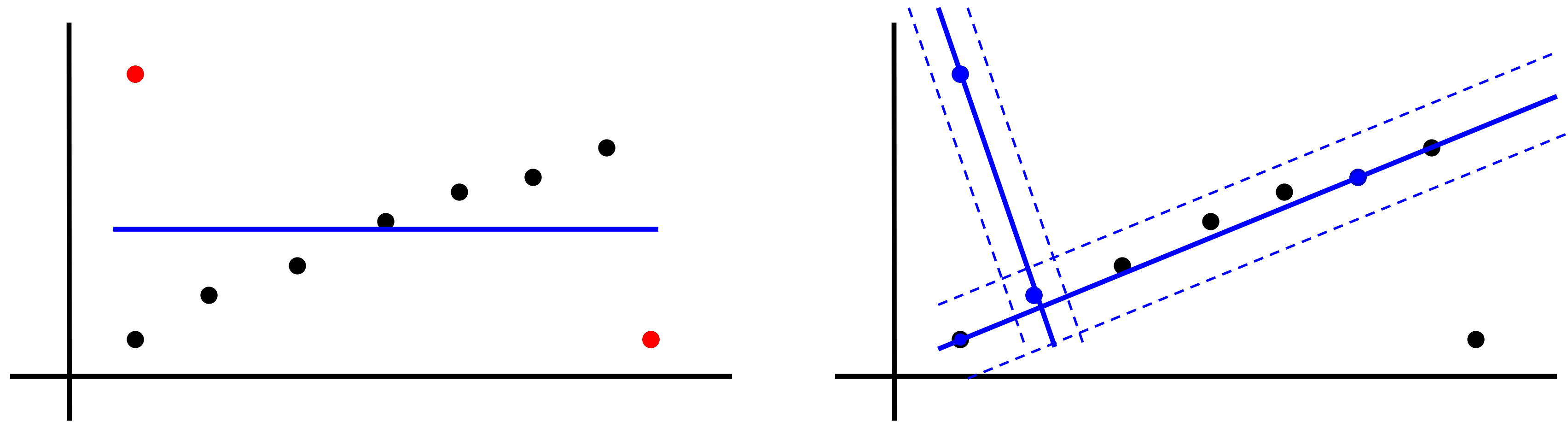
Matches consistent with an affine transformation

Matching of descriptors

- Geometric verification with global constraint
 - All matches must be consistent with a global geometric transformation
 - However, there are many incorrect matches
 - Need to estimate simultaneously the geometric transformation and the set of consistent matches
- Robust estimation of global constraints
 - RANSAC (RANdom Sampling Consensus) [Fishler&Bolles'81]
 - Hough transform [Lowe'04]

RANSAC: Example of robust line estimation

Fit a line to 2D data containing outliers



There are two problems

1. a line **fit** which minimizes perpendicular distance
2. a **classification** into inliers (valid points) and outliers

Solution: use robust statistical estimation algorithm RANSAC
(RANdom Sample Consensus) [Fishler & Bolles, 1981]

RANSAC robust line estimation

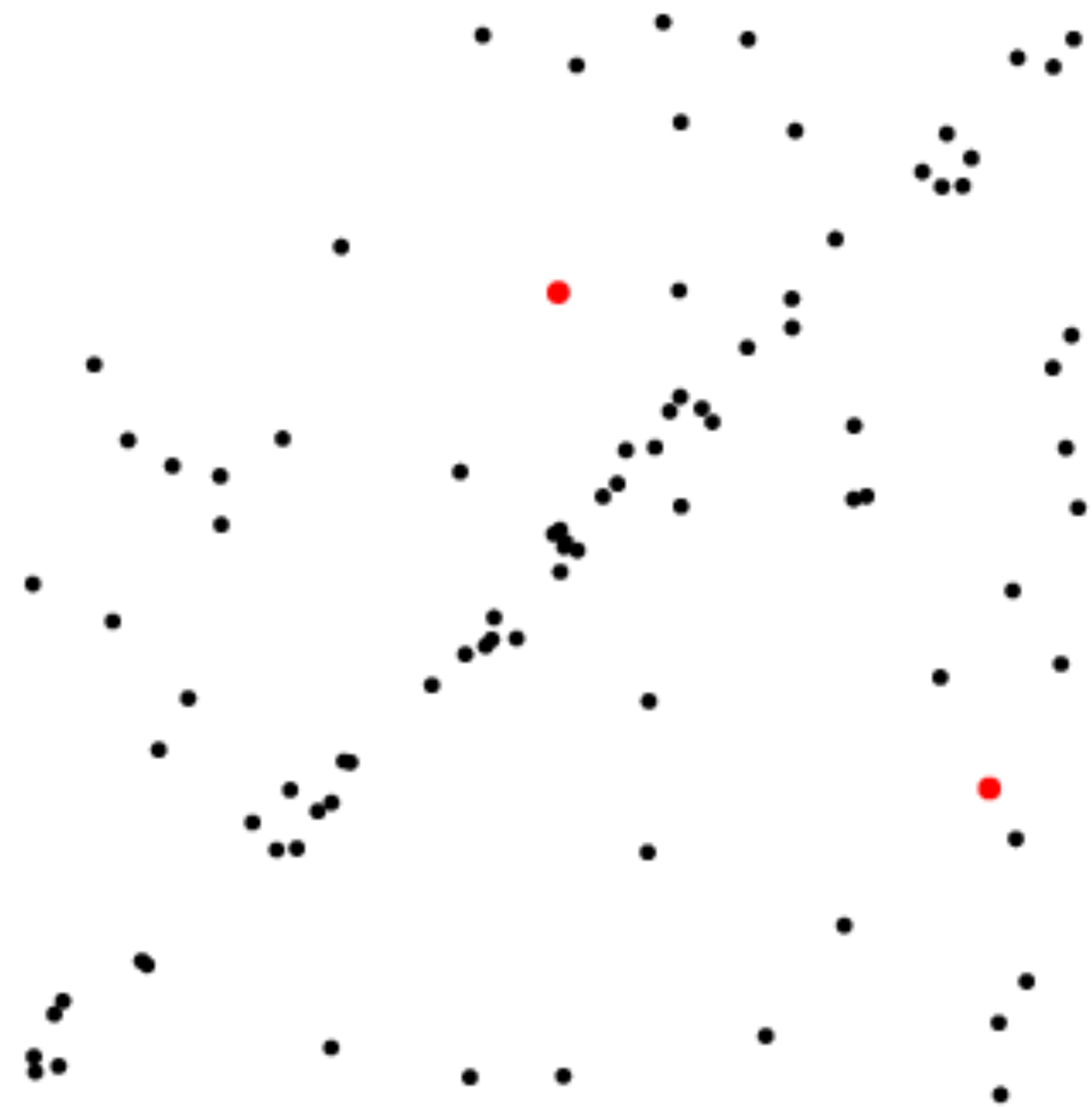
Repeat

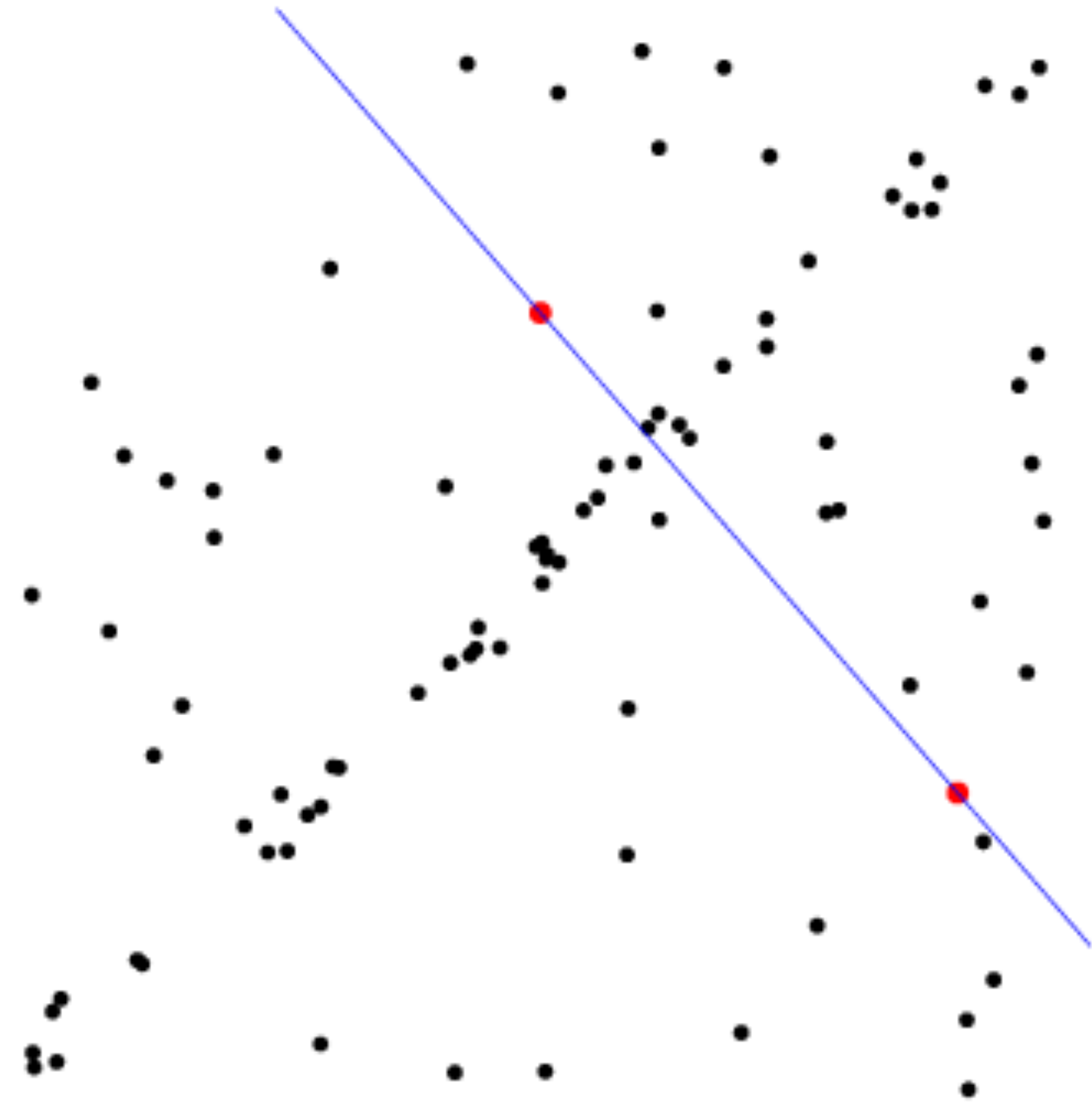
1. Select random sample of 2 points
2. Compute the line through these points
3. Measure support (number of points within threshold distance of the line)

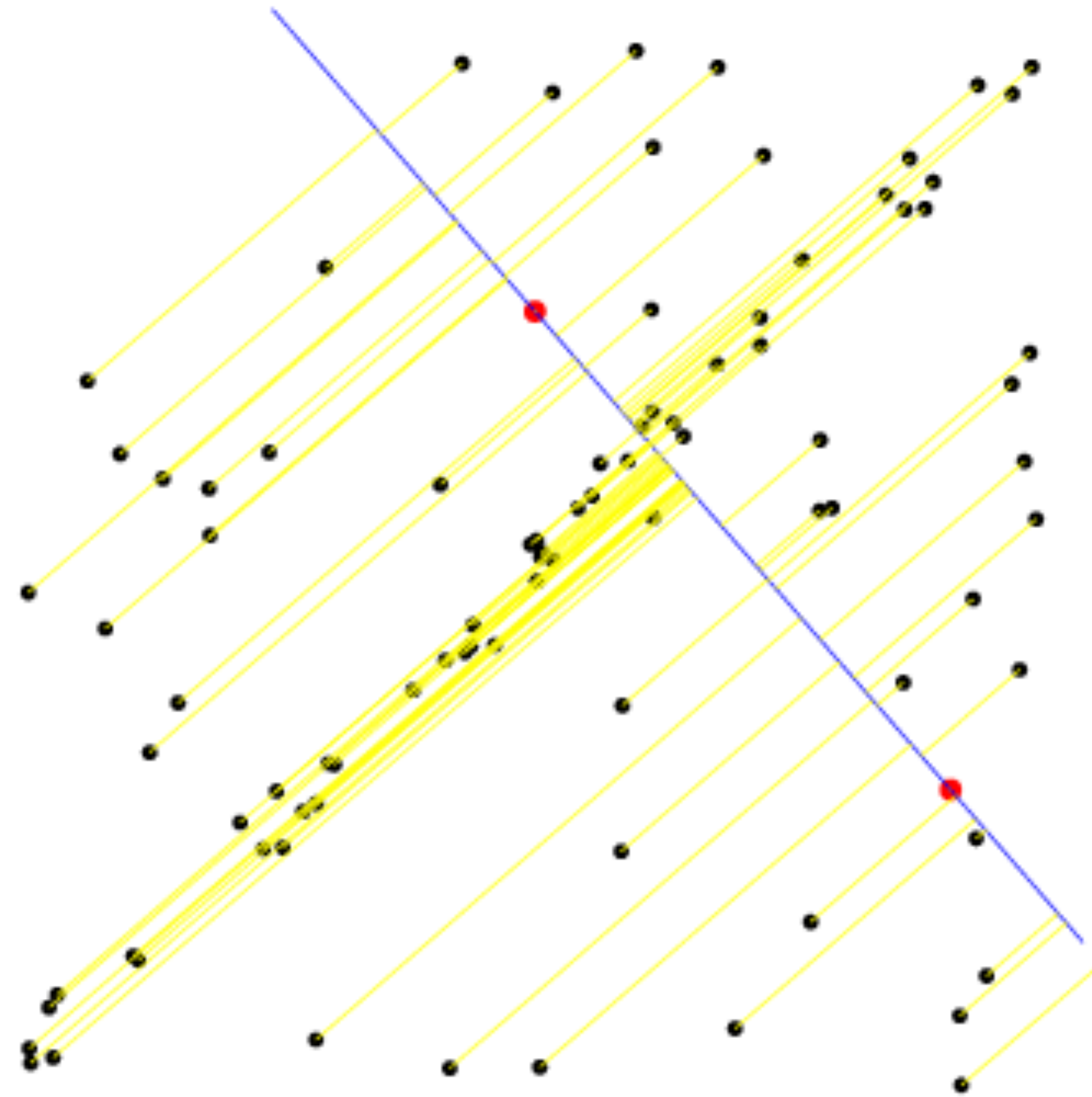
Choose the line with the largest number of inliers

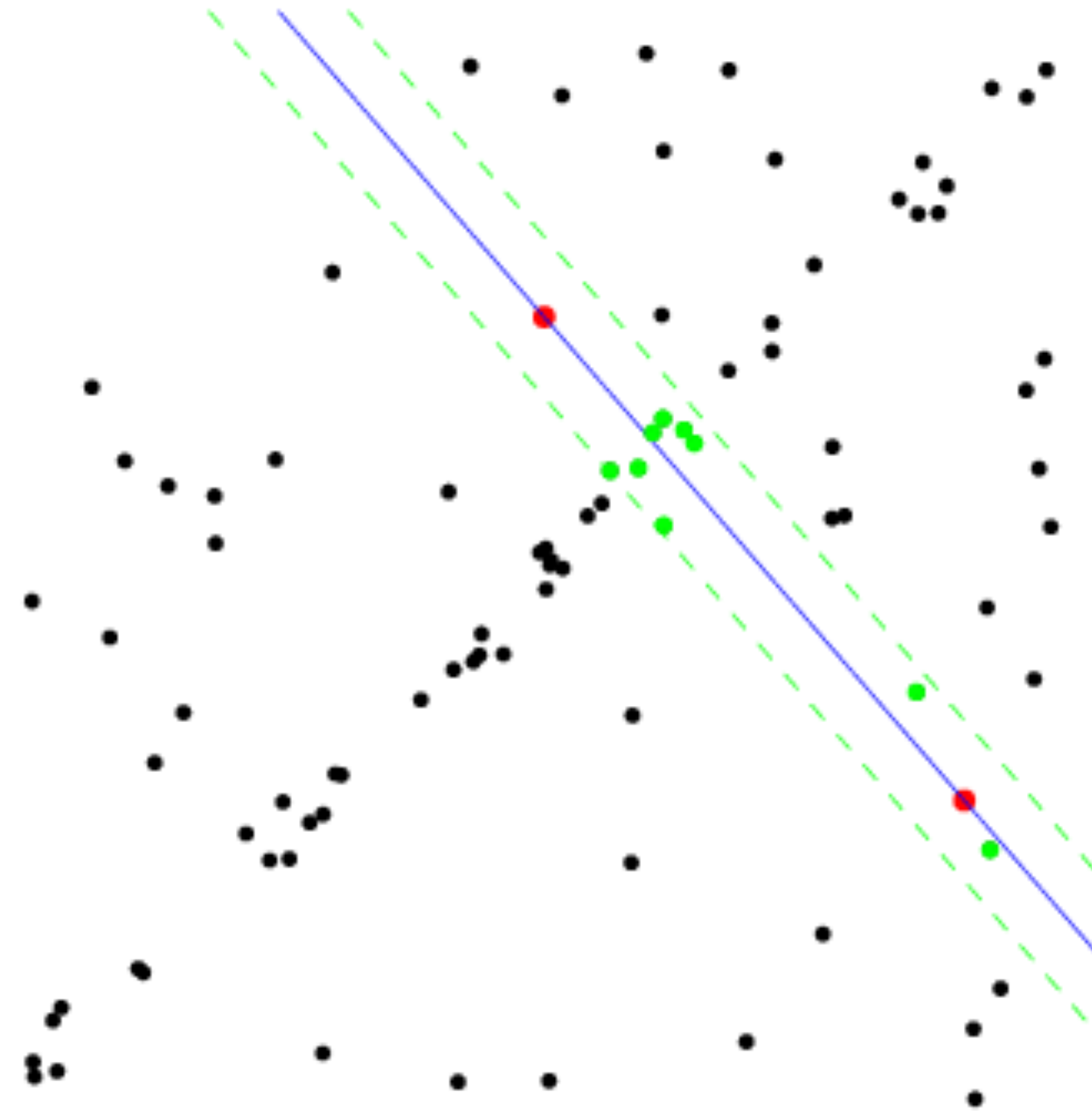
- Compute least squares fit of line to inliers (regression)

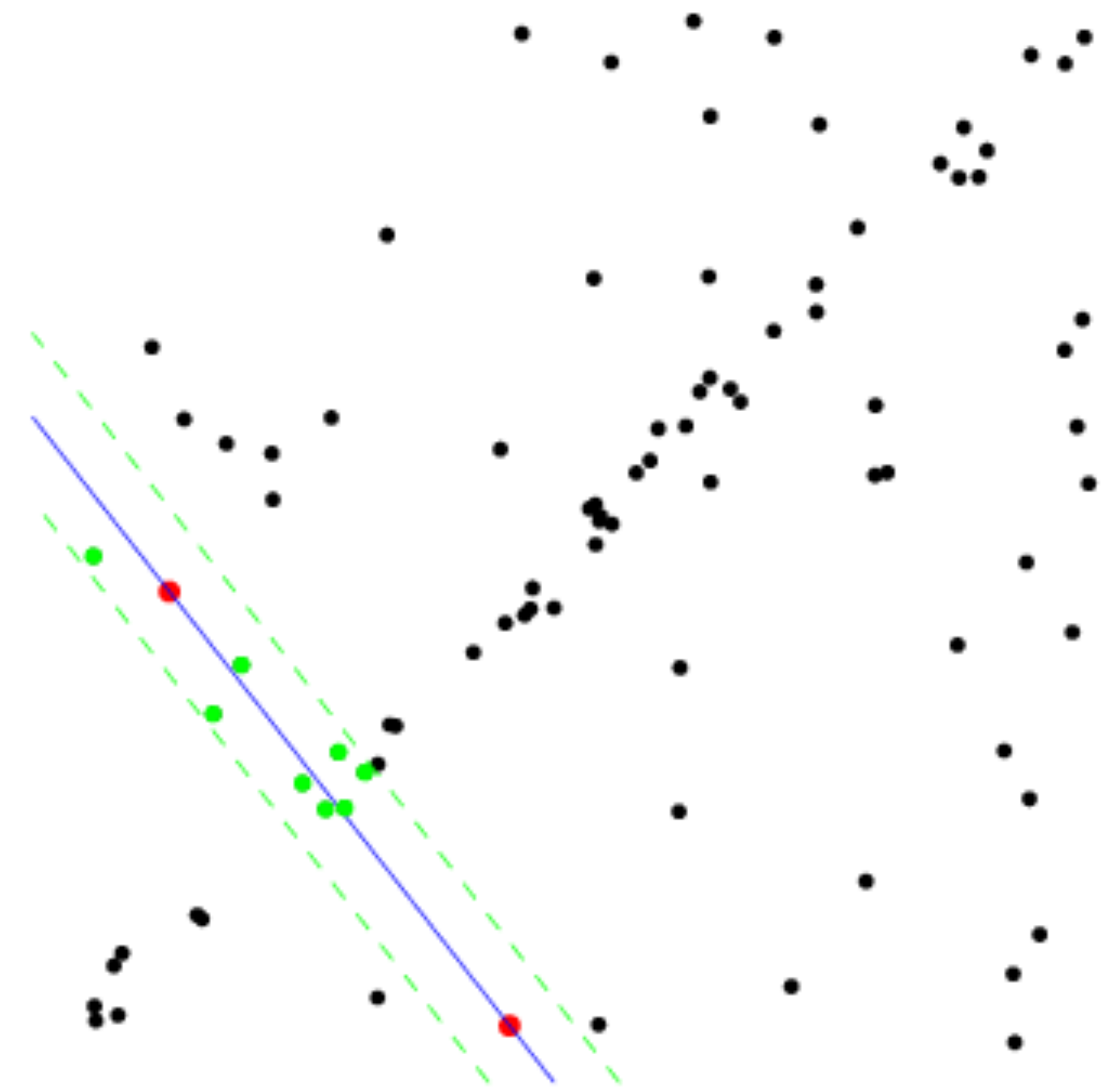


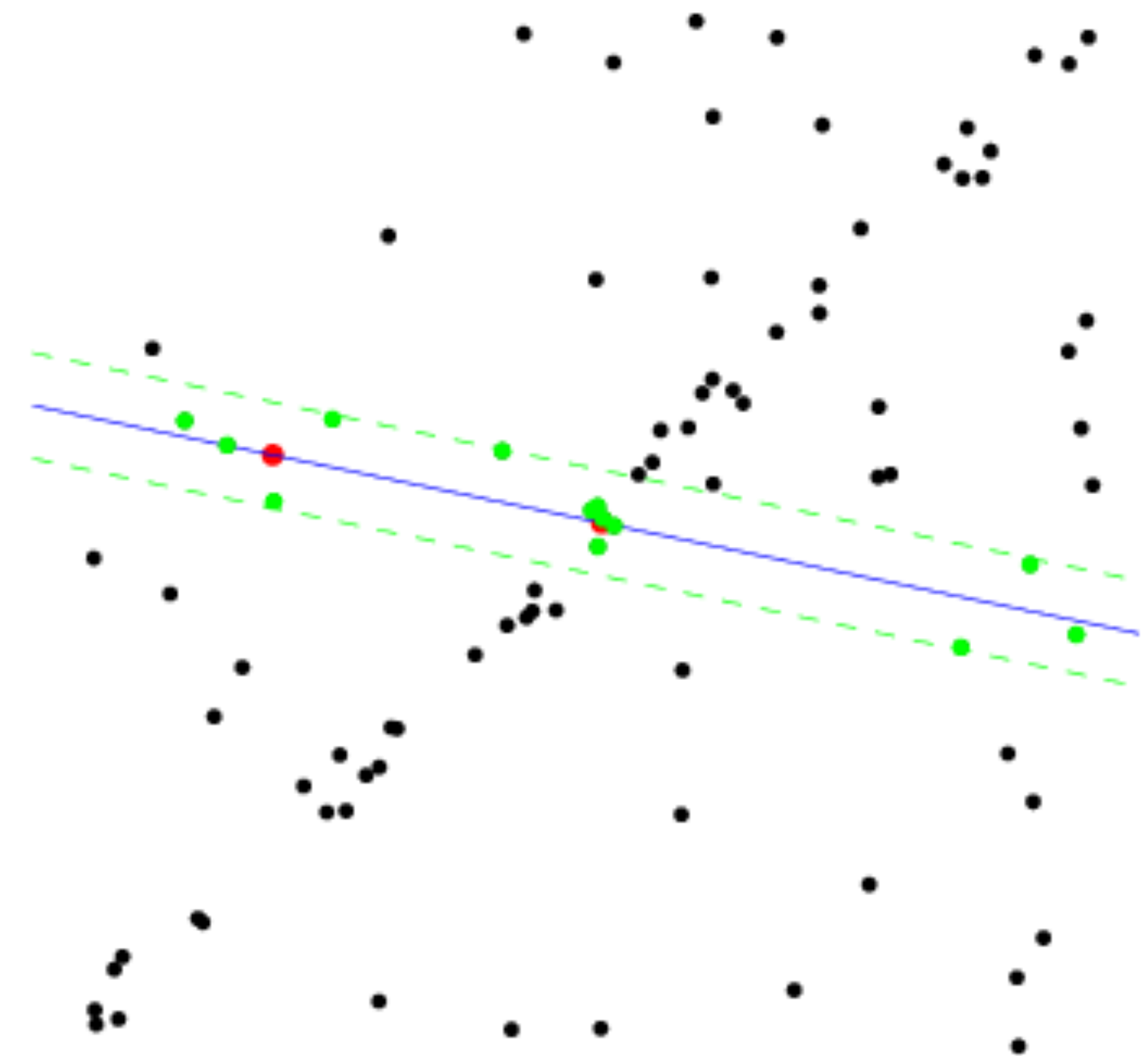


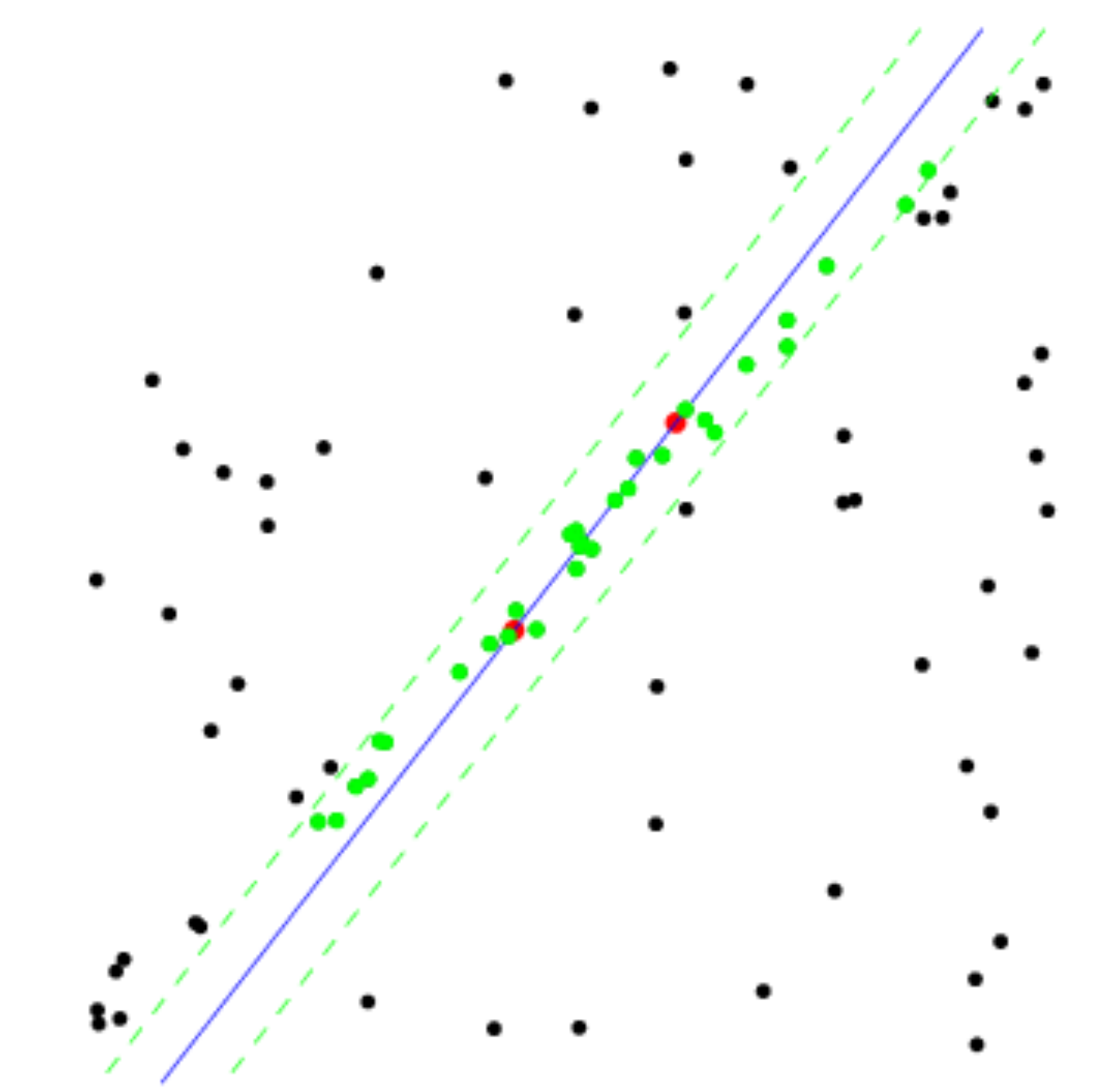


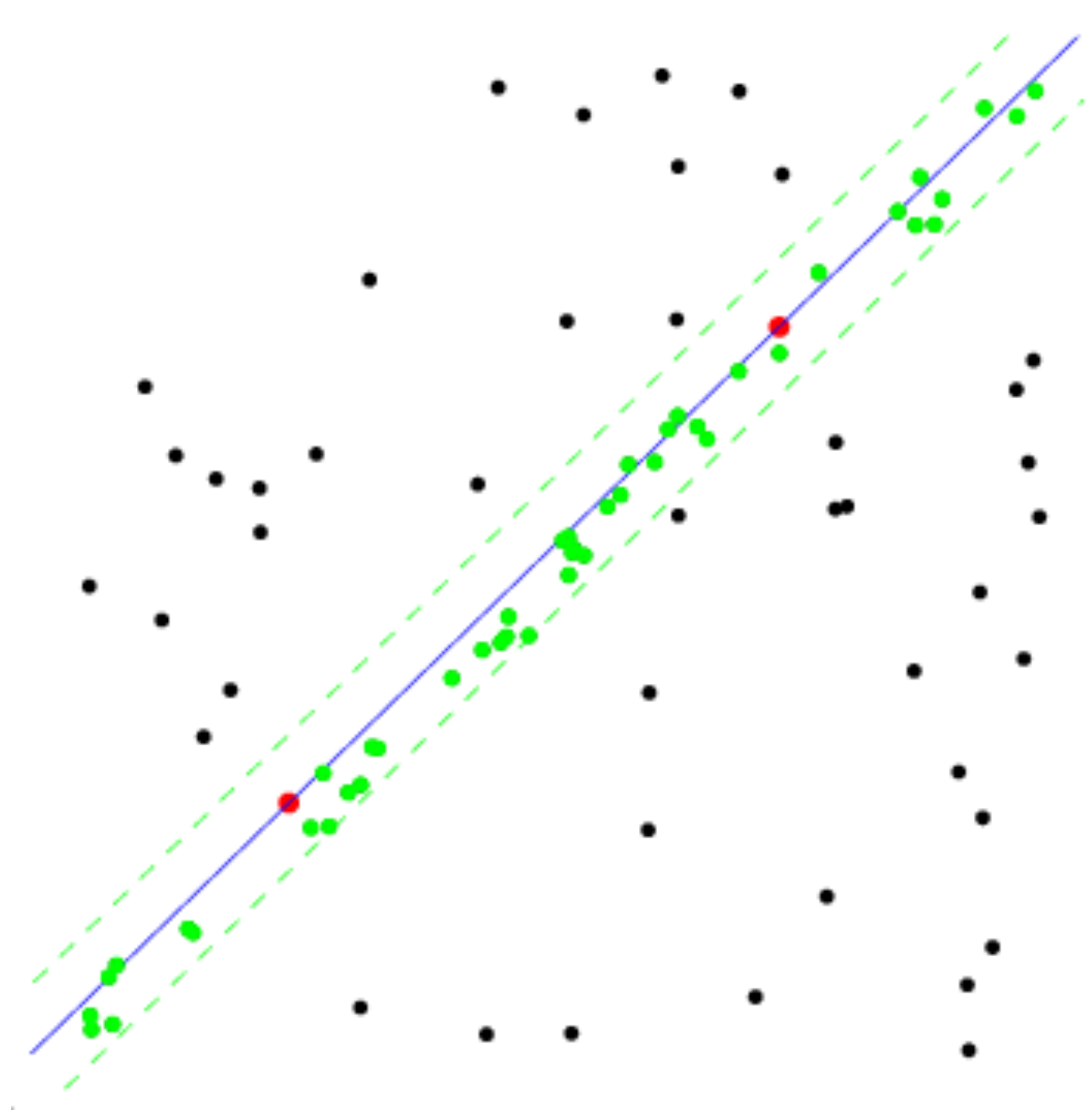








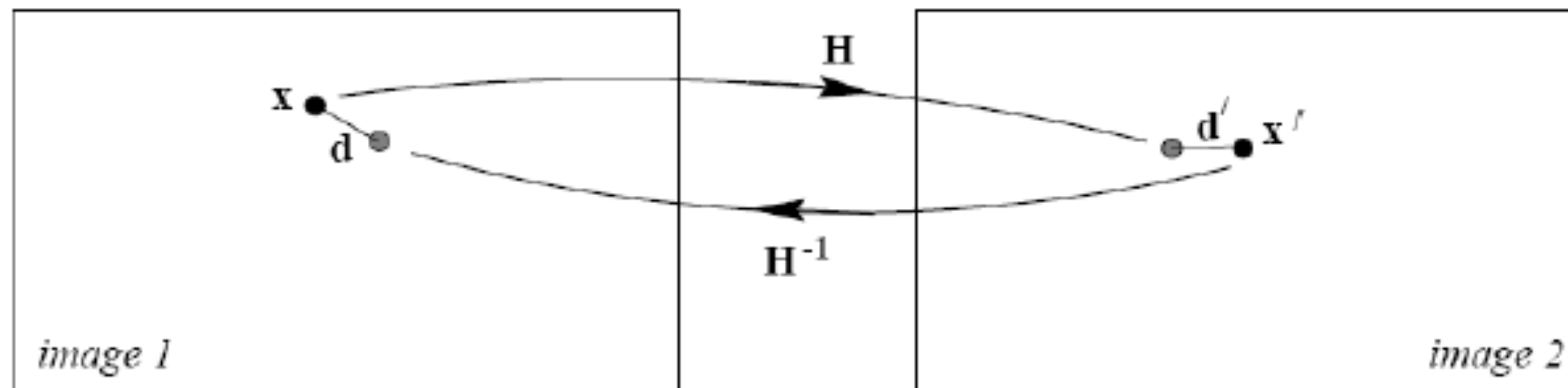




RANSAC Algorithm

- Robust estimation of a homography with RANSAC
 - Repeat
 - Select 4 point matches
 - Compute 3x3 homography
 - Measure support (number of inliers within threshold, i.e. $d_{\text{transfer}}^2 < t$)

$$d_{\text{transfer}}^2 = d(\mathbf{x}, \mathbf{H}^{-1}\mathbf{x}')^2 + d(\mathbf{x}', \mathbf{H}\mathbf{x})^2$$



- Choose (H with the largest number of inliers)
- Re-estimate H with all inliers

Matching of descriptors

- Geometric verification with global constraint
 - All matches must be consistent with a global geometric transformation
 - However, there are many incorrect matches
 - Need to estimate simultaneously the geometric transformation and the set of consistent matches
- Robust estimation of global constraint
 - RANSAC (RANdom Sampling Consensus) [Fishler&Bolles'81]
 - **Hough transform [Lowe'04]**

Strategy 2: Hough transform

- General outline:
 - Discretize parameter space into bins
 - For each feature point in the image, put a **vote** in every bin in the parameter space that could have generated this point
 - Find bins that have the most votes

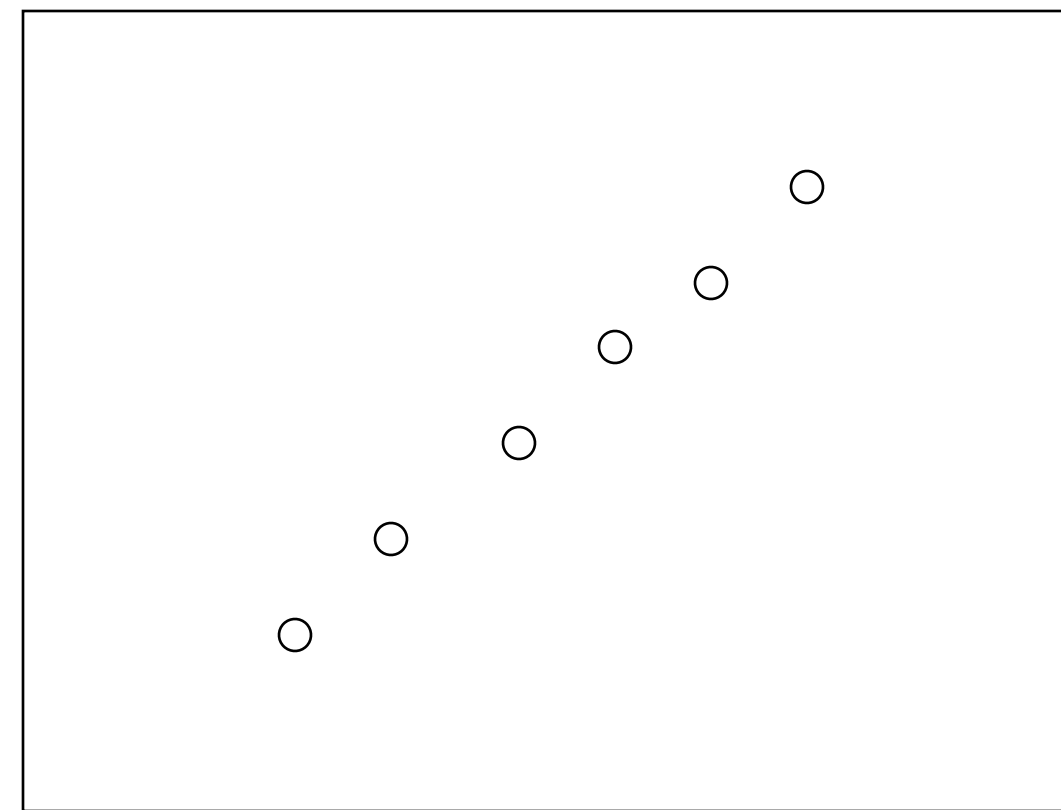
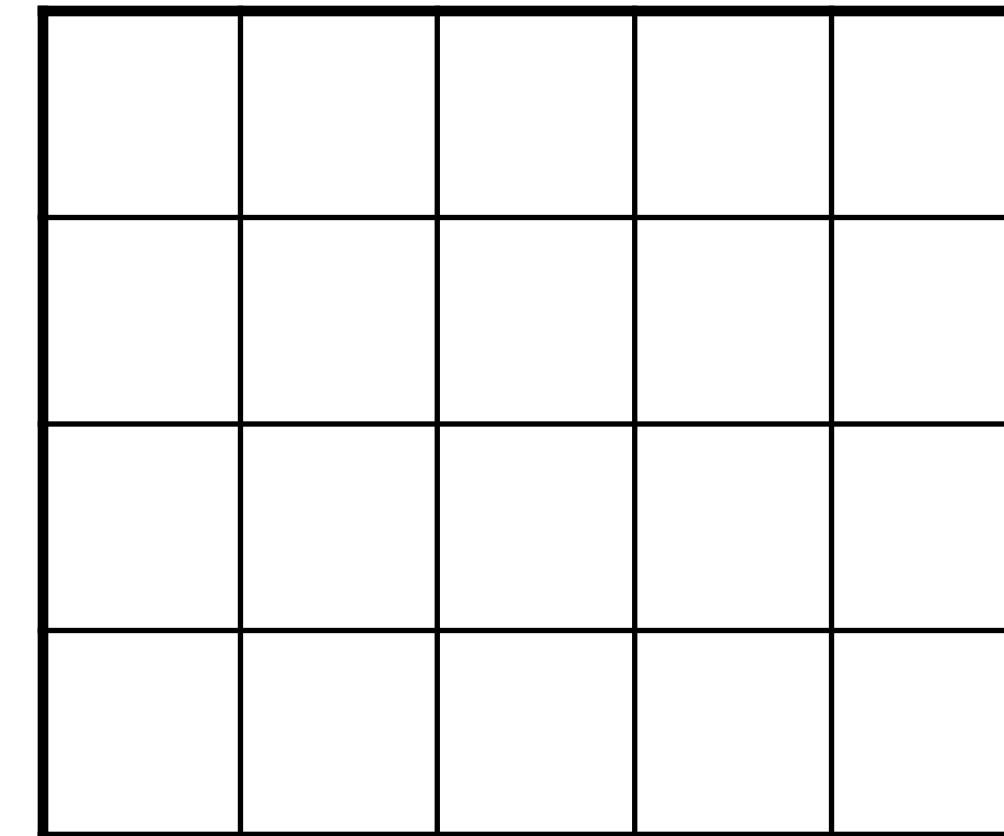
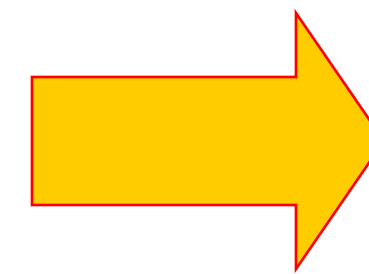


Image space

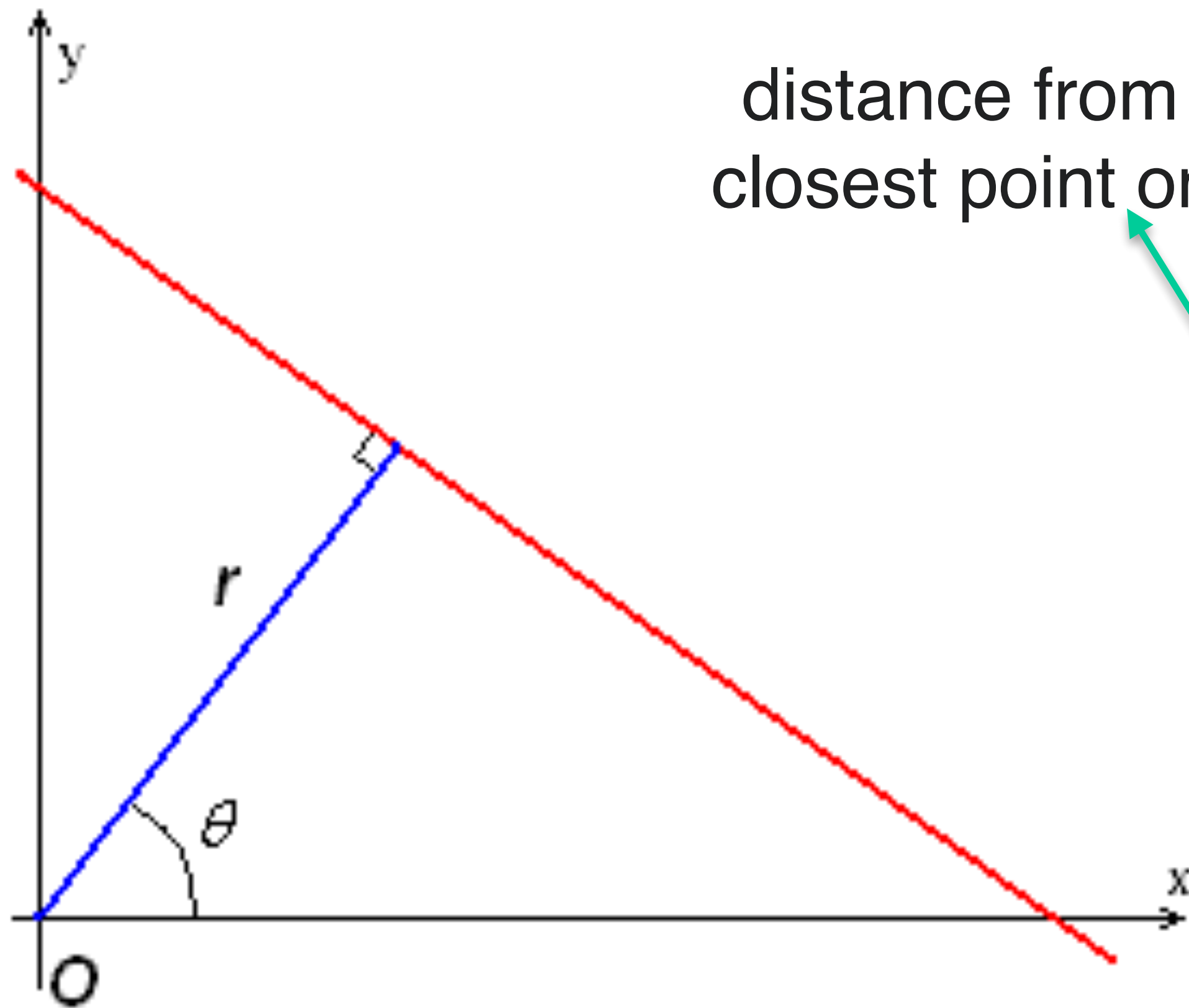


Hough parameter space

P.V.C. Hough, *Machine Analysis of Bubble Chamber Pictures*, Proc. Int. Conf. High Energy Accelerators and Instrumentation, 1959

Hough transform for lines

A straight line $y = mx + b$ can be represented as a point (r, θ) in the parameter space.



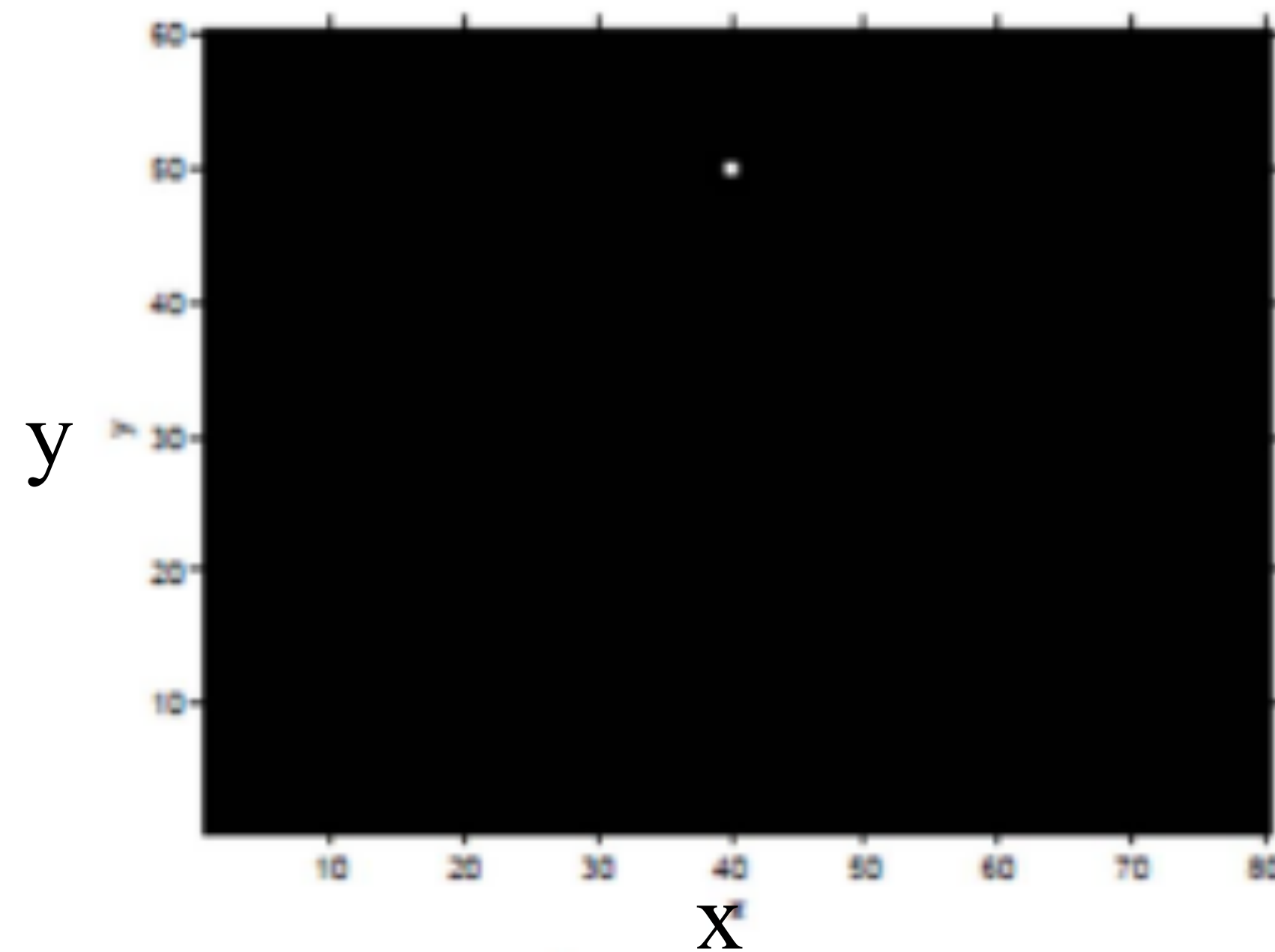
distance from the origin to the
closest point on the straight line

$$r = x \cos \theta + y \sin \theta,$$

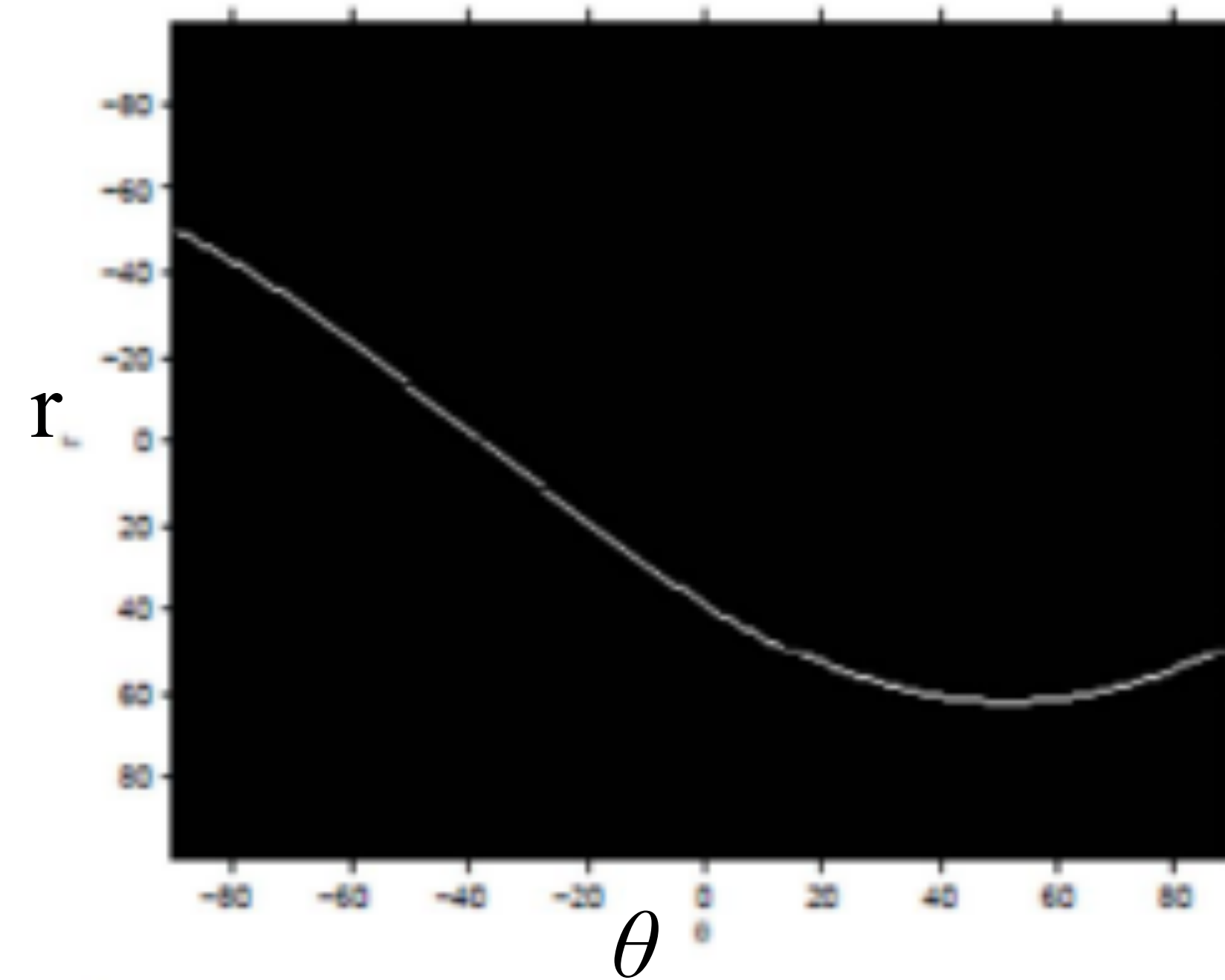
angle between the x-axis and the line
connecting the origin with that closest point

Hough transform for lines

Hough space



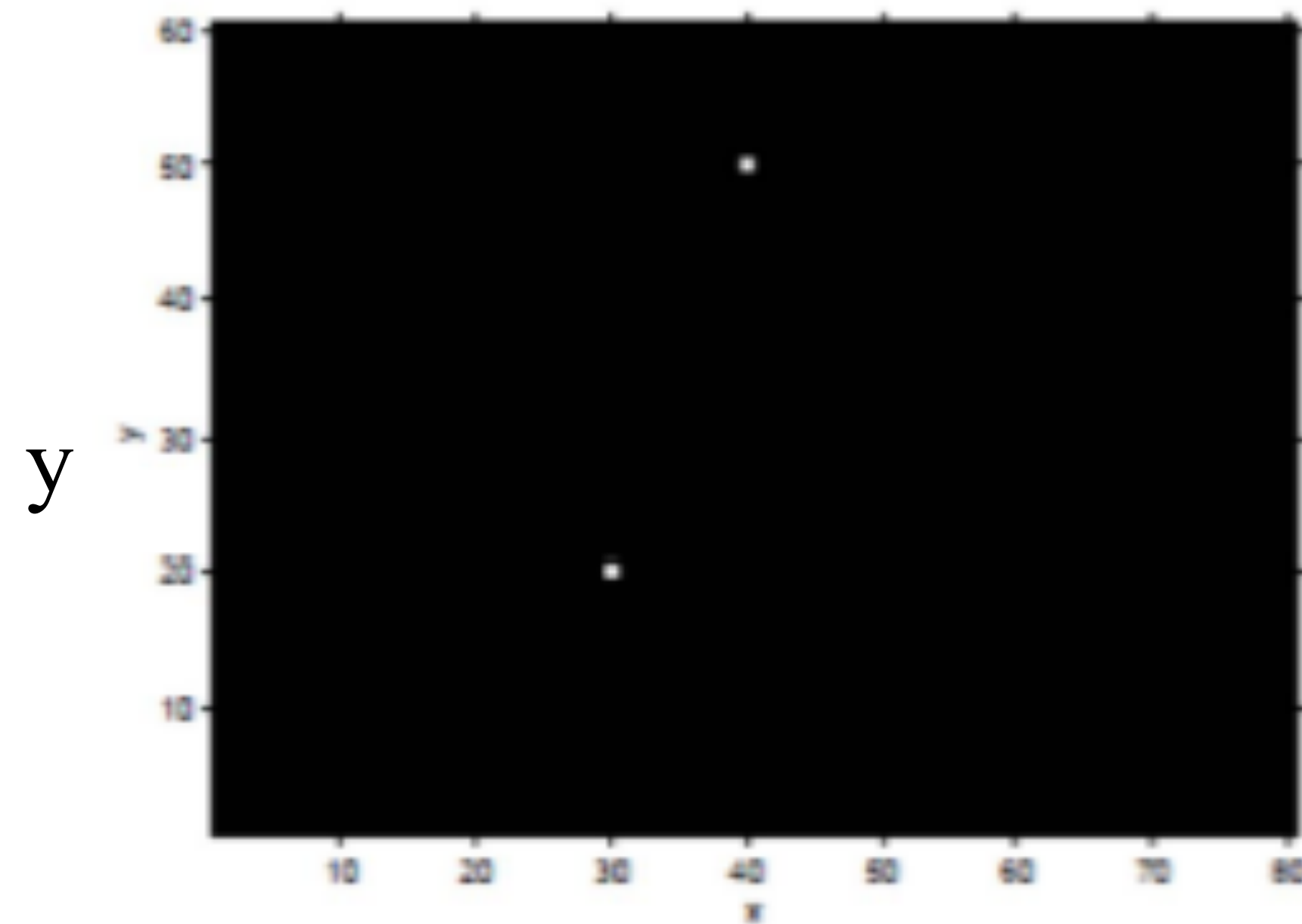
(a) Point p_0 .



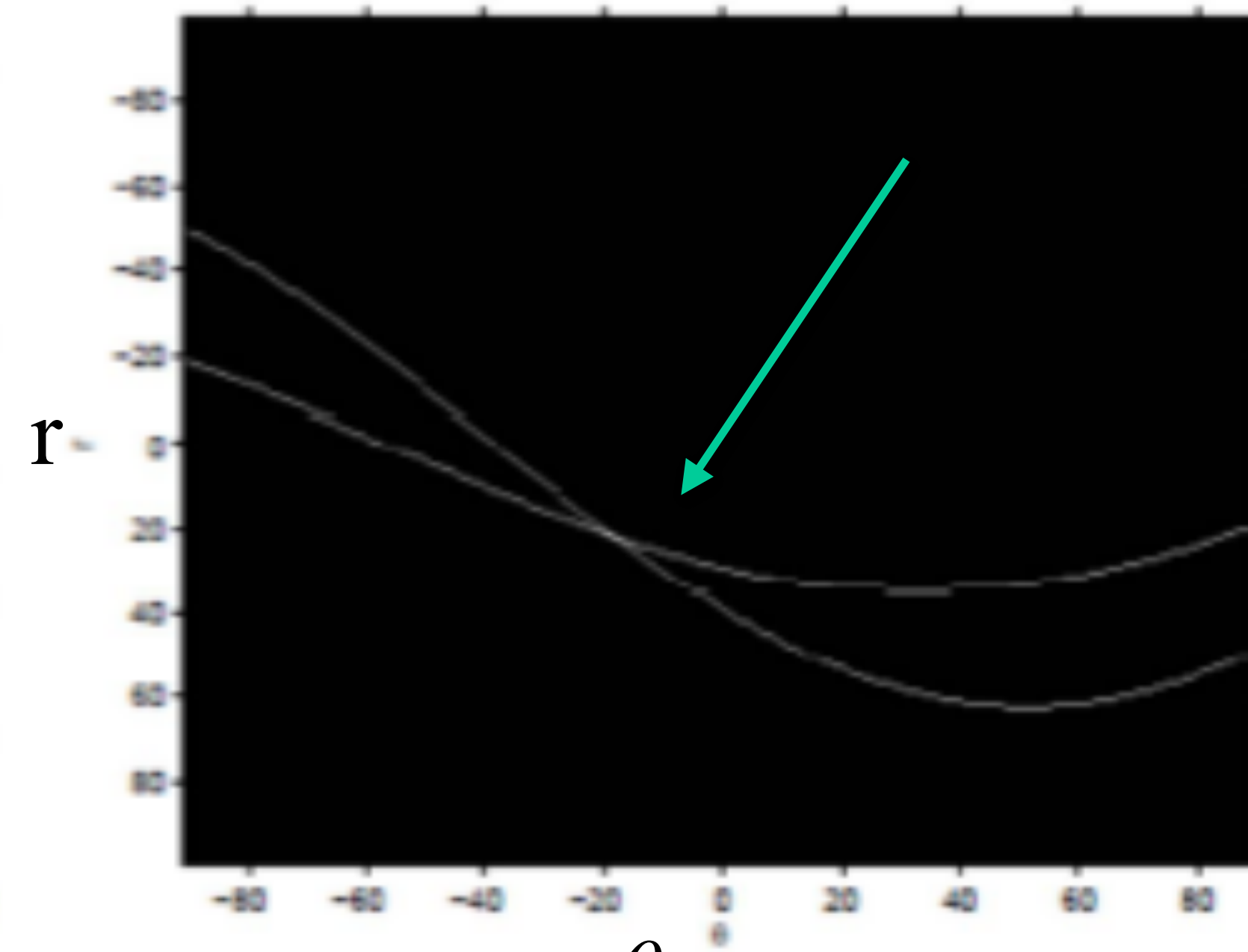
(b) All possible lines through p_0 represented in the Hough space.

Given a single point in the plane, the set of all straight lines going through that point corresponds to a sinusoidal curve in the (r, θ) plane, which is unique to that point.

Hough transform for lines



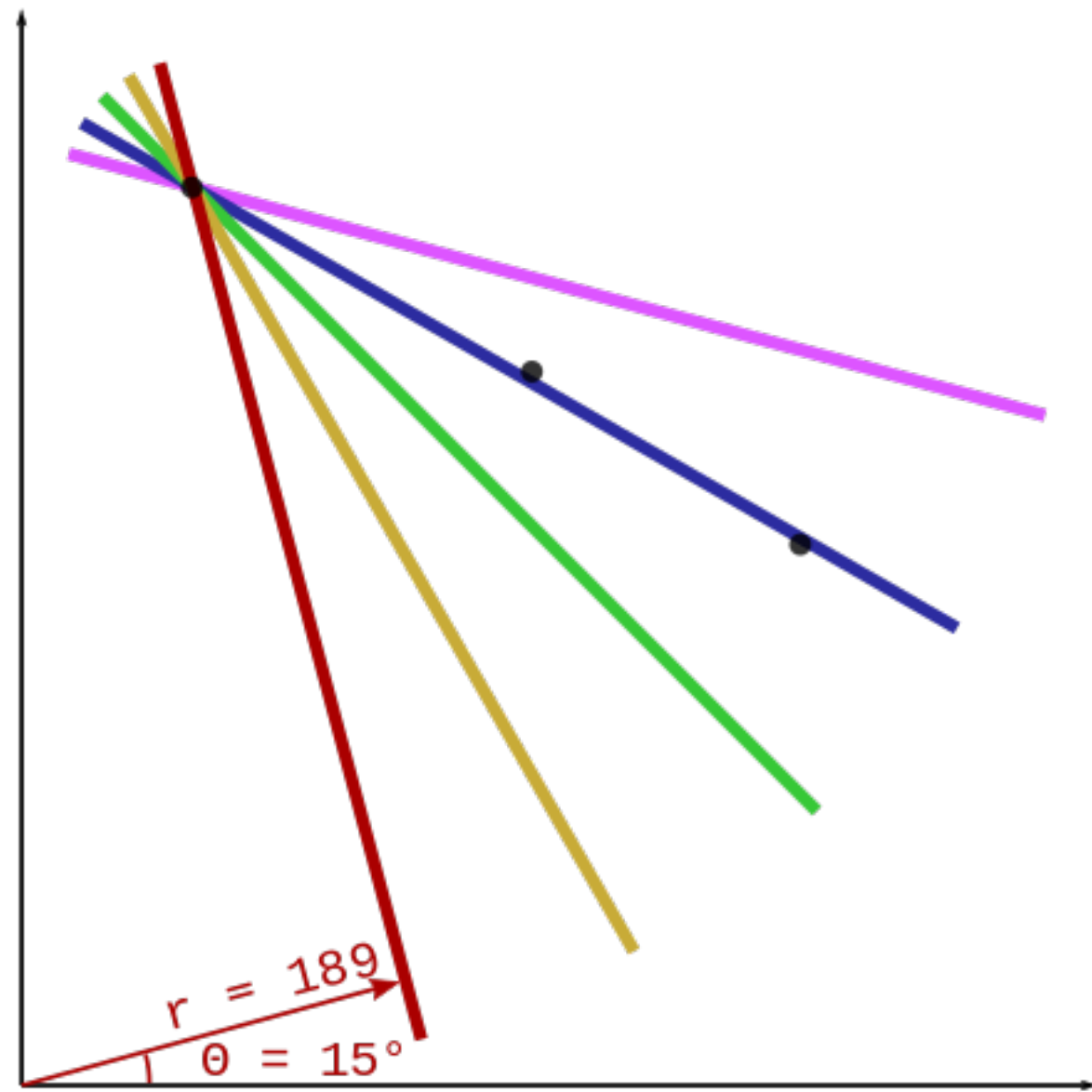
(a) Points p_0 and p_1 .



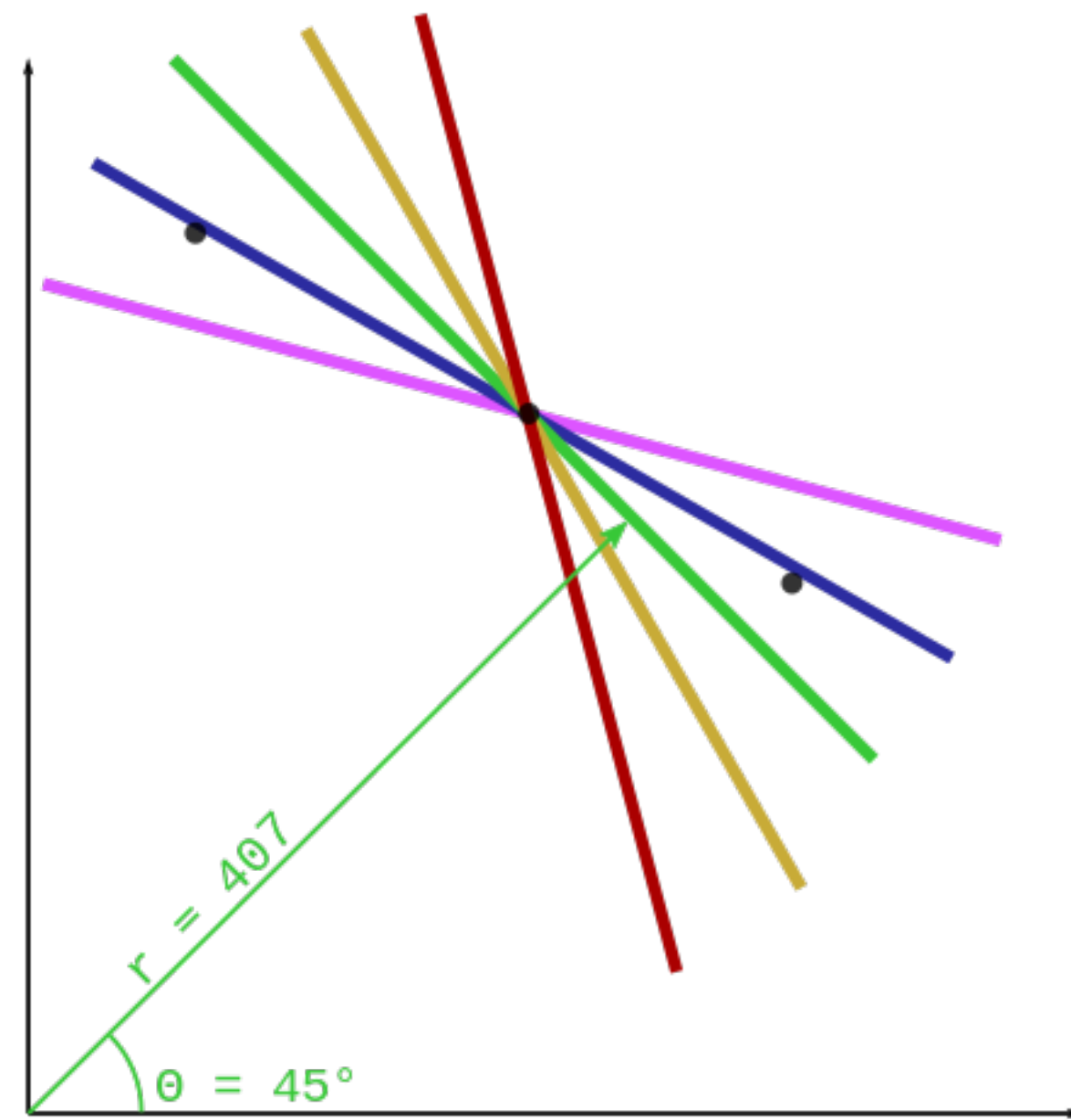
(b) All possible lines through p_0 and/or p_1 represented in the Hough space.

A set of two or more points that form a straight line will produce sinusoids crossing at the (r, θ) for that line.

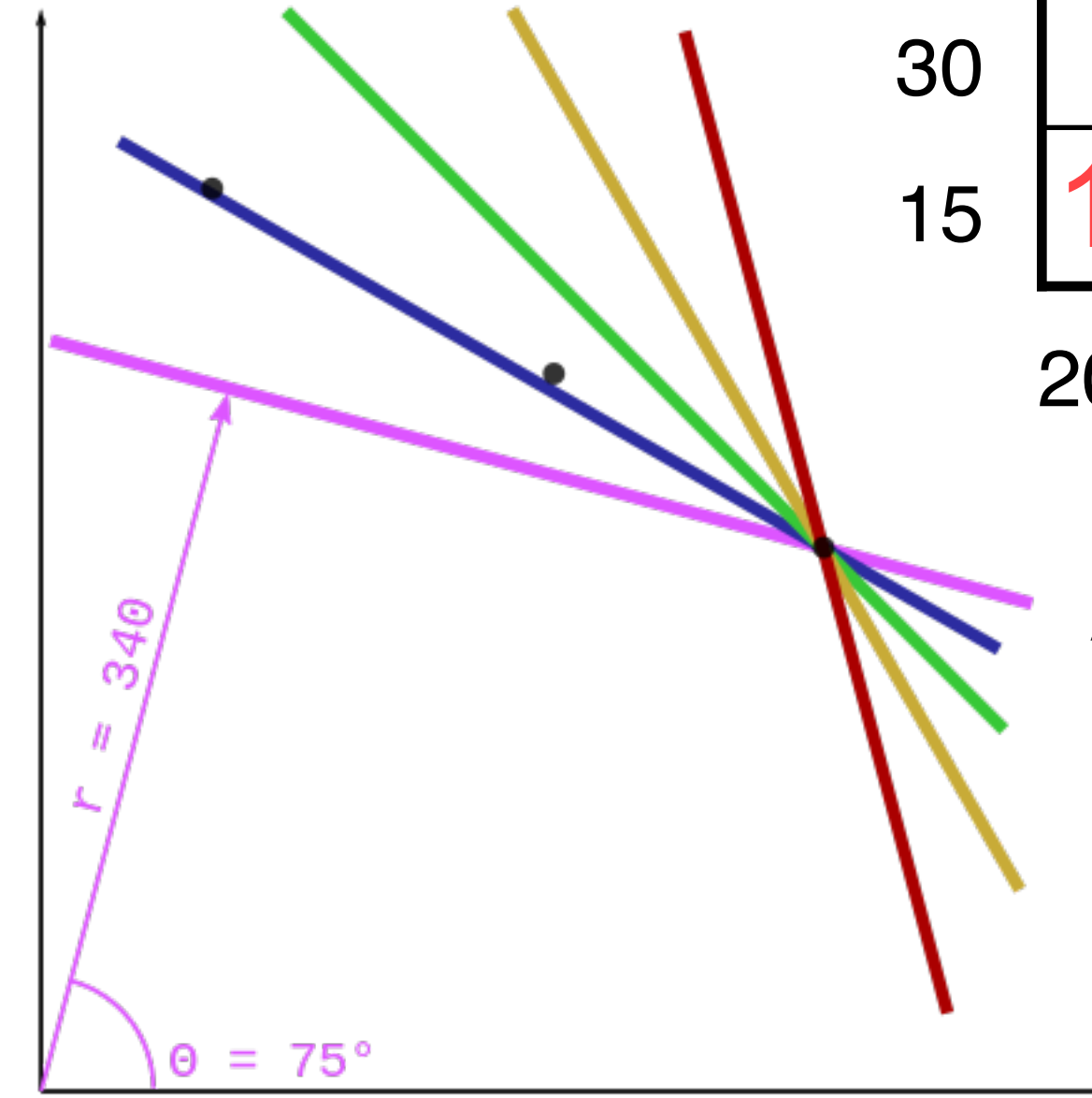
Hough transform for lines



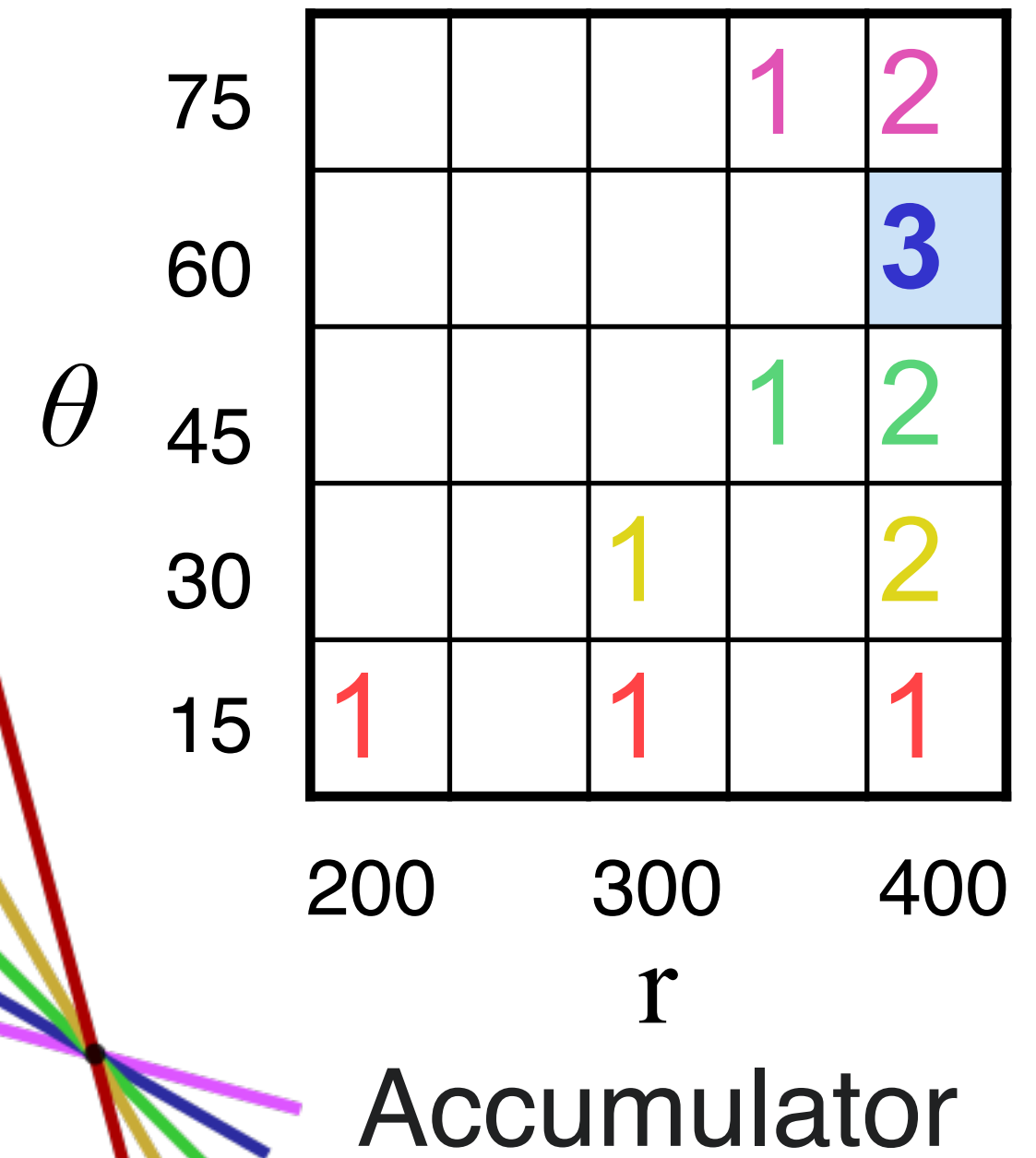
θ	r
15	189.0
30	282.0
45	355.7
60	407.3
75	429.4



θ	r
15	318.5
30	376.8
45	407.3
60	409.8
75	385.3



θ	r
15	419.0
30	443.6
45	438.4
60	402.9
75	340.1

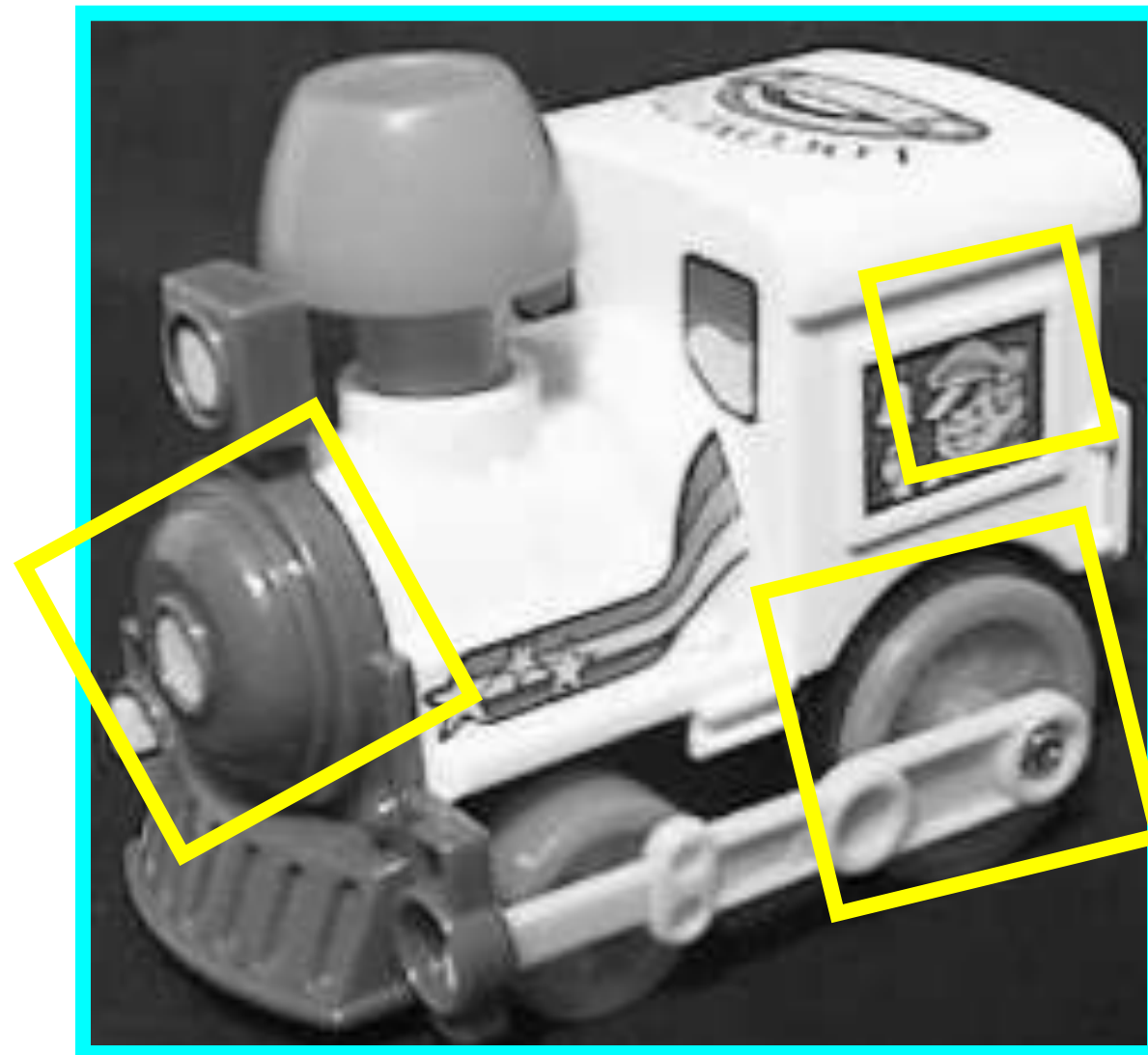


Hough transform for feature matching (object recognition)

Suppose our features are scale- and rotation-covariant

- Then a single feature match provides an alignment hypothesis: translation (t_x , t_y), scale (s), orientation (θ)
- Of course, a hypothesis obtained from a single match is unreliable
- Solution: Coarsely quantize the transformation space. Let each match vote for its hypothesis in the quantized space.

model



Hough transform for feature matching

Compute **similarity transformation** from a single correspondence:

$$(x_A, y_A, s_A, \theta_A) \leftrightarrow (x'_A, y'_A, s'_A, \theta'_A)$$



- Translation (t_x, t_y)
- Scale (s)
- Orientation (θ)

$$\theta = \theta'_A - \theta_A$$

$$s = s'_A / s_A$$

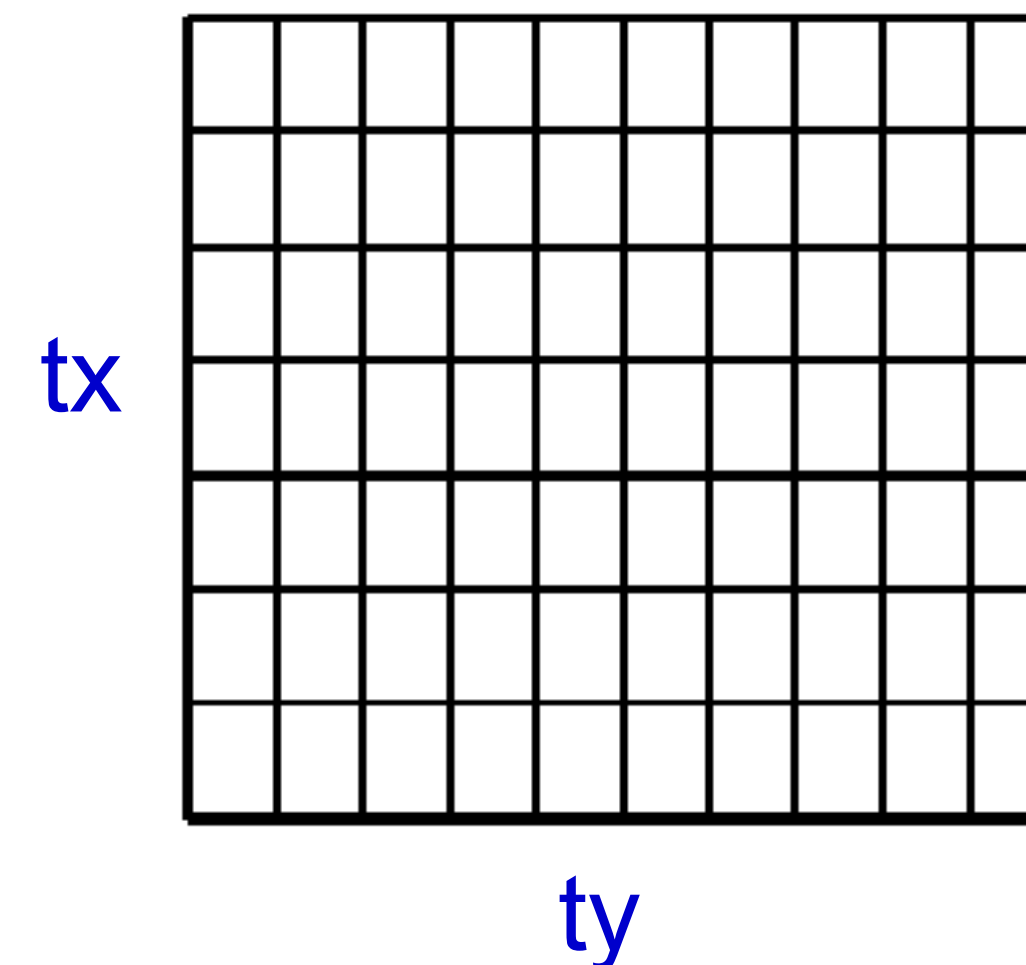
$$t_x = x'_A - sR(\theta)x_A$$

$$t_y = y'_A - sR(\theta)y_A$$

Basic algorithm outline

H: 4D-accumulator array
(only 2-d shown here)

1. Initialize accumulator H to all zeros.
2. For each tentative match:
 Compute transformation hypothesis: tx, ty, s, θ
 Increase vote $H(tx, ty, s, \theta) += 1$
end
3. Find all bins (tx, ty, s, θ) where $H(tx, ty, s, \theta)$ has at least 3 votes.



- Correct matches will consistently vote for the same transformation,
- while mismatches will spread votes.
- Cost:
 - Linear scan through the matches (step 2),
 - Followed by a linear scan through the accumulator (step 3).

Comparison

Hough Transform

•Advantages

- Can handle high percentage of outliers (>95%)
- Extracts groupings from clutter in linear time

•Disadvantages

- Quantization issues
- Only practical for small number of dimensions (up to 4)

•Improvements available

- Probabilistic Extensions
- Continuous Voting Space
- Can be generalized to arbitrary shapes and objects

RANSAC

•Advantages

- General method suited to large range of problems
- Easy to implement
- “Independent” of number of dimensions
- No accumulator needed, space-efficient, less prone to the choice of bin size

•Disadvantages

- Basic version only handles moderate number of outliers (<50%)
- More hypotheses may need to be generated and tested than those obtained by finding peaks in the accumulator array.

•Many variants available, e.g.

- PROSAC: Progressive RANSAC [Chum05]
- Preemptive RANSAC [Nister05]

Summary

- Finding correspondences in images is useful for
 - Image matching, panorama stitching
 - Object recognition
 - Image search
- Beyond local point matching
 - Semi-local relations
 - Global geometric relations:
 - Epipolar constraint
 - 3D constraint (when 3D model is available)
 - 2D tnfs: Similarity / Affine / Homography
 - Algorithms:
 - RANSAC
 - Hough transform

$$\mathbf{x}'^T \mathbf{F} \mathbf{x} = 0$$

$$\mathbf{x} = \mathbf{P} \mathbf{X}$$

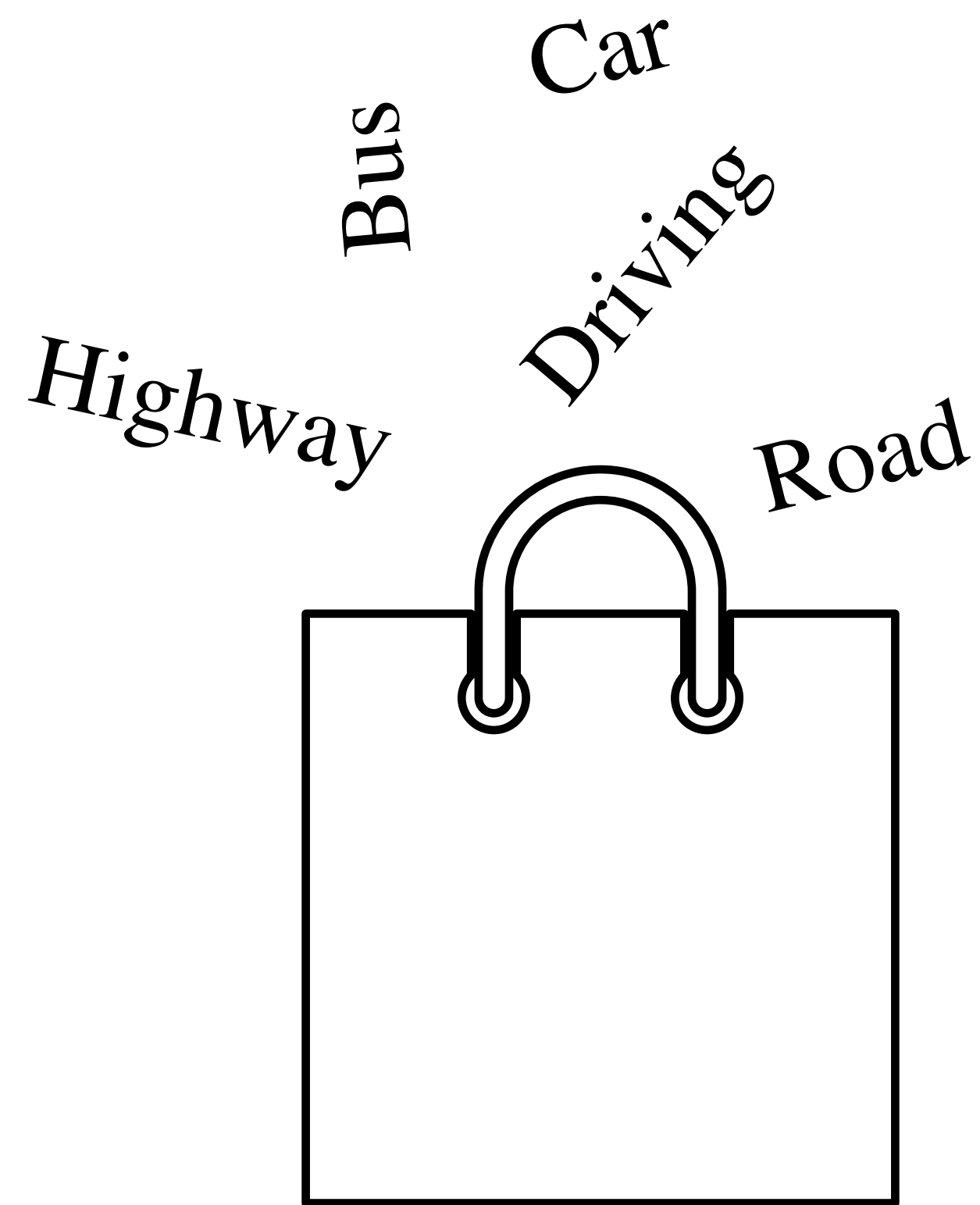
$$\mathbf{x}' = \mathbf{H} \mathbf{x}$$

Agenda: Instance-level recognition

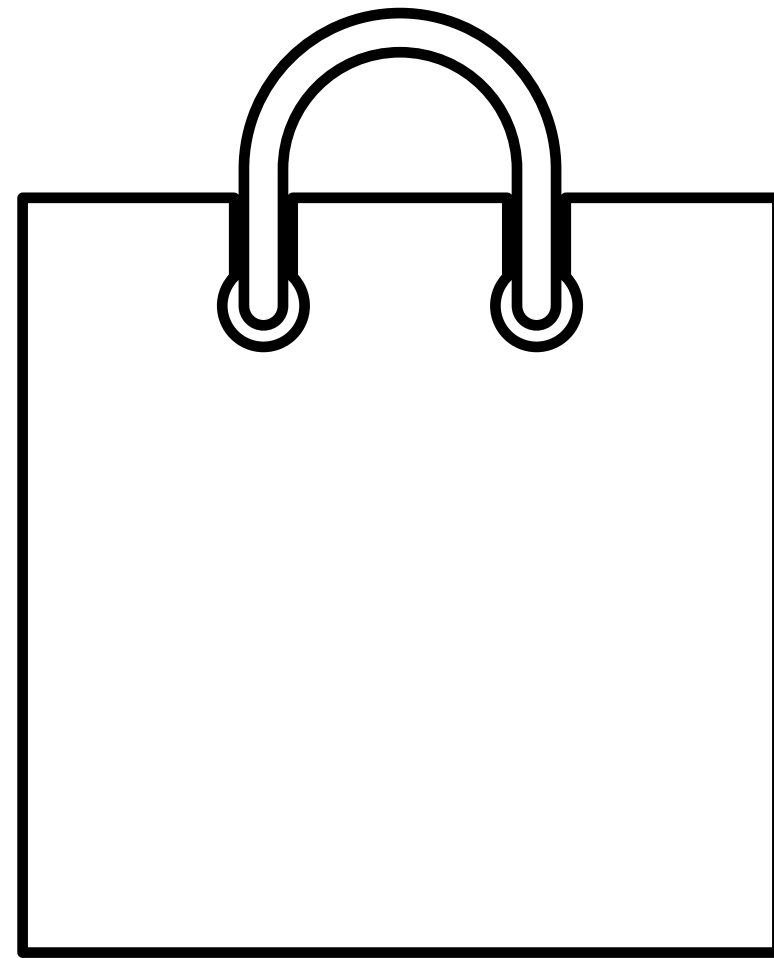
- 1) Introduction to local features
- 2) Interest point detectors (e.g., Harris, scale invariance)
- 3) Comparison of patches (SSD, ZNCC on pixel values)
- 4) Feature descriptors (e.g., SIFT)
- 5) Matching and recognition with local features
- 6) Local feature aggregation for a single image-level description

Need for aggregation

- Memory footprint of local features can be very high for one image.
- Example:
 - An image with 256×256 resolution (65536 pixels)
 - Densely extracted SIFT features from a grid of 32×32
 - $32 \times 32 = 1024$ features, each with 128-dimensions.
 - $1024 \times 128 = 131072$ -dimensional image feature
 - Bigger than the original pixel dimensionality.



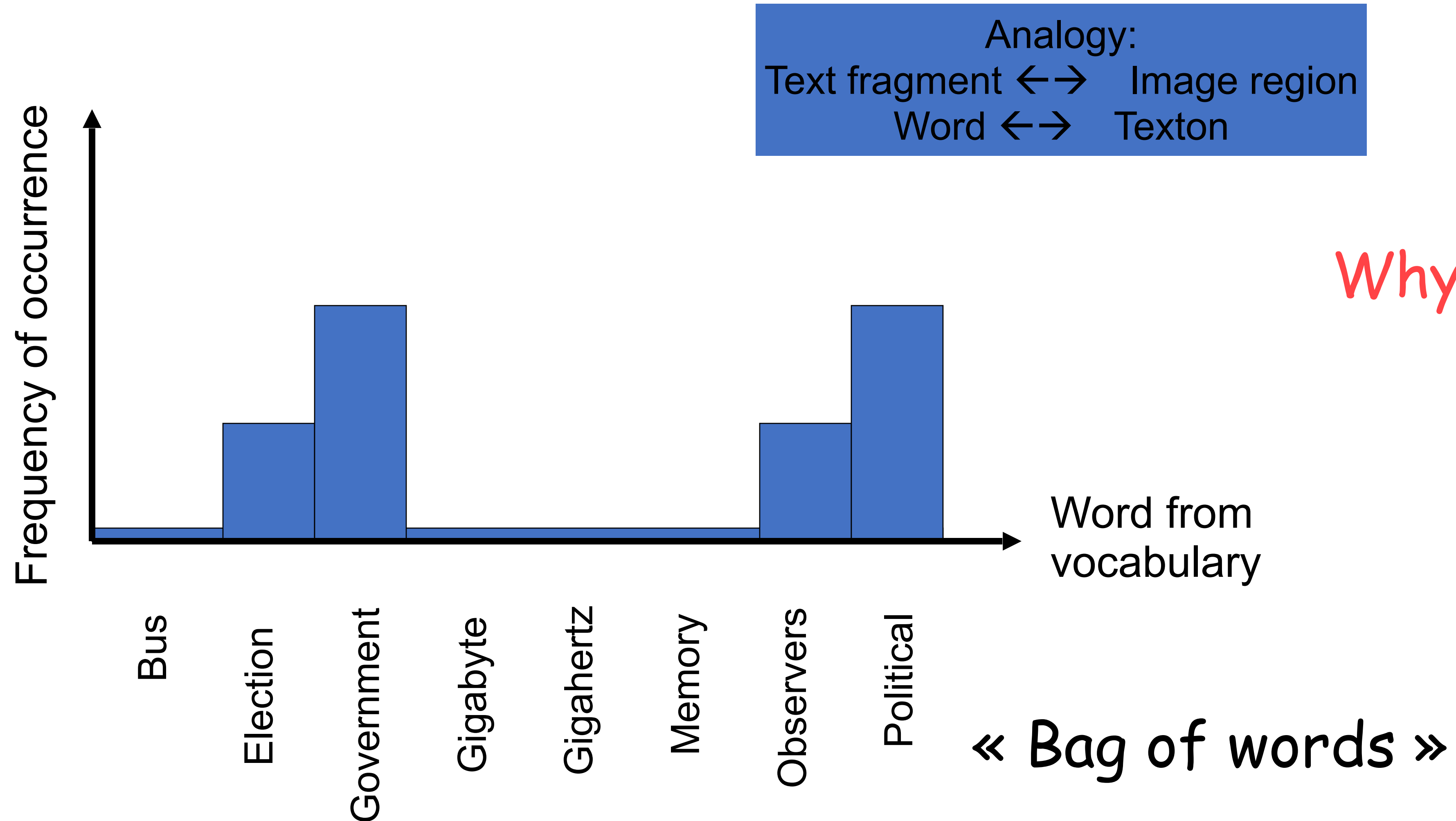
Bag of Words



Bag of **Visual Words**

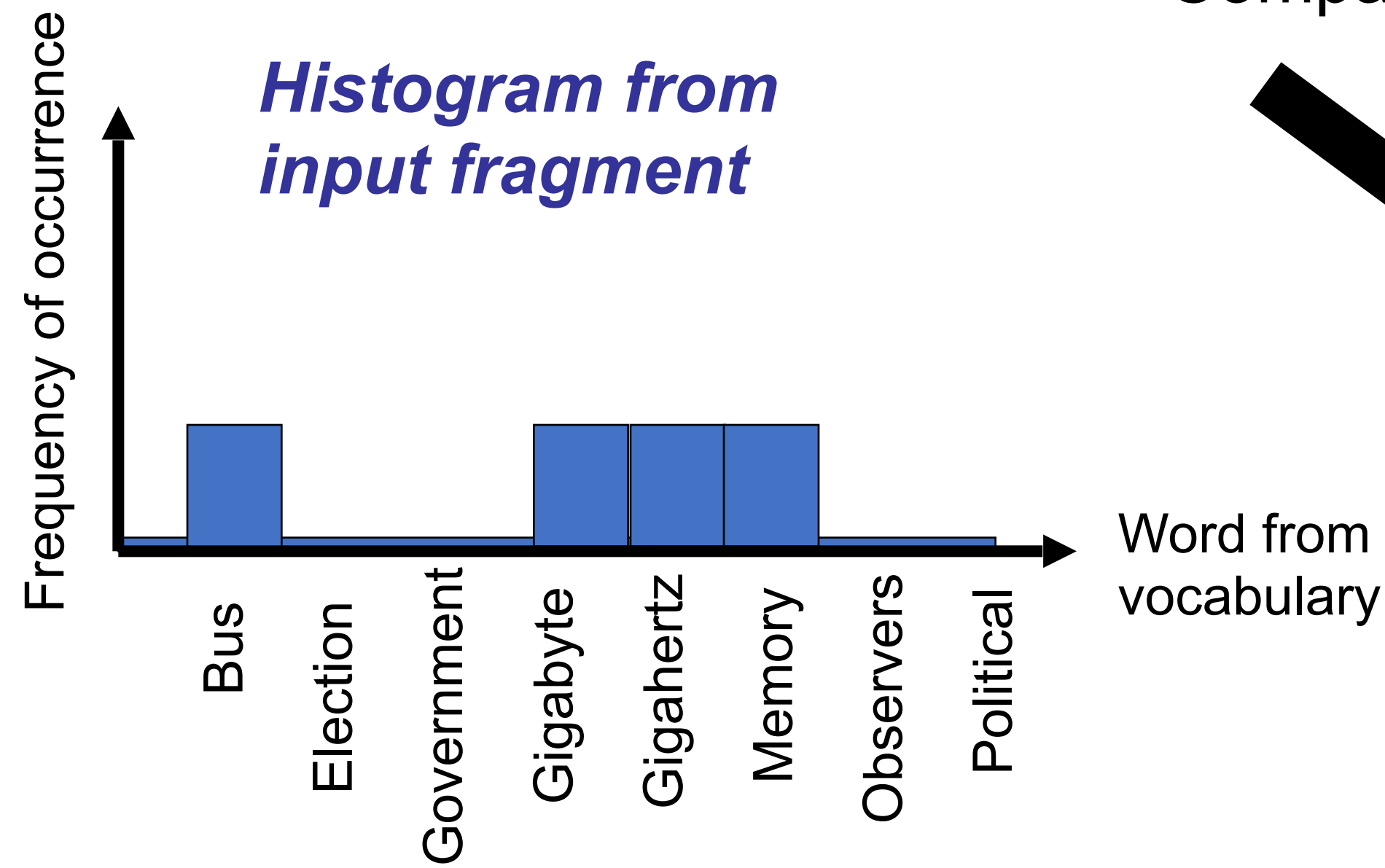
Analogy with Text Analysis

Political observers say that the government of Zorgia does not control the political situation. The government will not hold elections ...

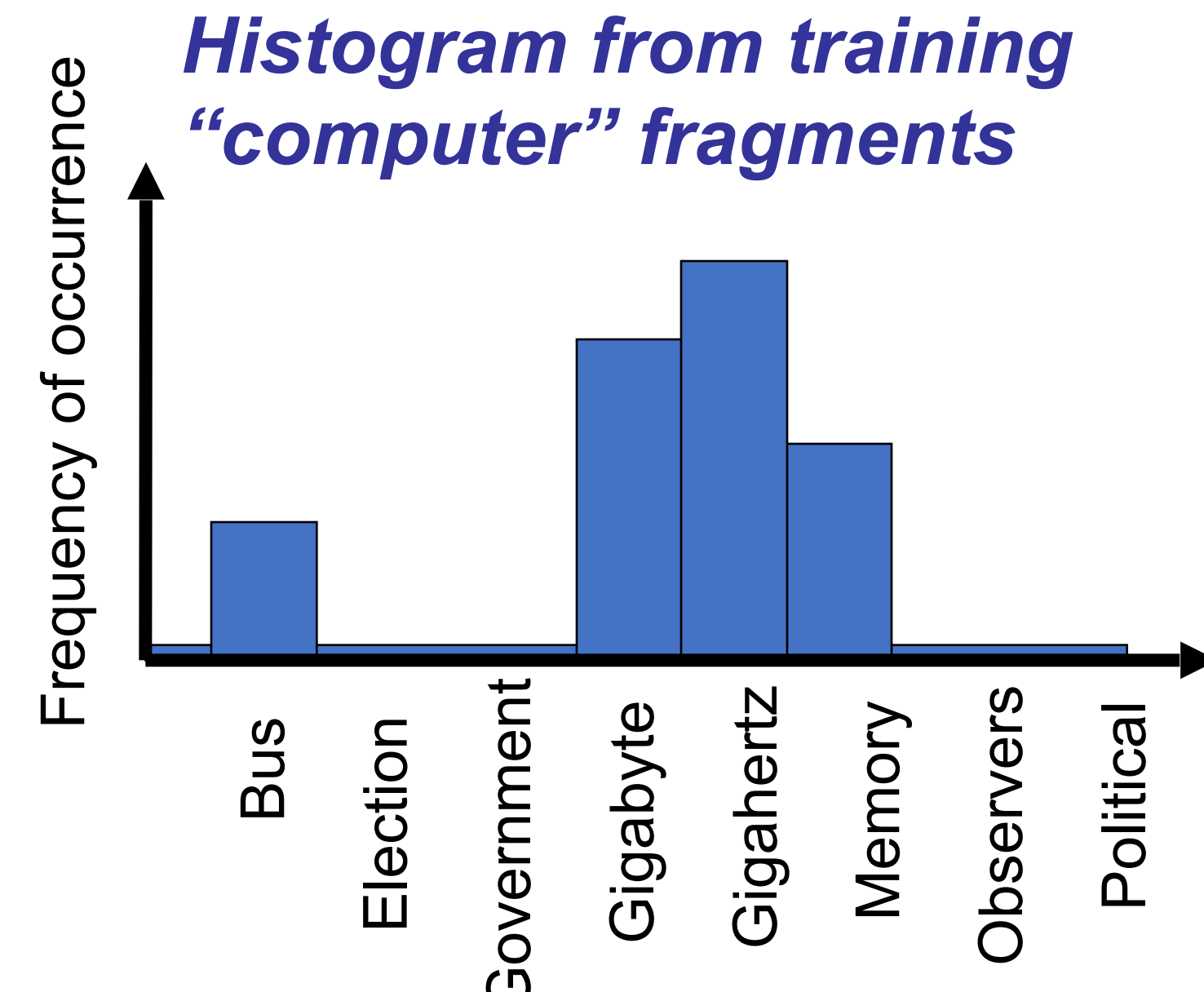
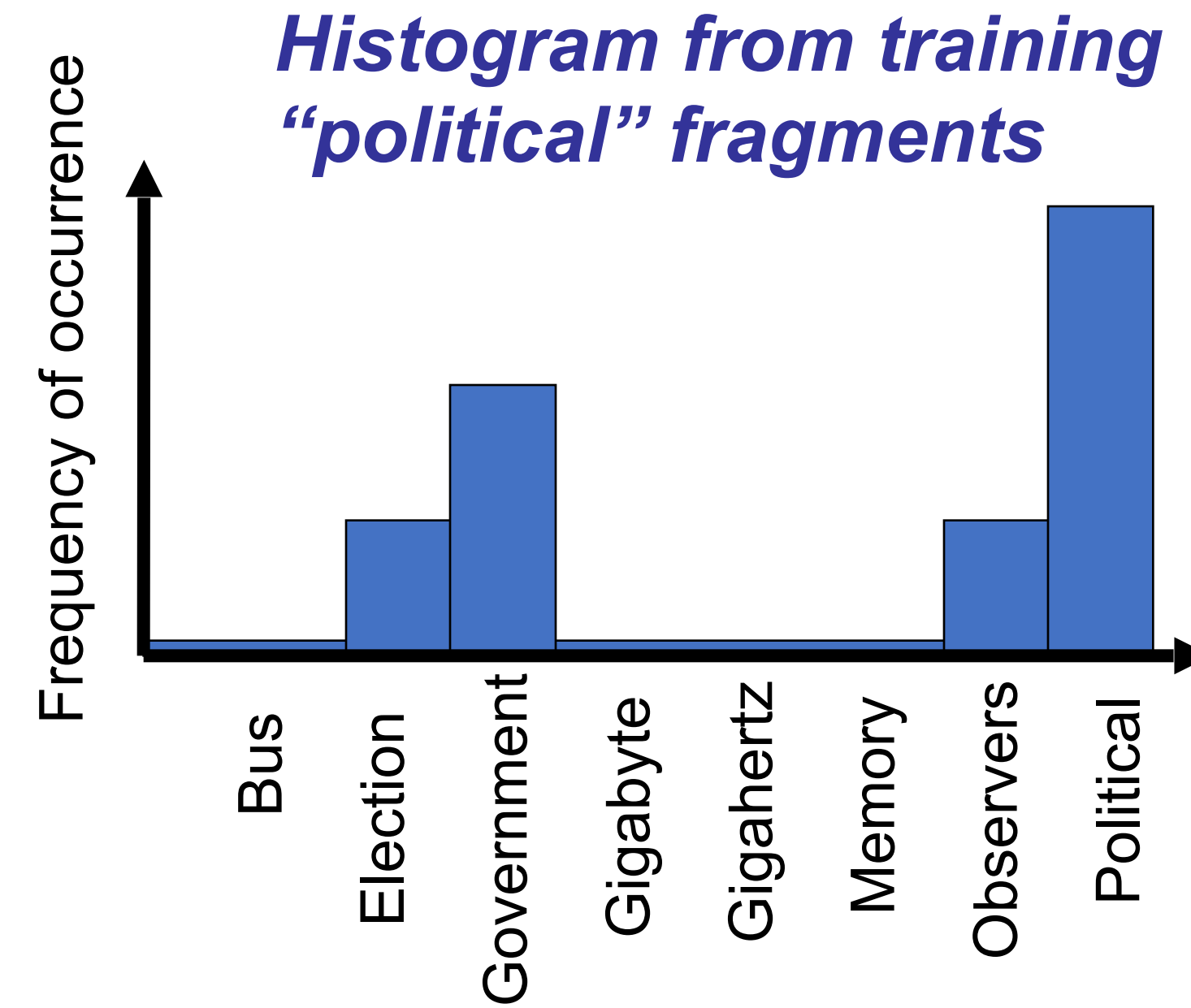


Analogy with Text Analysis

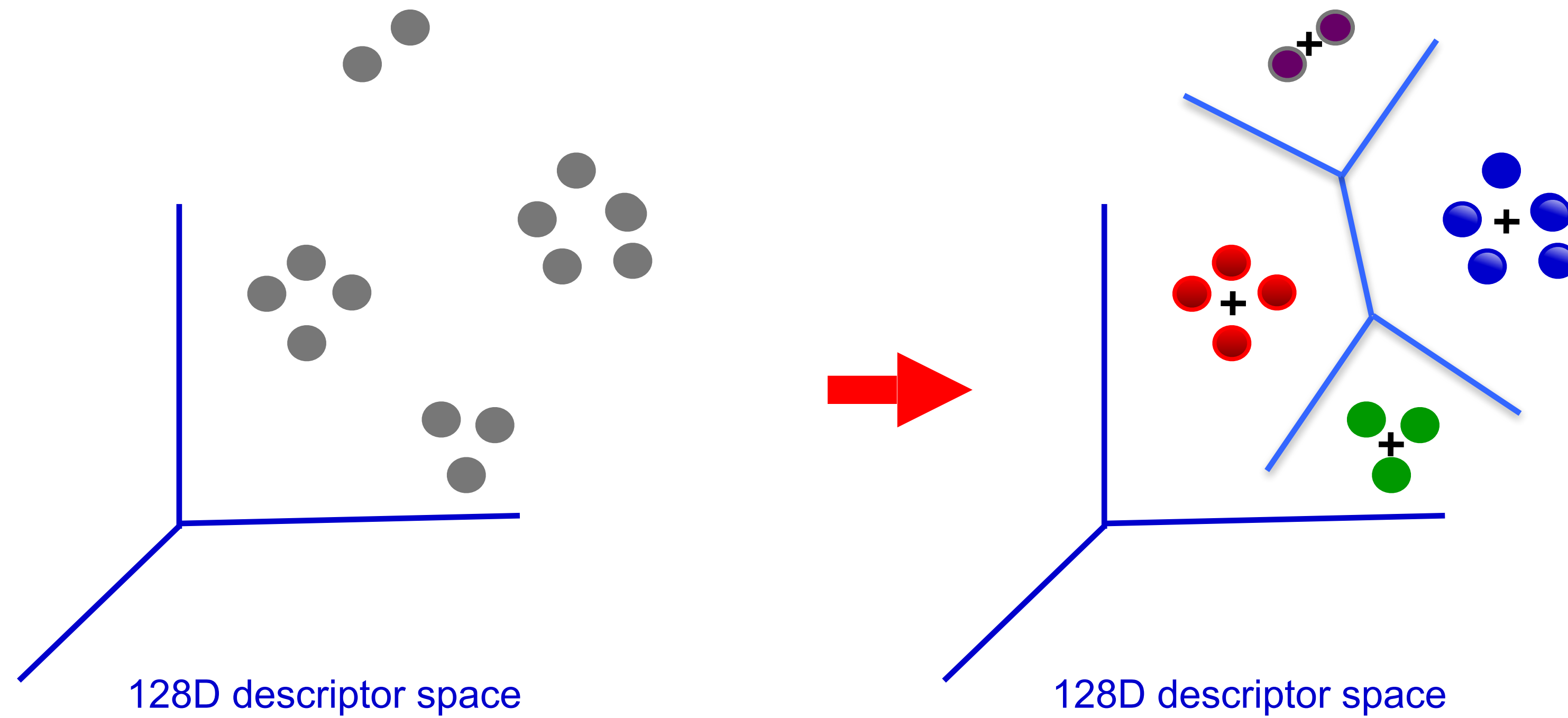
The ZH-20 unit is a 200Gigahertz processor with 2Gigabyte memory. Its strength is its bus and high-speed memory.....



Compare



Build a visual vocabulary

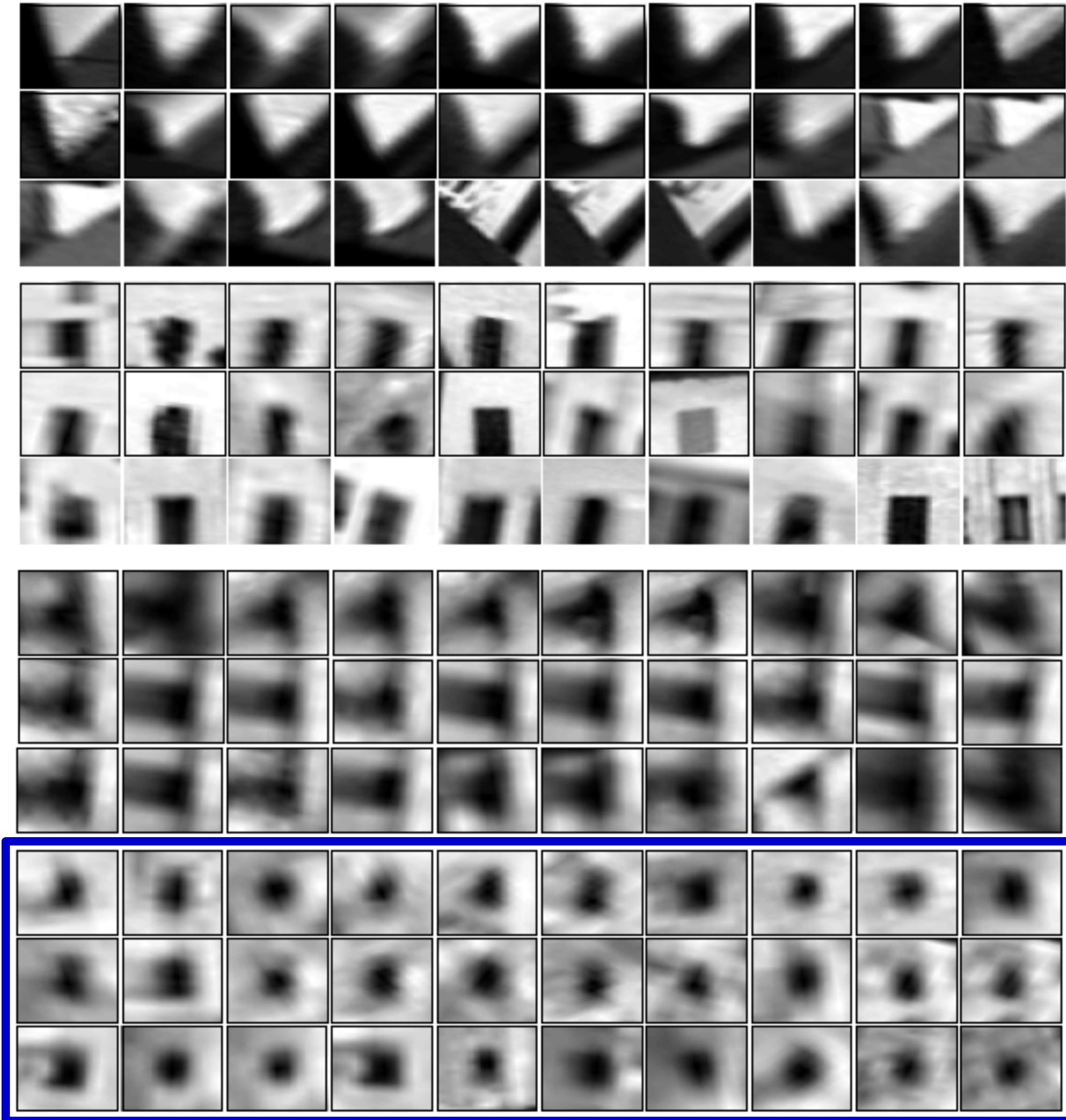
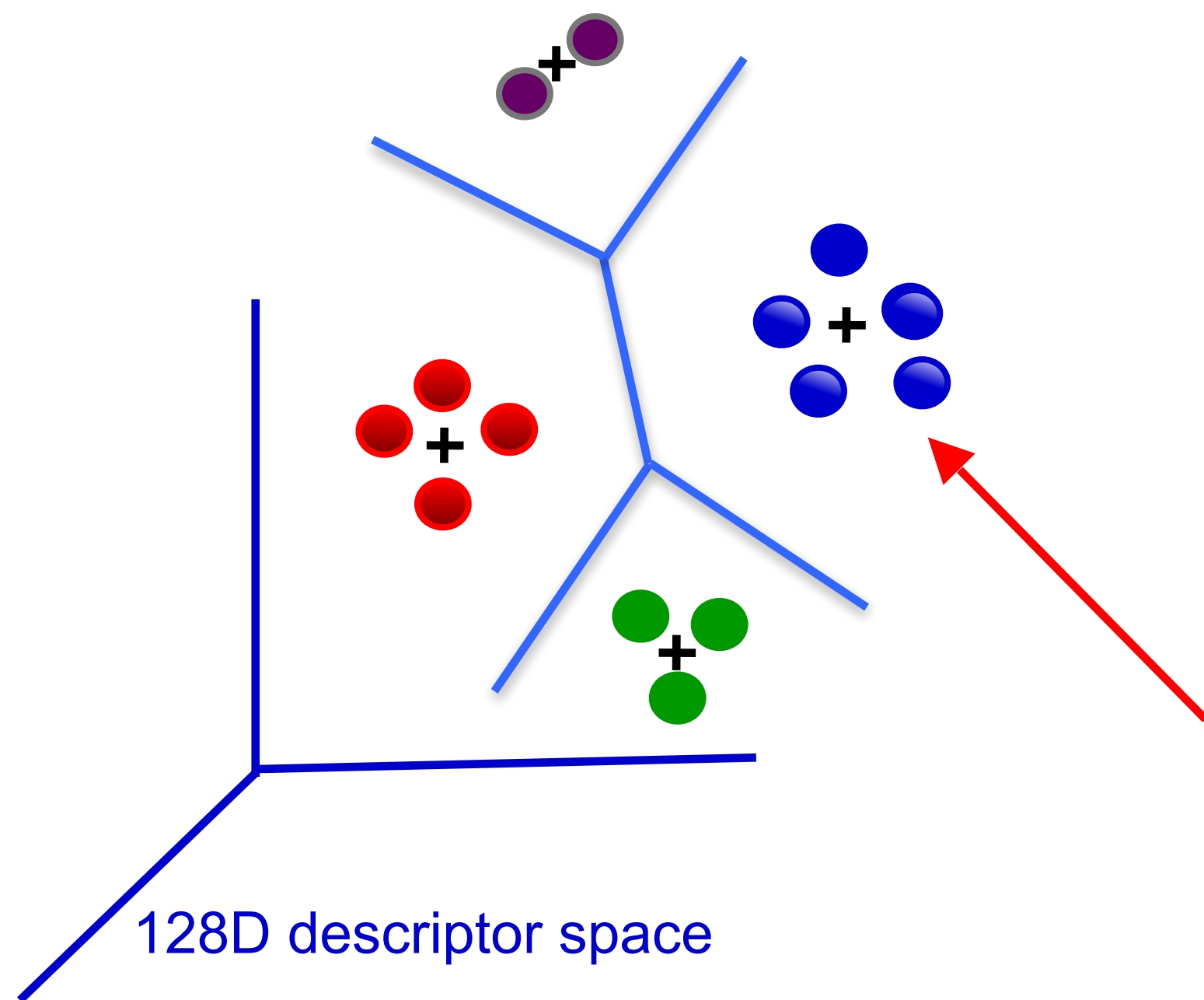


Vector quantize descriptors

- Compute SIFT features from a subset of images
- K-means clustering (need to choose K)

Visual words

Example: each group of patches belongs to the same visual word



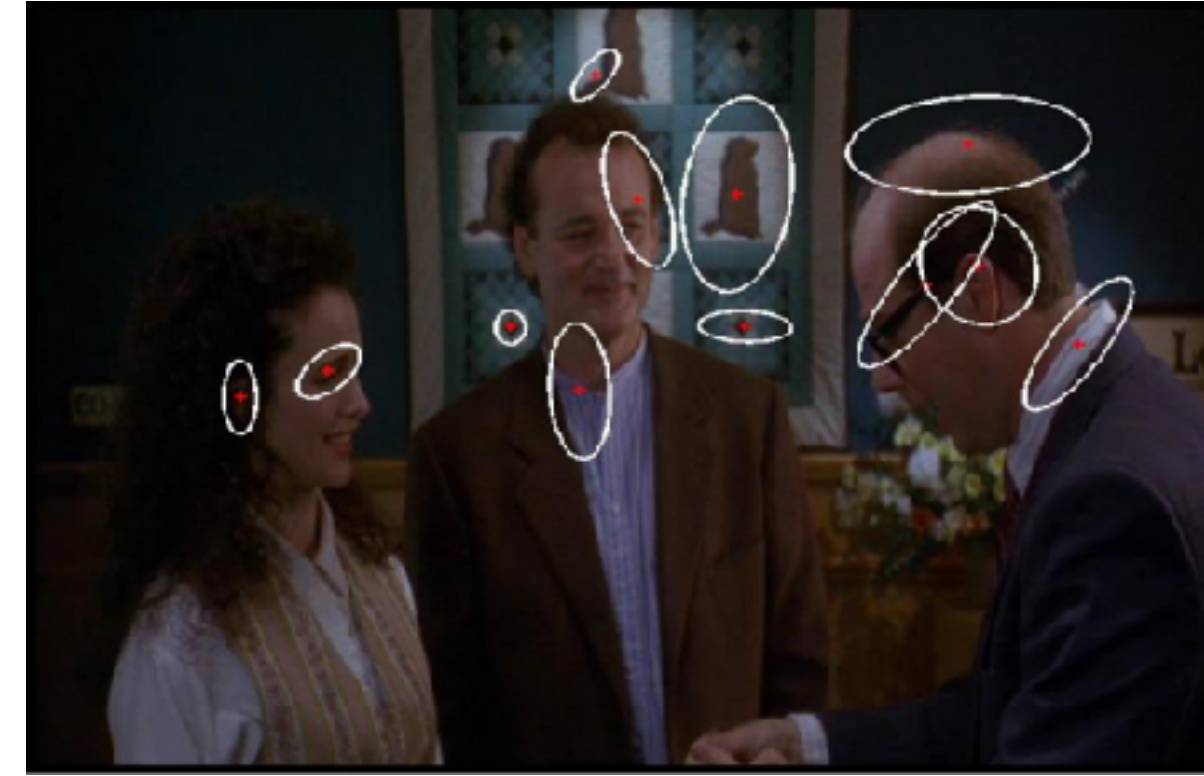
Step 1: feature extraction

Sparse sampling

- SIFT as interest point detector

Dense sampling

- Interest points do not necessarily capture “all” features



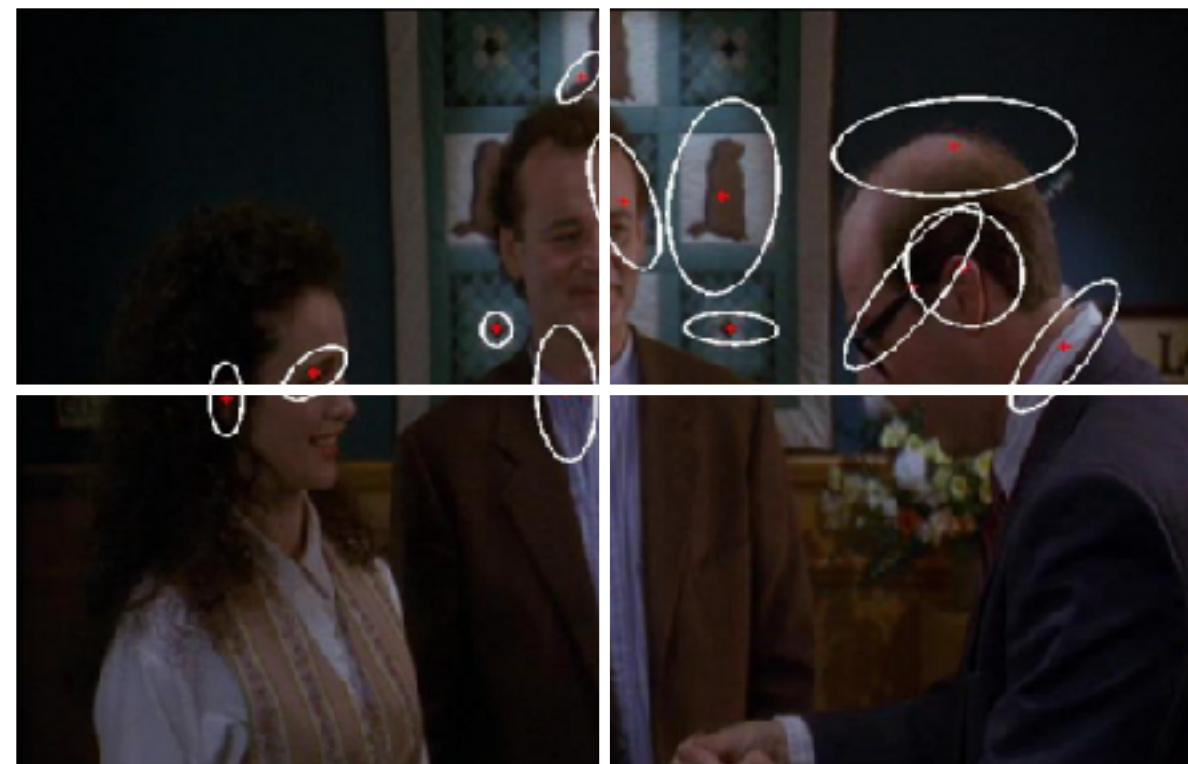
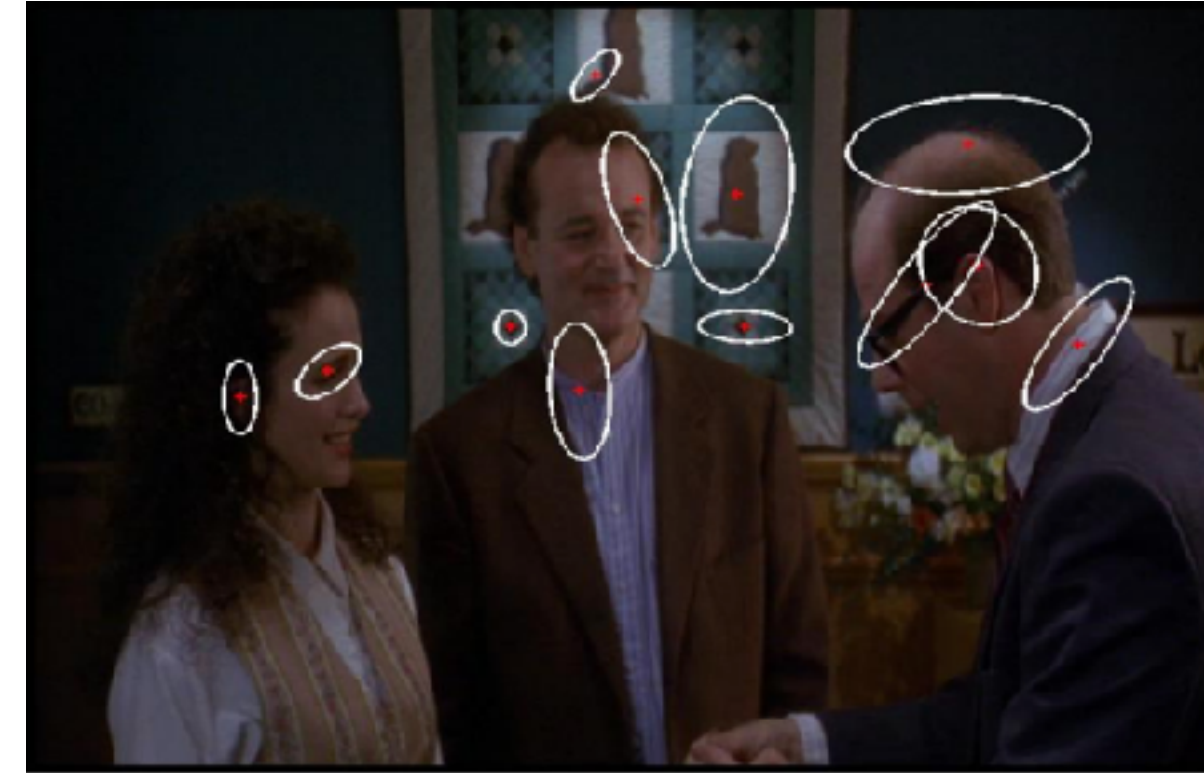
Step 1: feature extraction

Sparse sampling

- SIFT as interest point detector

Dense sampling

- Interest points do not necessarily capture “all” features
- Spatial pyramid (Lazebnik, Schmid & Ponce, CVPR 2006)



Step 2: Quantization

Cluster descriptors

- K-means
- Gaussian mixture model

Assign each visual word to a cluster

- Hard or soft assignment

Build frequency histogram

Examples for visual words

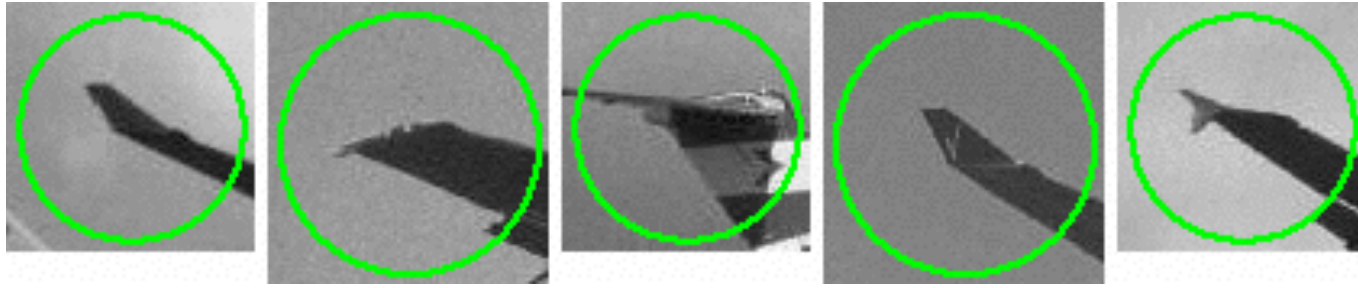



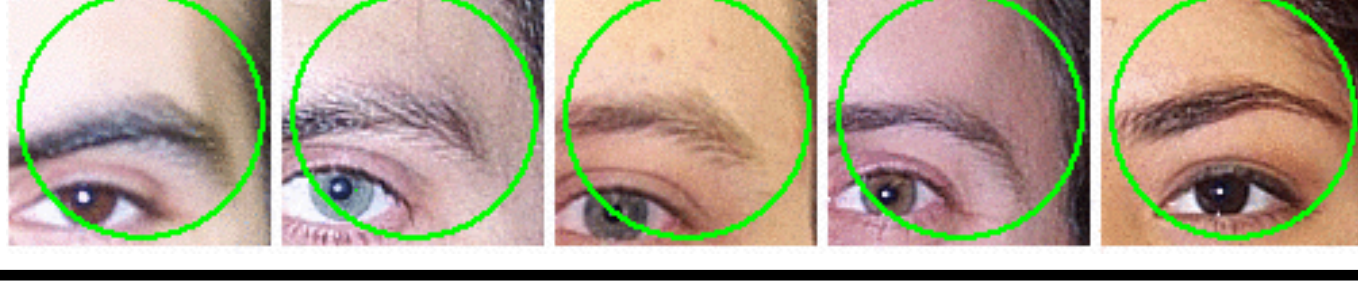
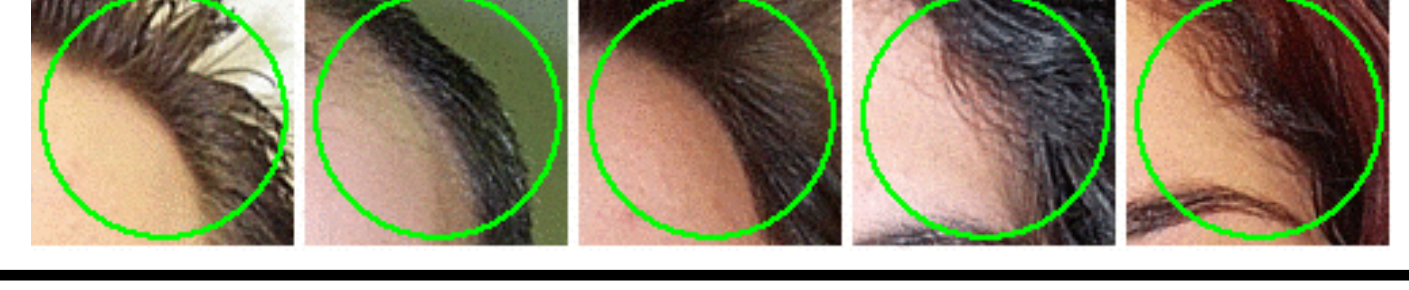



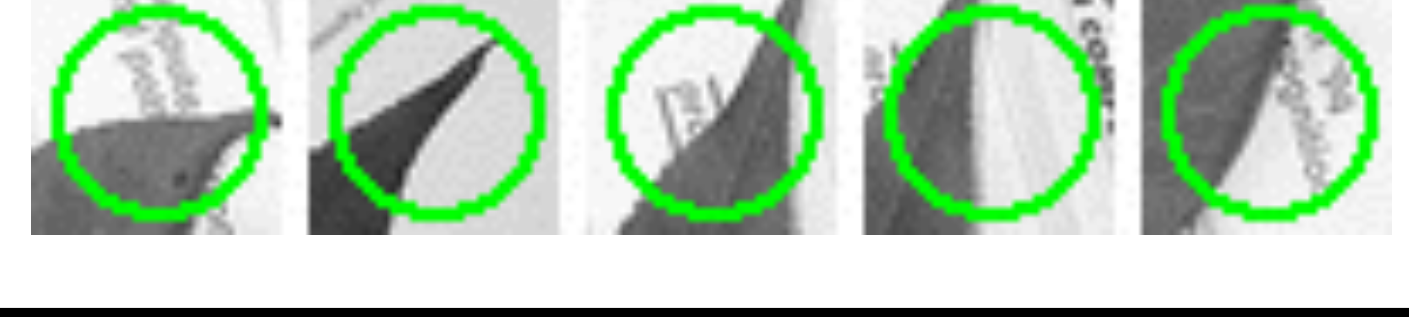

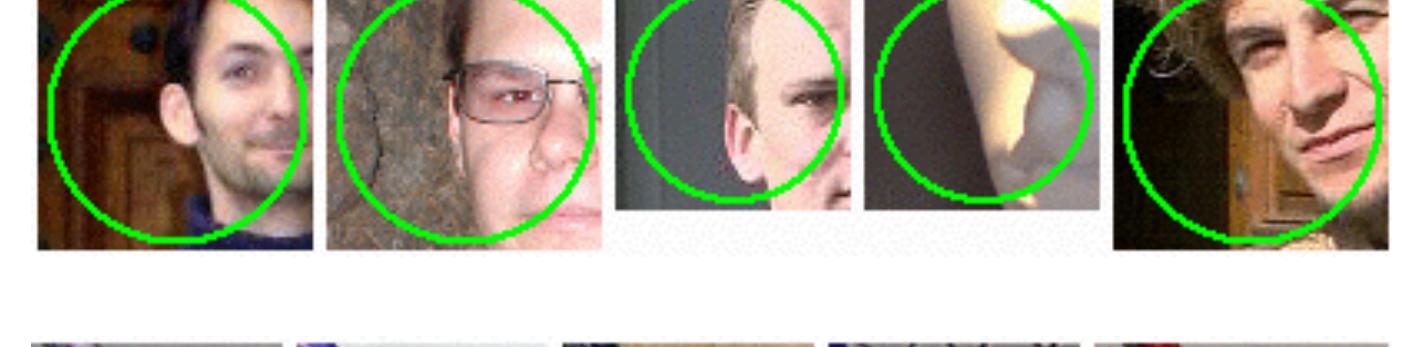
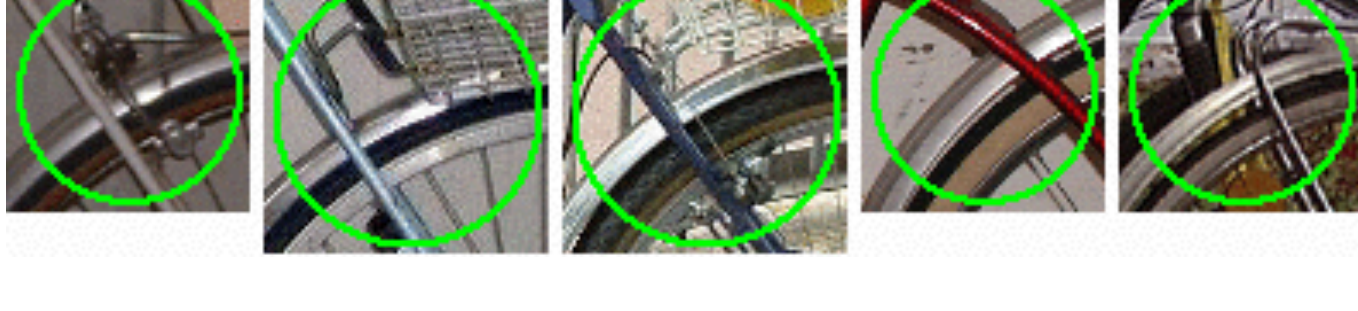

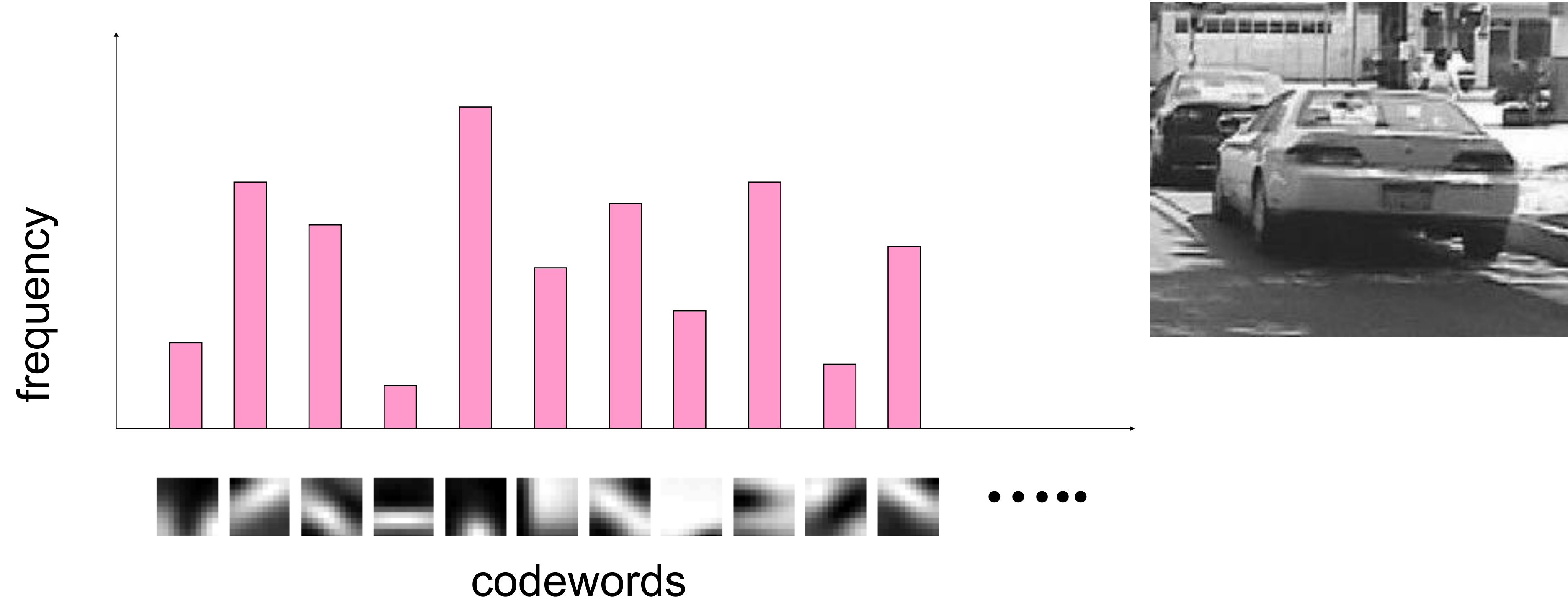
Airplanes		
Motorbikes		
Faces		
Wild Cats		
Leaves		
People		
Bikes		

Image representation



- Each image is represented by an aggregated histogram vector, typically 1000-4000 dimensional
- Normalized with L2 norm
- Fisher Vectors [Perronnin et al. ECCV'10]: improvements over Bag of Features

Agenda: Instance-level recognition

- 1) Introduction to local features
- 2) Interest point detectors (e.g., Harris, scale invariance)
- 3) Comparison of patches (SSD, ZNCC on pixel values)
- 4) Feature descriptors (e.g., SIFT)
- 5) Matching and recognition with local features
- 6) Local feature aggregation for a single image-level description